Problem 1

- **a.** Use the equations of stellar structure to find the mass-luminosity relation and the mass-radius relation of Main Sequence stars. You may use dimensional analysis and drop all constants to find simple proportionalities. For example, the mass conservation equation can reduce to $\rho \sim M/R^3$. Assume the equation of state for an ideal gas, nuclear fusion with the CNO cycle, and opacity is dominated by electron Thompson scattering.
- **b.** Make simple assumptions and estimate how the lifetime of such a Main Sequence star scales with the star's mass.
- **c.** Use the Stefan-Boltzmann relation to find the proportionality between luminosity L and effective temperature $T_{\it eff}$

Problem 2

On the course website (http://people.vanderbilt.edu/~a.berlind/teaching/352_sp08/), you will find a file called "cluster.dat". It contains four columns with measurements of 75 stars in a cluster that you made last time you went observing. The first two columns are Right Ascension and Declination (the star's coordinates), the third column is the star's V-band magnitude V, and the last column is the (B-V) color. Make a color-magnitude plot for the cluster using this data.

Problem 3

You were lucky enough to find a visual binary system in the cluster. After observing the system for many years, you found an angular binary separation of $\alpha = 0.388''$ and an orbital period of P = 53.98 years. You also measured the two stars' V-band magnitudes to be $V_1 = 8.44$ and $V_2 = 9.21$. Using the mass-luminosity relation you found from theory (normalized to the sun), determine the system's distance, parallax, masses, and absolute magnitudes M_V for the two stars. Iterate your solution until it converges (you should get convergence after 2-3 iterations so you don't need a computer to do this). You can use the fact that the absolute V-band magnitude for the sun is 4.83, and bolometric corrections are approximately constant for most stars.

Problem 4

Now that you have a distance to the cluster, convert the 75 V-band magnitudes into absolute magnitudes. You can now make a M_V vs. (B-V) plot and compare it to the theoretical $L-T_{eff}$ relation you found above to see how well the theory does. To do this, you need to convert the $L-T_{eff}$ relation into a $M_V-(B-V)$ relation. You can follow these steps:

a. Make a finely spaced (e.g., every 100K) table of values for T_{eff} , running from 3500K to 40,000K (corresponding to the temperature sequence from M stars to O stars). For each value of temperature compute a luminosity using the $L-T_{eff}$ relation (again, normalized to the sun: $L=L_{sun}$, $T_{eff}=5,778K$).

b. For each temperature, compute the predicted (B-V) color by convolving the blackbody spectrum for that temperature with the B and V-band filter response functions to compute the expected flux in each band. You can find these functions in the file "BV_filters.dat", also on the course website. The file has 3 columns: wavelength in nm, transmittance of B filter, transmittance of V filter (transmittance is the fraction of light that passes through the filter). The blackbody spectrum as a function of wavelength is:

$$B_T(\lambda) = \frac{2hc^2}{\lambda^5} \frac{1}{\exp(hc/\lambda kT - 1)}$$
, and the flux in a given filter is $\int_0^\infty B(\lambda)F(\lambda)d\lambda$, where

- $F(\lambda)$ is the filter transmittance function. (Note: all colors are defined to be zero for A0 stars with $T_{\rm eff} = 9500 K$ so you need to subtract from all colors the value for that temperature)
- **c.** Convert the luminosities to absolute V-band magnitudes, using the fact that the absolute bolometric magnitude of the sun is 4.75 and the average bolometric correction for stars like the sun is approximately 0.2.
- **d.** Now plot your theoretical $M_V (B V)$ on top of your observed one to see how well they agree. List the main assumptions you made in your theoretical calculation.

Problem 5 - optional for extra credit

If the above problems take you less time than I anticipate and you feel like challenging yourself more, look at the spectra of 5 stars on the course website (labeled star1 – star5) and classify them as best you can into spectroscopic classes, looking up whatever information you need. The files list wavelength in Angstroms and flux.