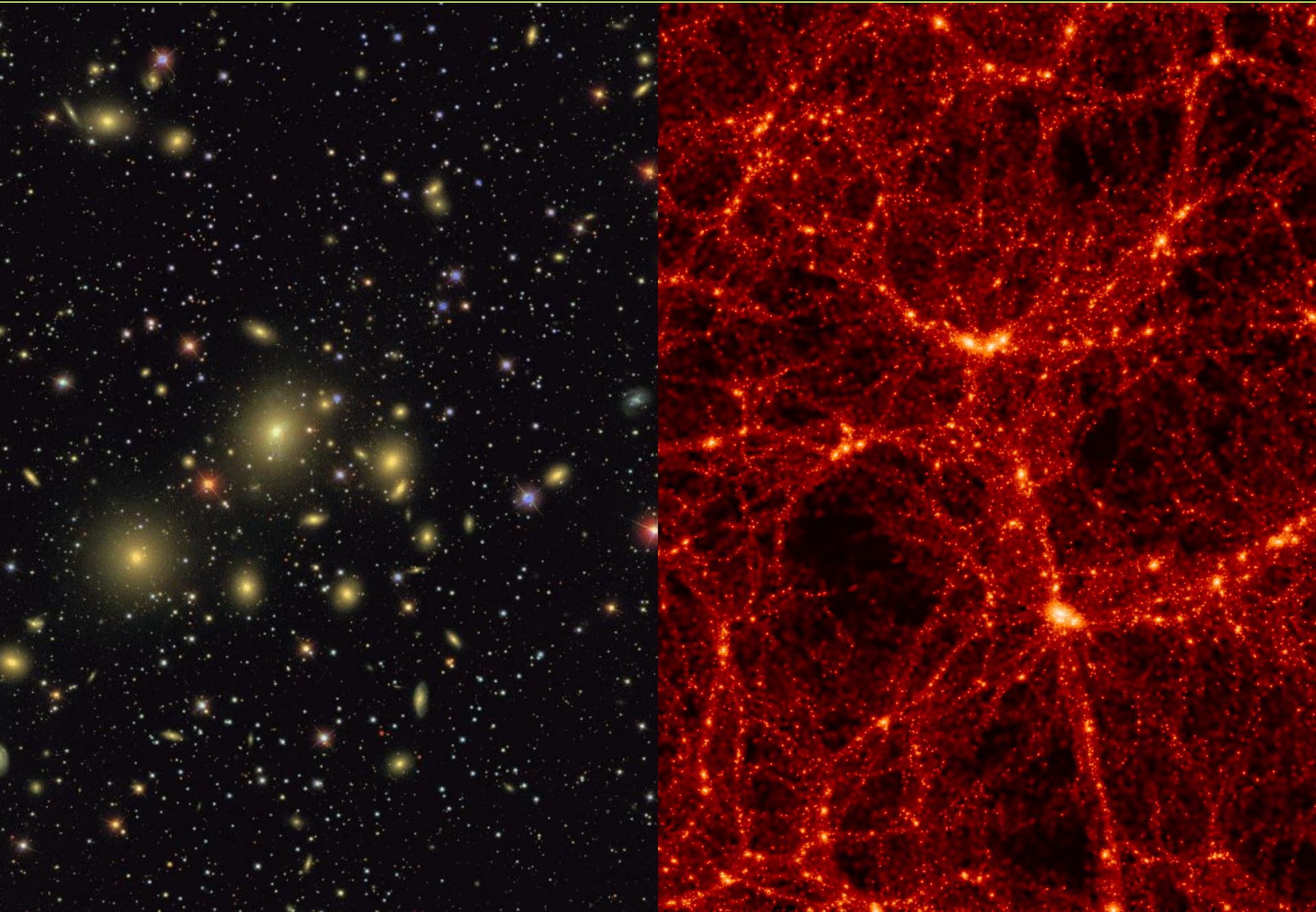
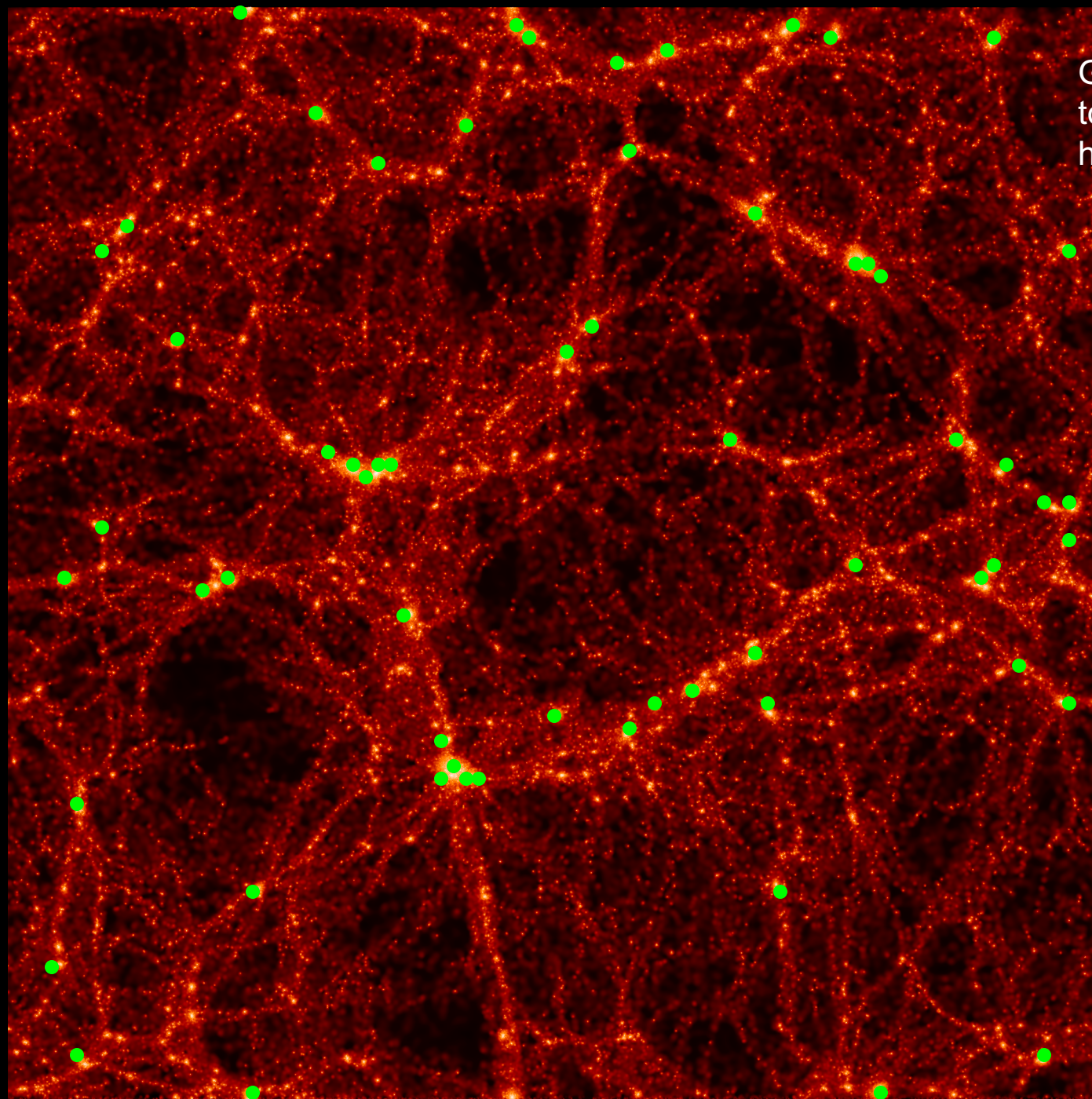


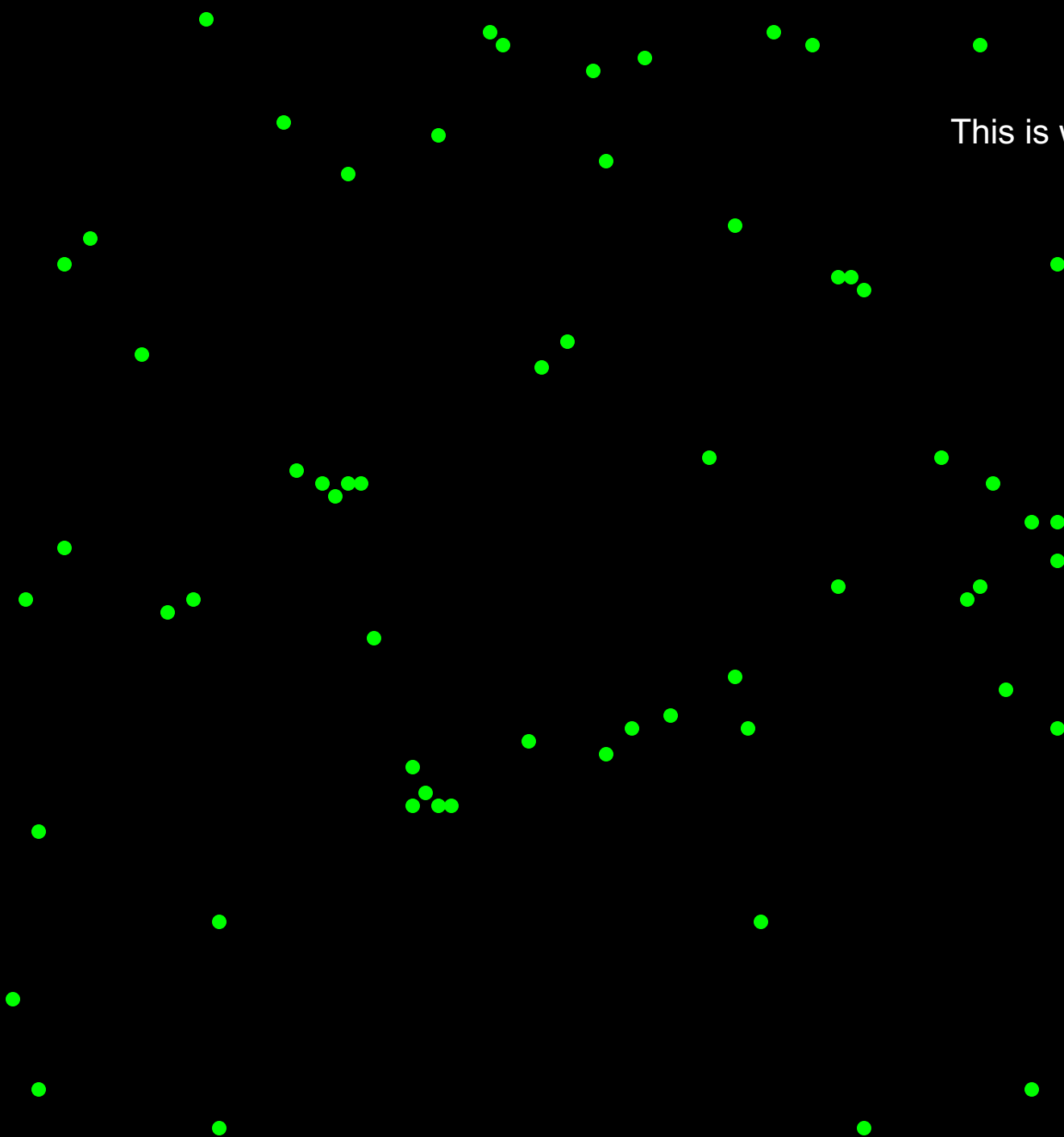
# From dark matter to galaxies





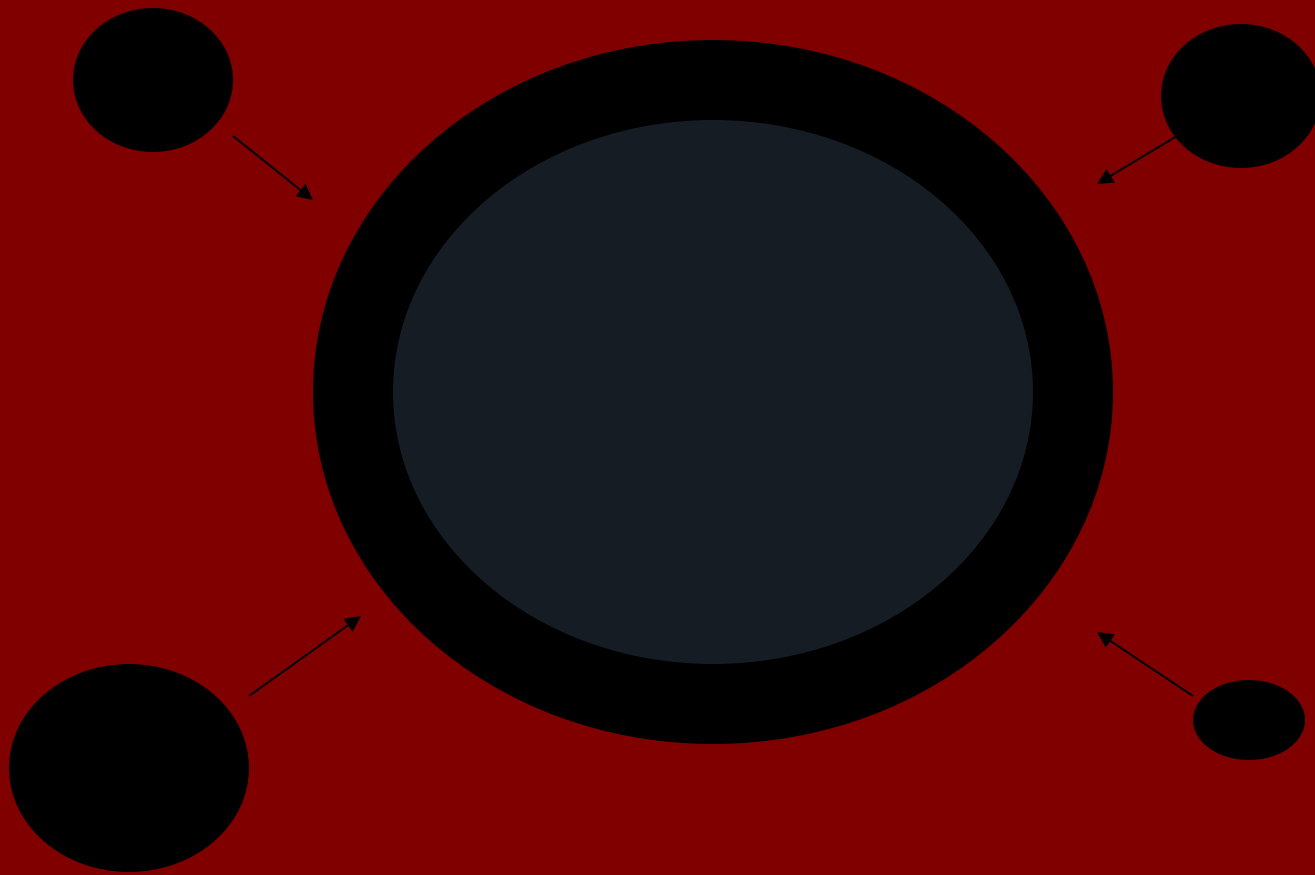
Galaxies are assumed to form in dark matter halos.

This is what we see!



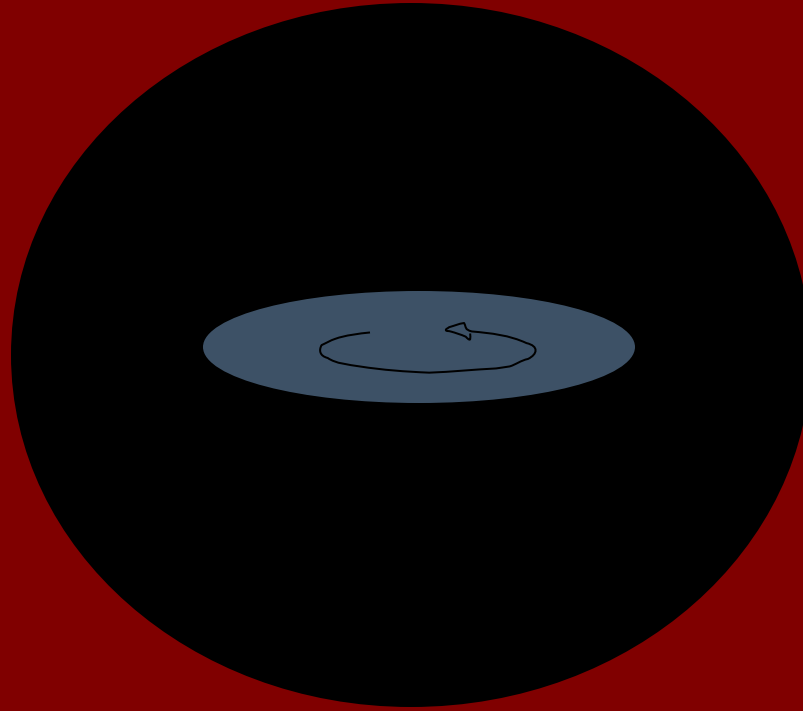
# Galaxy formation theory in a nutshell

A dark matter halo forms. Inside the halo is hot/warm gas.  
The gas has some angular momentum.



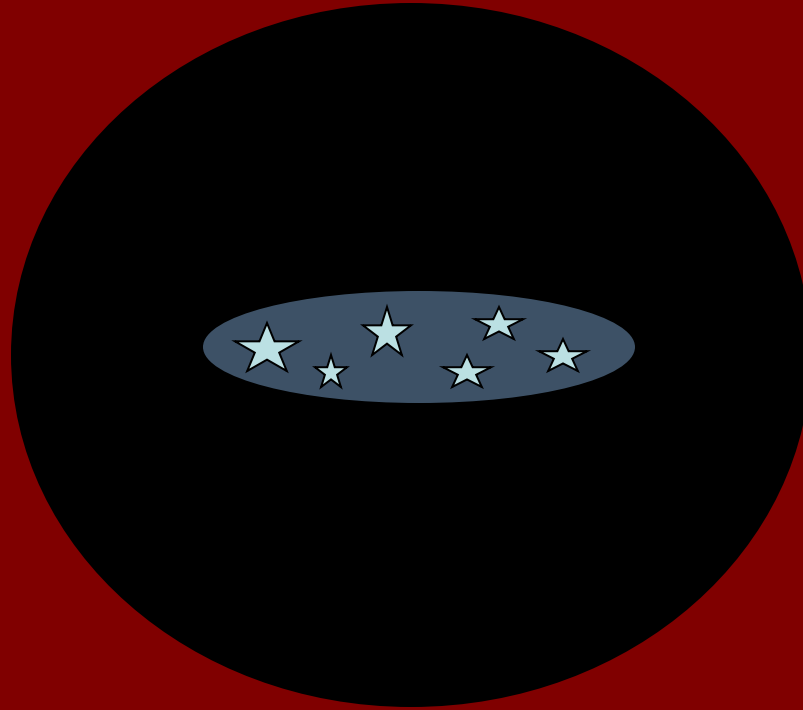
# Galaxy formation theory in a nutshell

Gas cools inside the halo and settles into a rotating disk.



# Galaxy formation theory in a nutshell

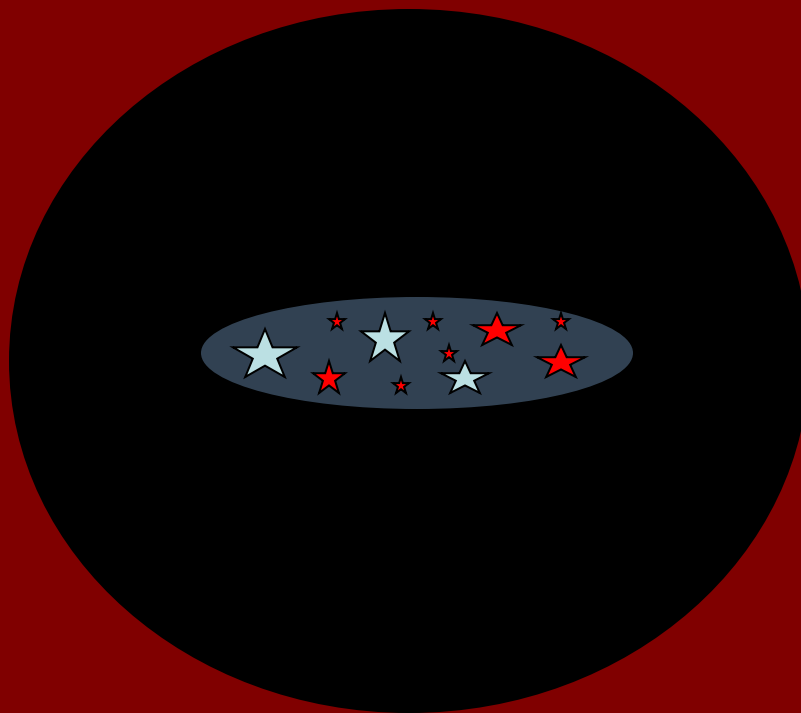
Stars form from the cold dense gas.



SF: ON

# Galaxy formation theory in a nutshell

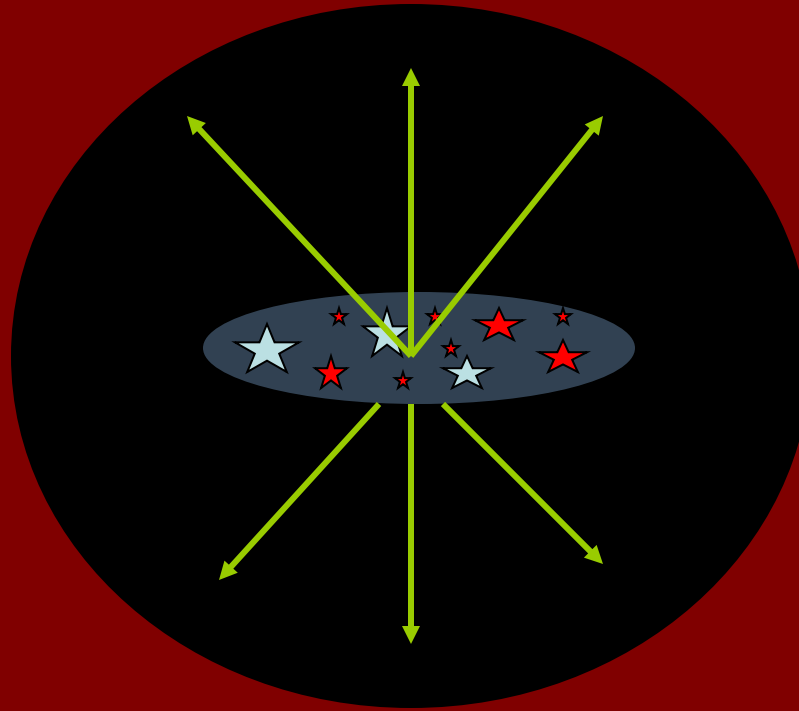
Stellar populations grow old and fade, new stars are born.  
Gas undergoes heating and cooling.



SF: ON

# Galaxy formation theory in a nutshell

Energy feedback due to supernovae or a massive central black hole can reheat the gas or blow it out of the galaxy.  
This can end star formation.

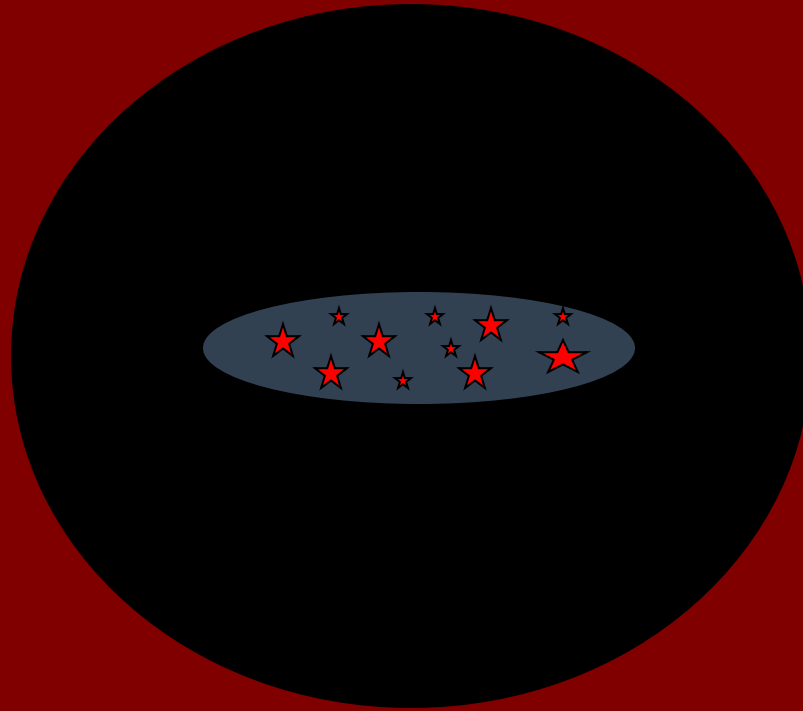


SF: OFF



# Galaxy formation theory in a nutshell

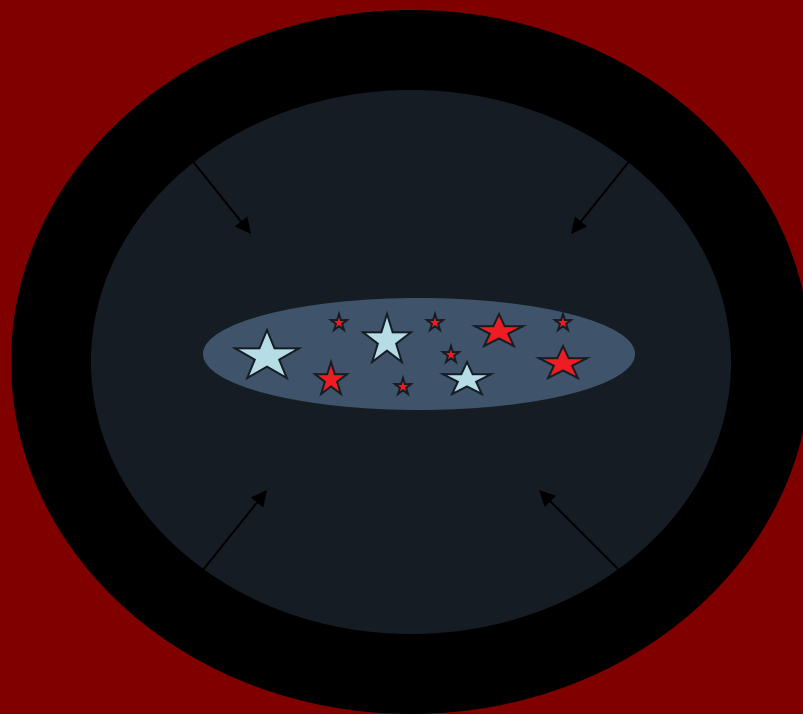
The galaxy gets dimmer and redder.



SF: OFF

# Galaxy formation theory in a nutshell

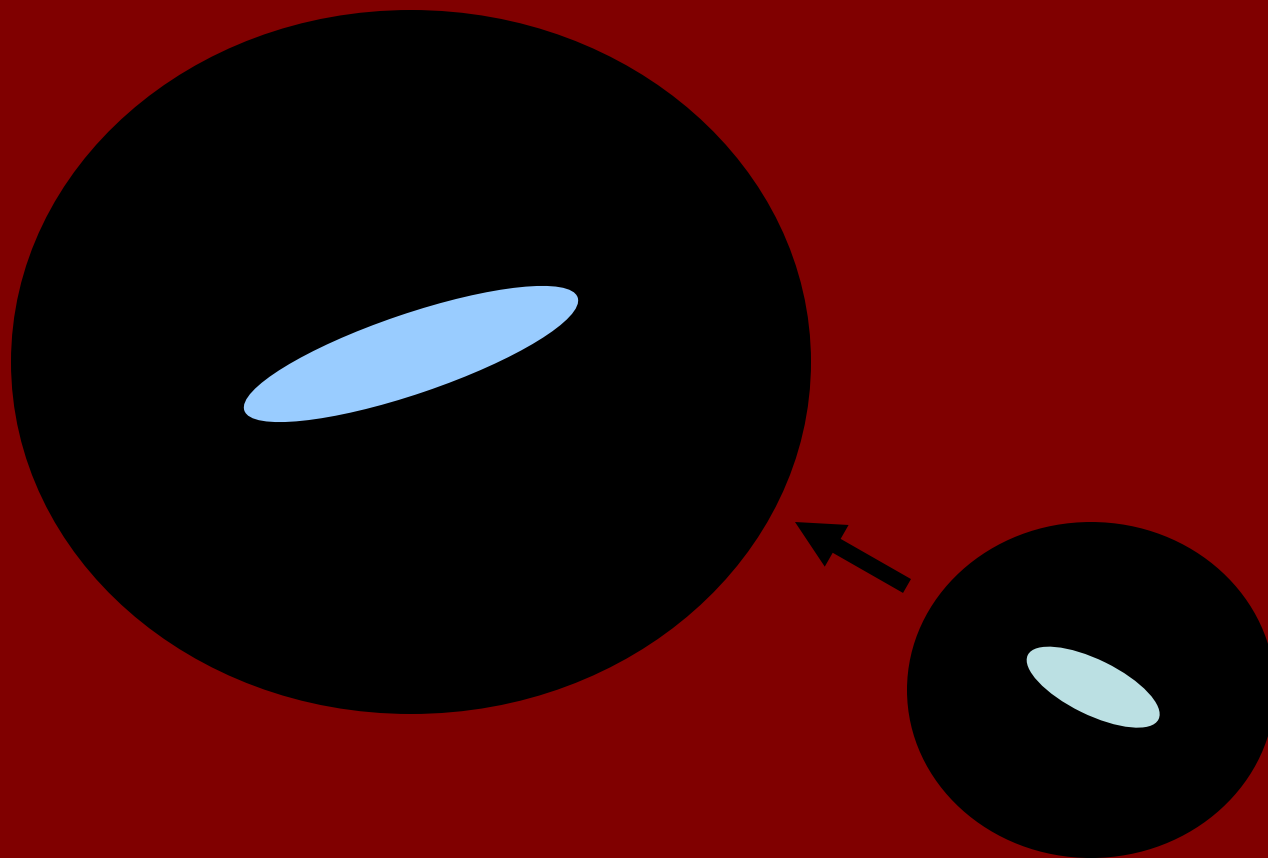
If the halo is in a gas-rich environment, more gas can fall into the halo from the inter-galactic medium.



SF: ON

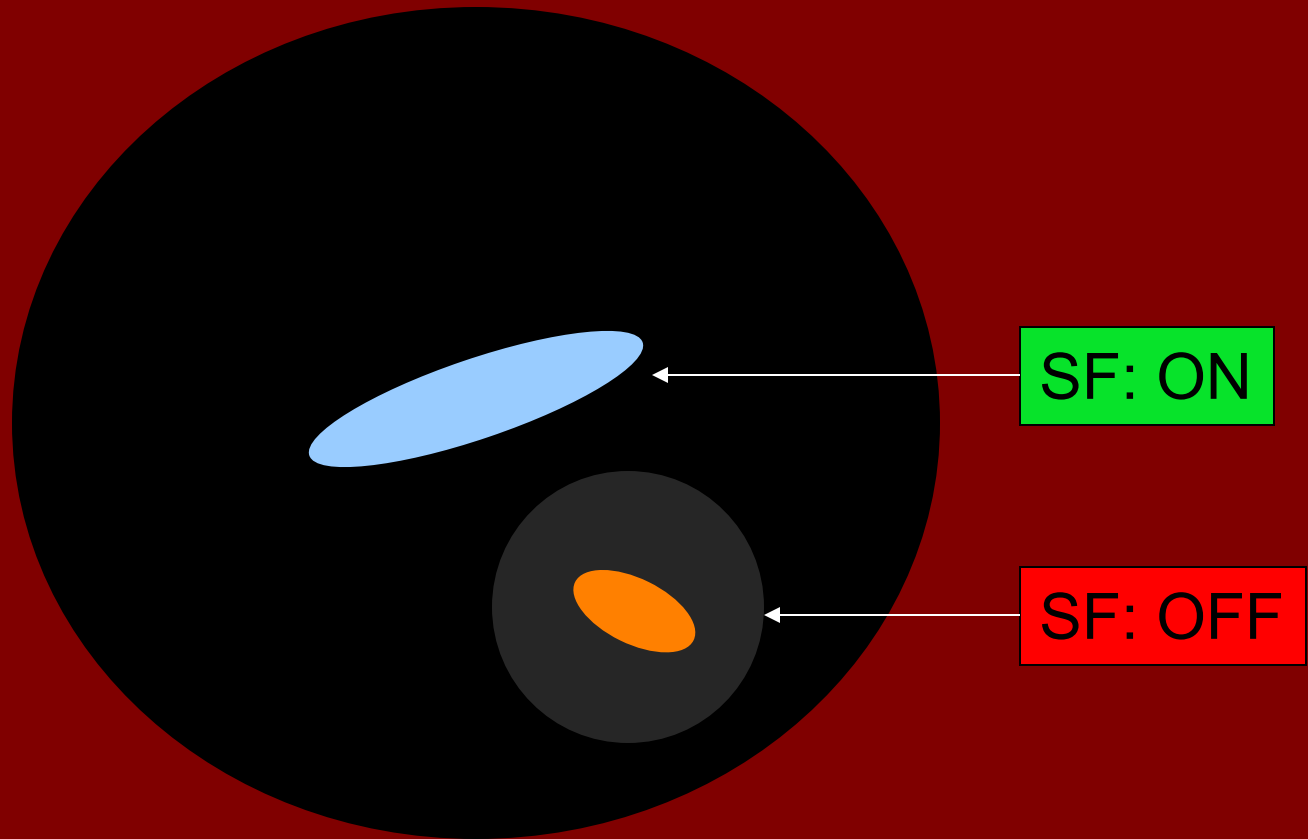
# Galaxy formation theory in a nutshell

If the halo merges with another halo containing a galaxy, the smaller galaxy becomes a satellite.



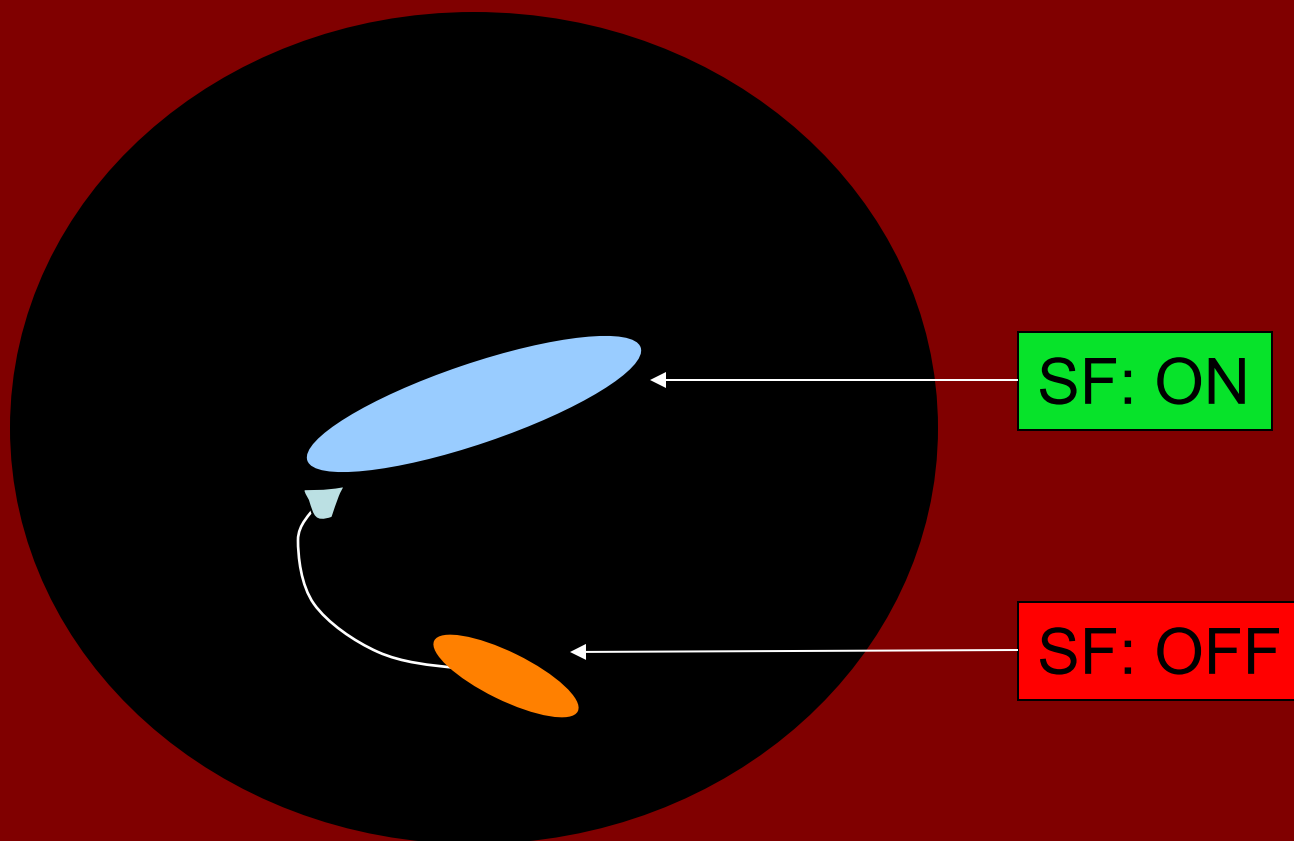
# Galaxy formation theory in a nutshell

If the main halo is massive enough to contain a galaxy, that might ram pressure strip the gas out of a satellite galaxy, thereby ending its star formation.



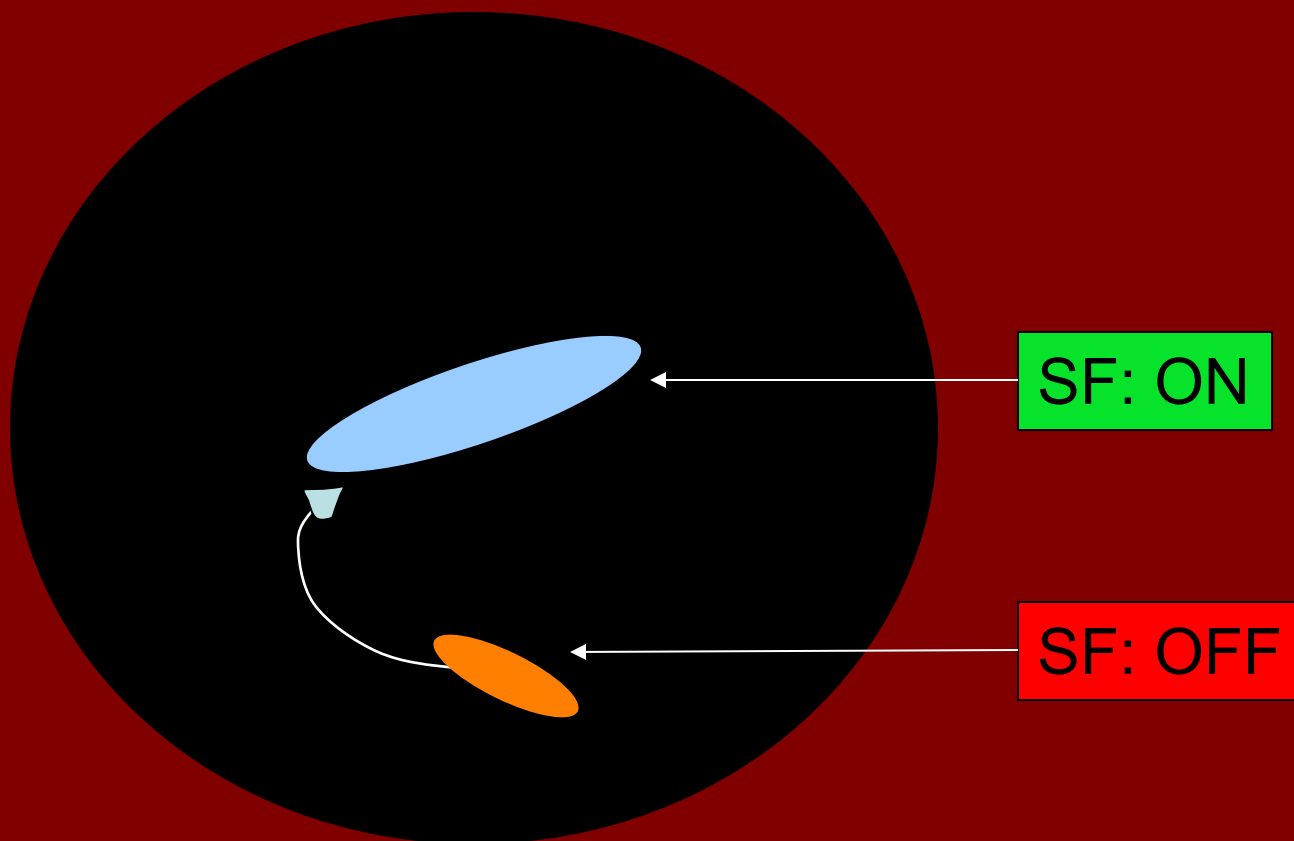
# Galaxy formation theory in a nutshell

Eventually, the subhalo will be destroyed via tidal stripping and the satellite galaxy will spiral in due to dynamical friction.



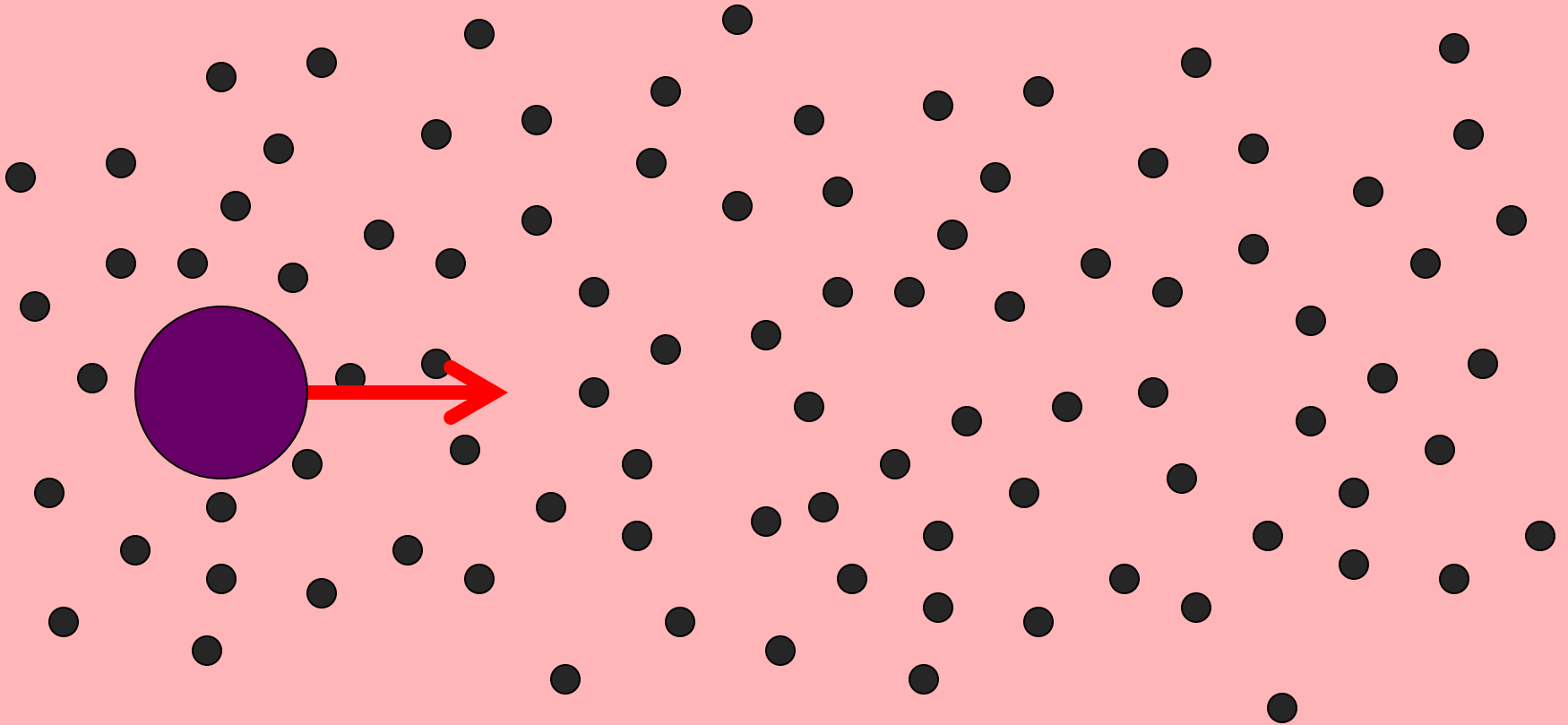
# Galaxy formation theory in a nutshell

Eventually, the subhalo will be destroyed via tidal stripping and the satellite galaxy will spiral in due to dynamical friction.



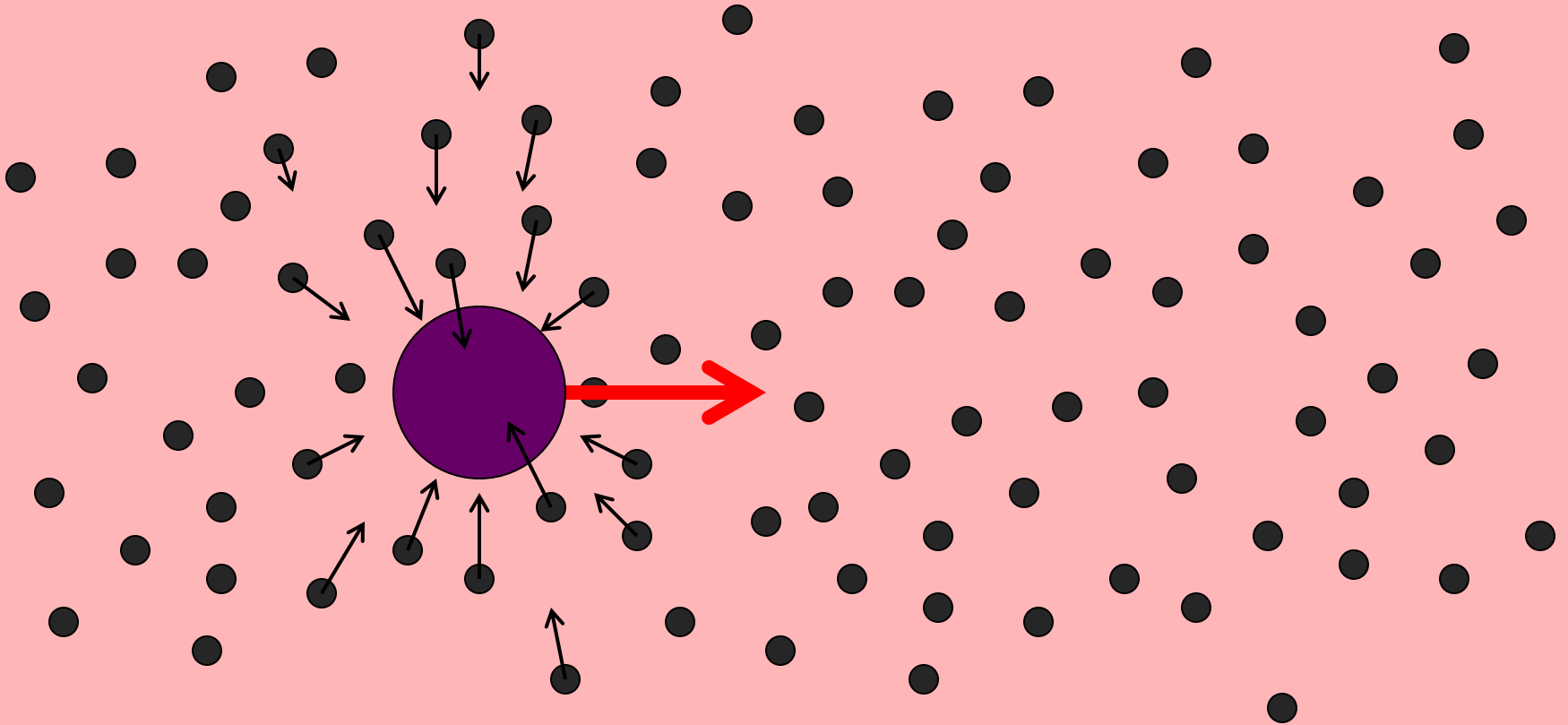
# Dynamical Friction

Dynamical friction is a force experienced by a massive body moving within a sea of lower mass particles.



# Dynamical Friction

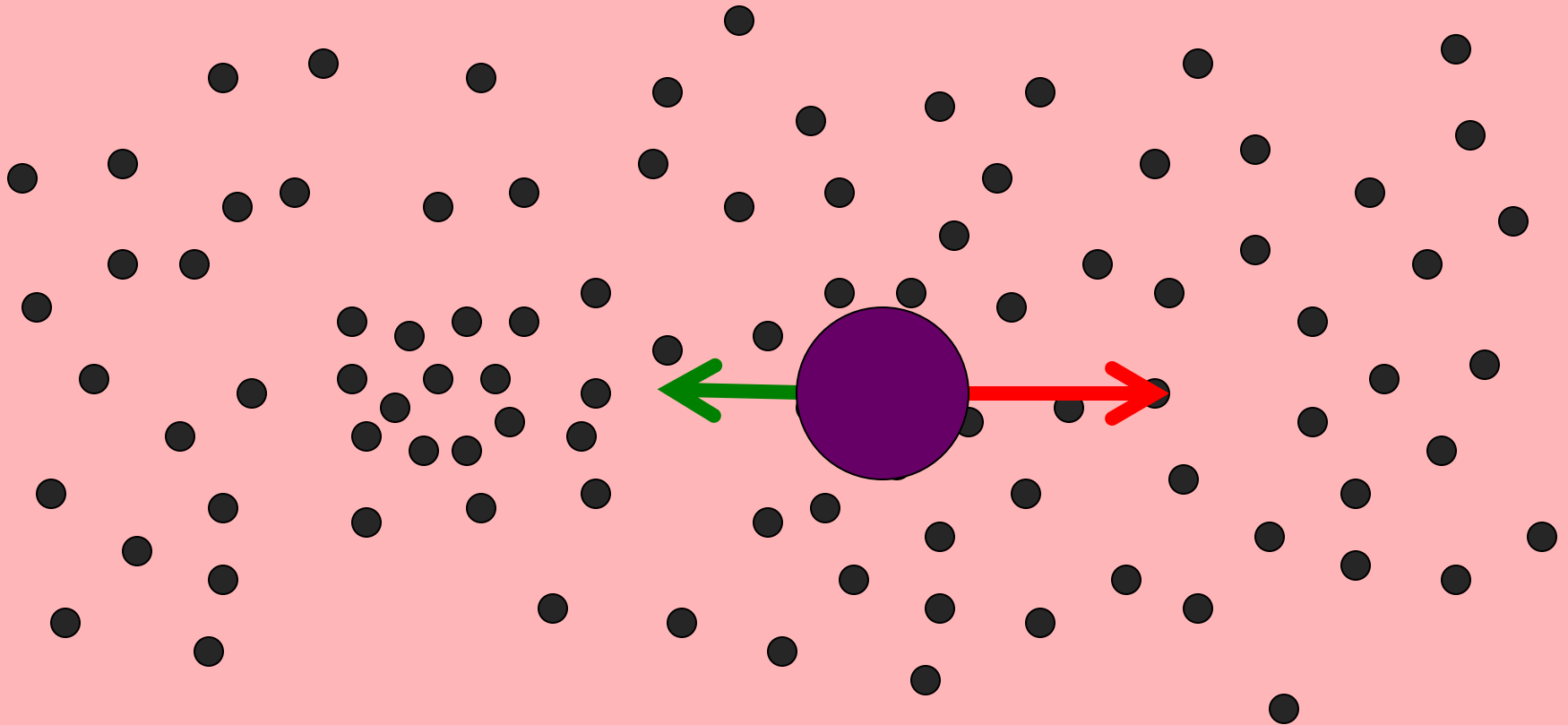
Dynamical friction is a force experienced by a massive body moving within a sea of lower mass particles.





# Dynamical Friction

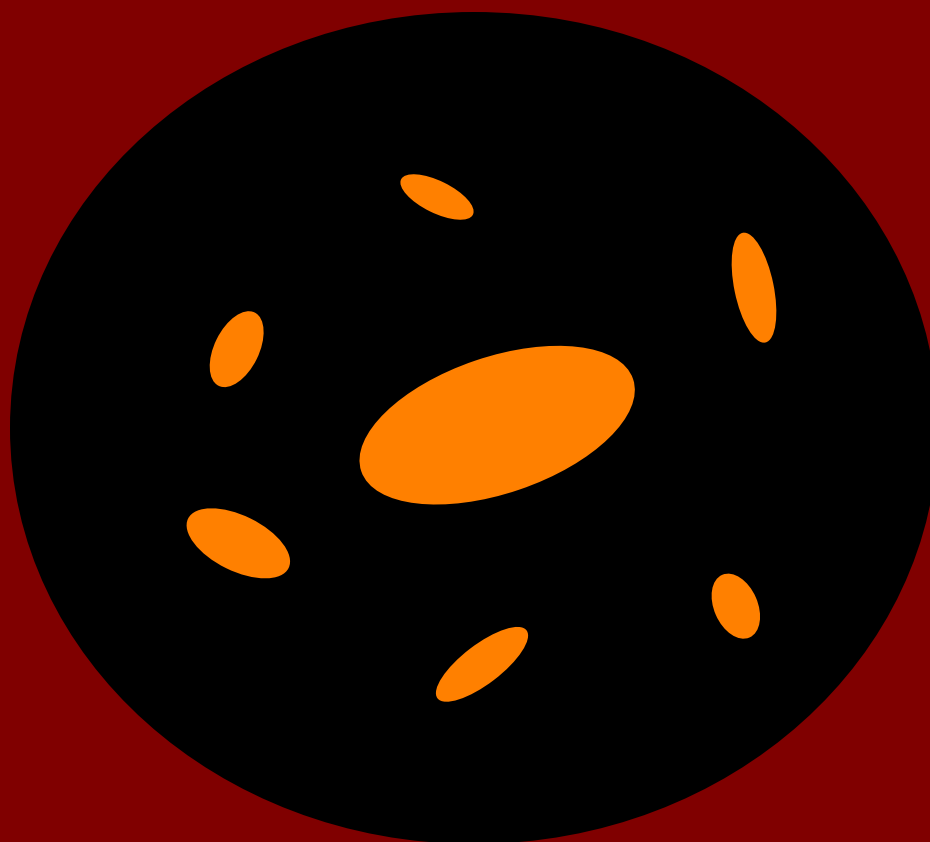
The body creates a wake of particles behind it, which creates a drag force.



Friction is high if mass of body is large and body moves slowly.

# Galaxy formation theory in a nutshell

In high mass halos, halo mergers happen frequently, but dynamical friction timescales are long, resulting in galaxy clusters.



SF: OFF

# Galaxy formation theory in a nutshell

## Key questions:

- What is the initial distribution of gas within halos and how does it cool?(e.g., multiphase medium)
- How do stars form exactly? (e.g., conditions for star formation, dependence of IMF on environment, metallicity)
- How does supernova feedback work? (e.g., thermal vs. kinetic energy injection, efficiency)
- How does AGN feedback work?
- How does merging affect galaxies' star formation and morphology?
- How does fresh gas in the IGM feed galaxies?

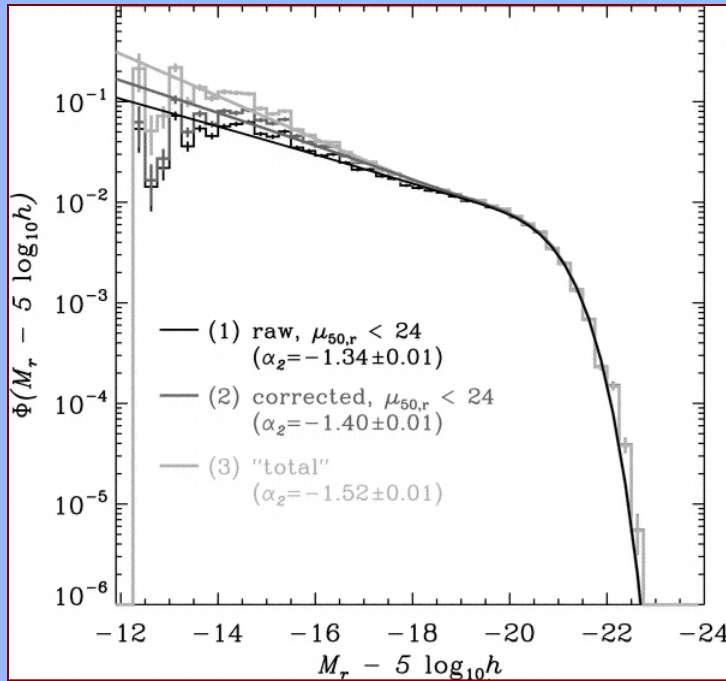
Lots of unknowns!

But also lots of data describing the distribution  
of galaxies!

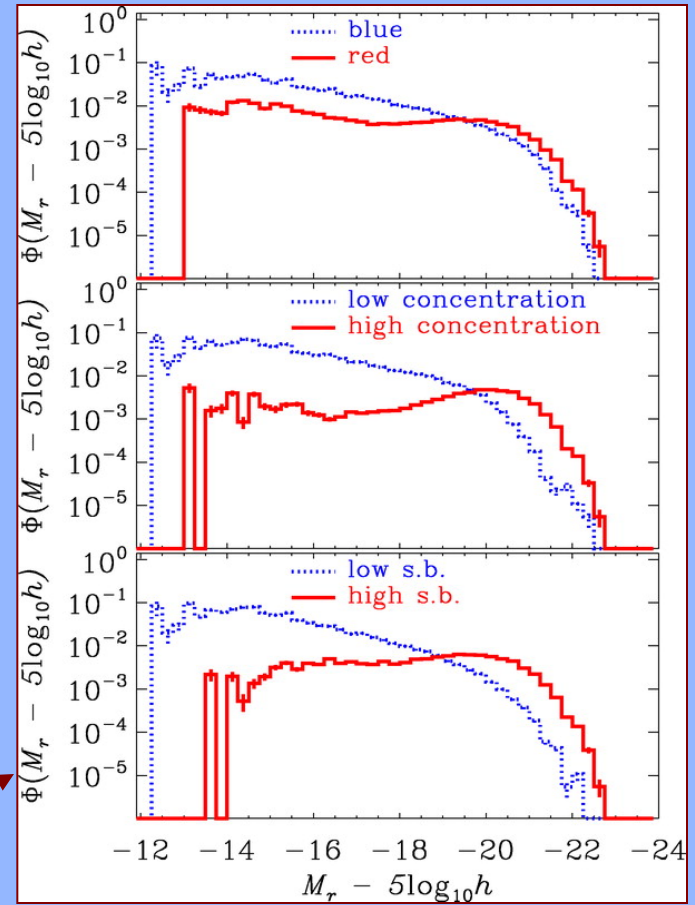


# Large surveys: Measurements of Galaxy Clustering

## First Moments $\langle \delta(\vec{x}) \rangle$



Blanton et al. (2005)



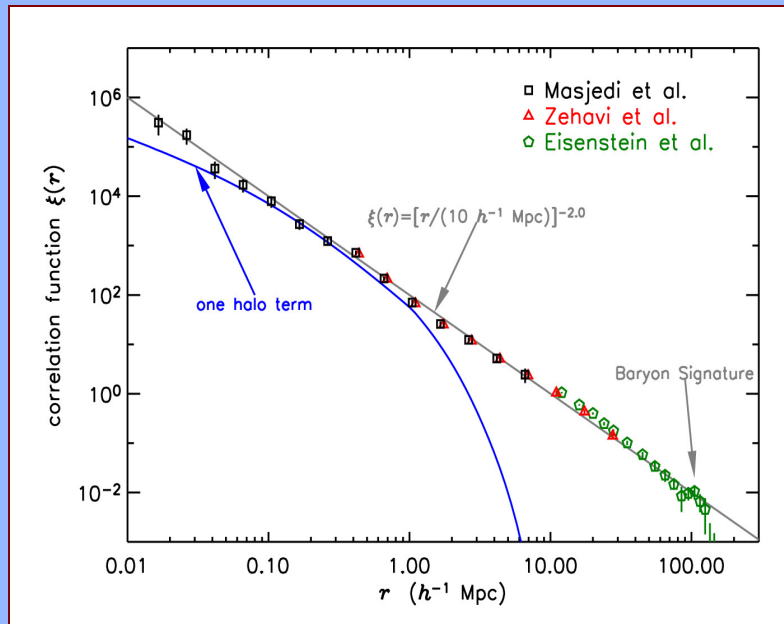
Luminosity Functions



# Large surveys: Measurements of Galaxy Clustering

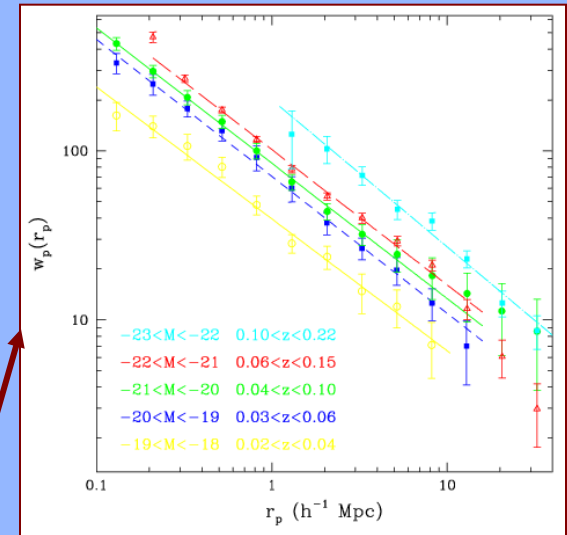
Second Moments  $\langle \delta(\vec{x})\delta(\vec{x} + r) \rangle$

$\xi_{gg}(r)$

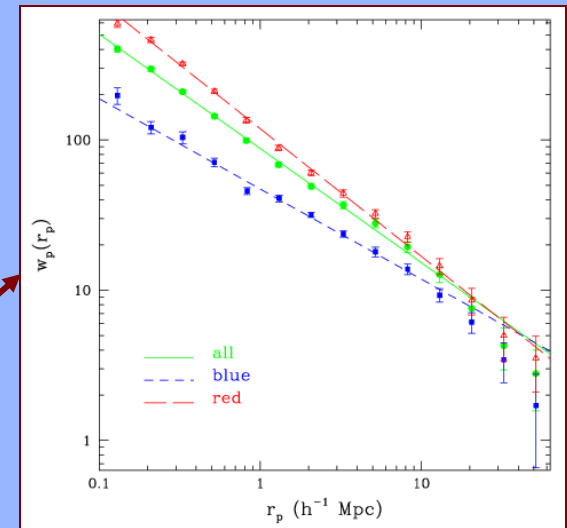


Masjedi et al. (2006)

$w_p(r_p)$



Zehavi et al. (2005)

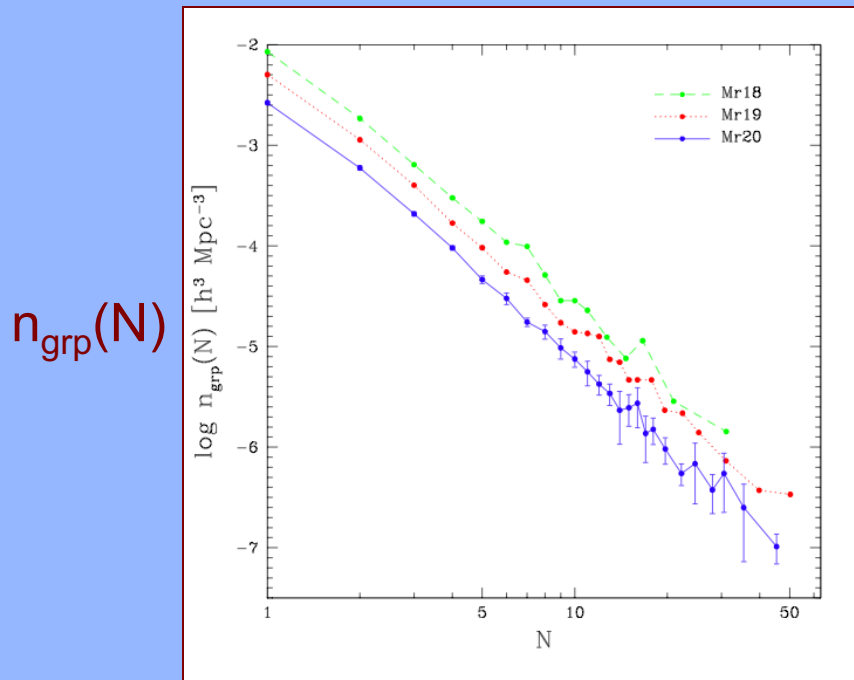


Correlation Functions



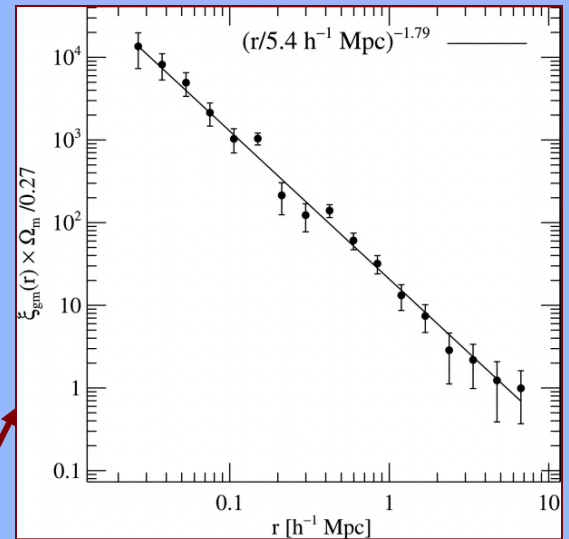
# Large surveys: Measurements of Galaxy Clustering

## Higher Moments and Other Statistics



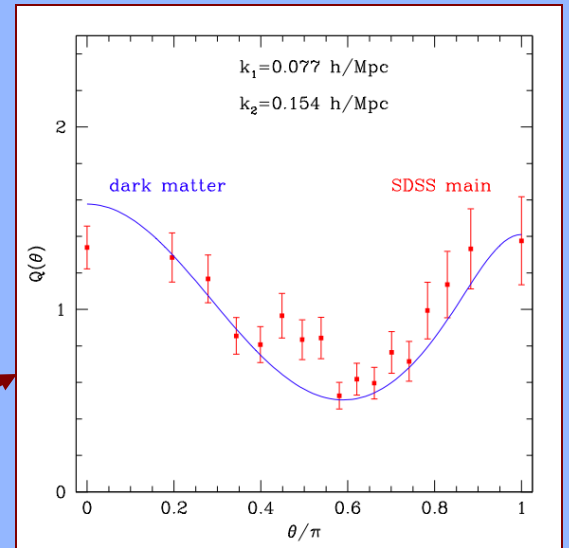
Berlind et al. (2006)

$\xi_{gm}(\rho)$



Sheldon et al. (2005)

$Q(\vartheta)$



Scoccimarro et al. (2006)

**Galaxy-Mass Correlations**

**Group Multiplicity Function**

**Bispectrum**

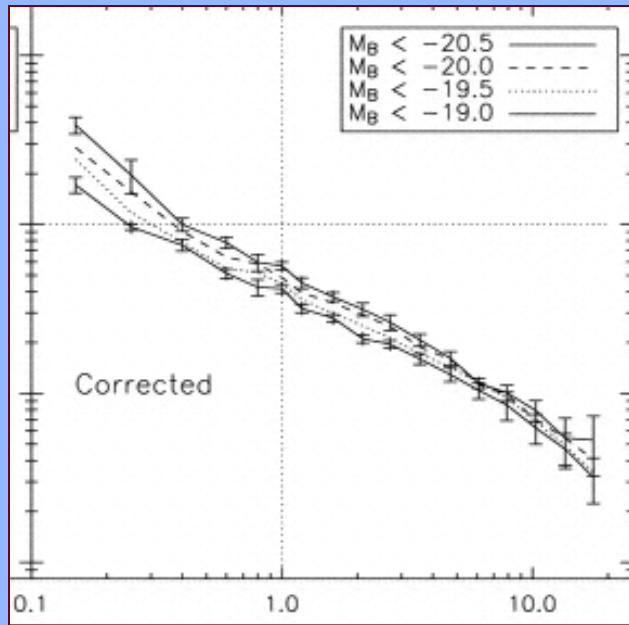


# Large surveys: Measurements of Galaxy Clustering

High Redshift

**GOODS**

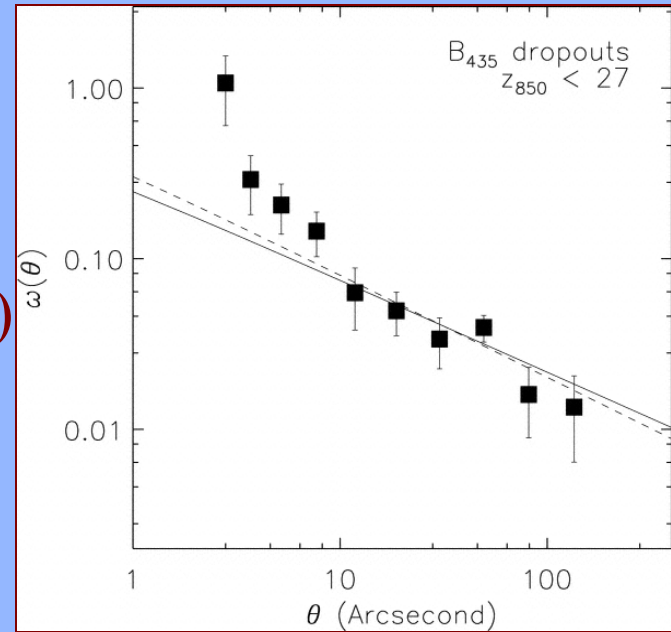
$w_p(r_p)$



Coil et al. (2006)

$z \sim 1$

$\omega(\theta)$

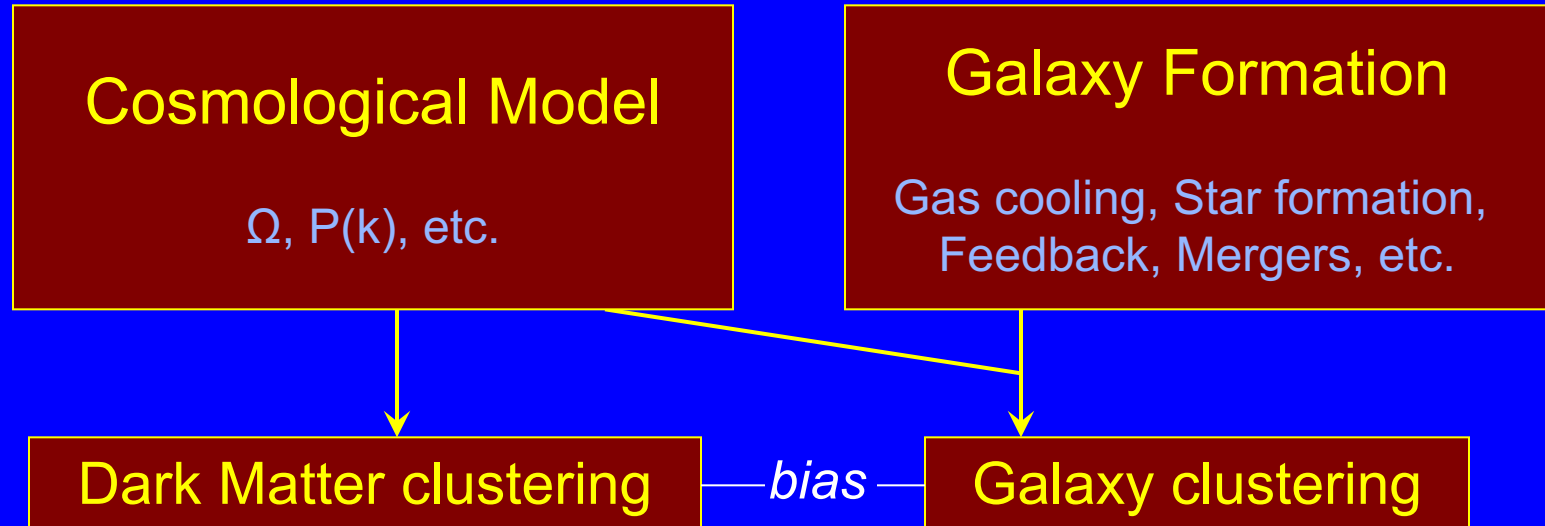


Lee et al. (2006)

$z \sim 4$



Galaxy clustering data contains information about cosmology and galaxy formation/evolution.



How can we extract this information from the data?  
*e.g., what does a particular shape of  $\xi(r)$  for bright red galaxies tell us about how these galaxies formed? Can we use this statistic to constrain cosmological parameters?*

# Ab-initio Predictions

## Hydrodynamic Simulations of Dark Matter + Gas

Gravity  
and  
Hydrodynamics

+

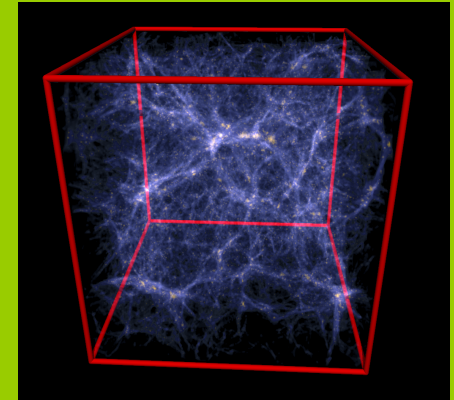
Heating  
and  
Cooling

+

Prescriptions for  
Star Formation  
and  
Feedback

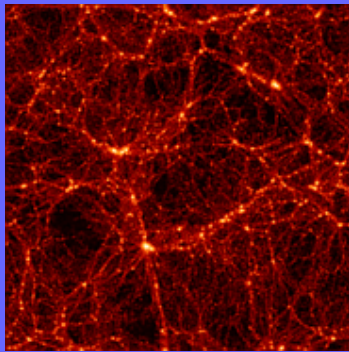
(Sub-grid physics)

=



Springel et al.

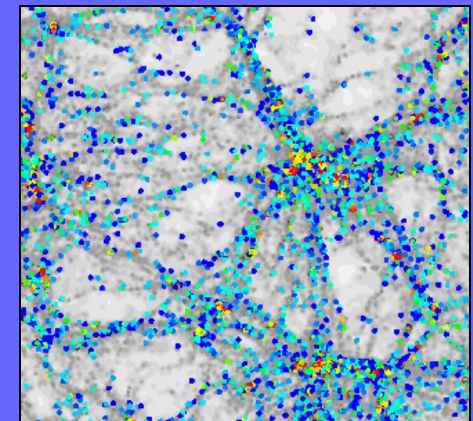
## Semi-Analytic Models



+

Prescriptions for:  
Gas distribution, Gas Cooling,  
Star Formation, Feedback,  
Galaxy Mergers + more  
in DM halos

=



Virgo Consortium

# RAMSES code (AMR)



# RAMSES code (AMR)



# GASOLINE code (SPH)

## Gas Rich Mergers and Disk Galaxy Formation

Galaxy formation simulations created at the

### N-body shop

*makers of quality galaxies*

key: gas- green new stars- blue old stars- red

credits:

Fabio Governato (University of Washington)

Alyson Brooks (University of Washington)

James Wadsely (McMaster University)

Tom Quinn (University of Washington)

Chris Brook (University of Washington)

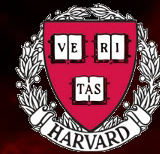
Simulation run on Columbia (NASA Advanced Supercomputing)

contact: [fabio@astro.washington.edu](mailto:fabio@astro.washington.edu)

# AREPO code (Moving Mesh)

**Mark Vogelsberger**

Harvard-Smithsonian Center for Astrophysics  
Institute for Theory and Computation



# AREPO code (Moving Mesh)

**Mark Vogelsberger**

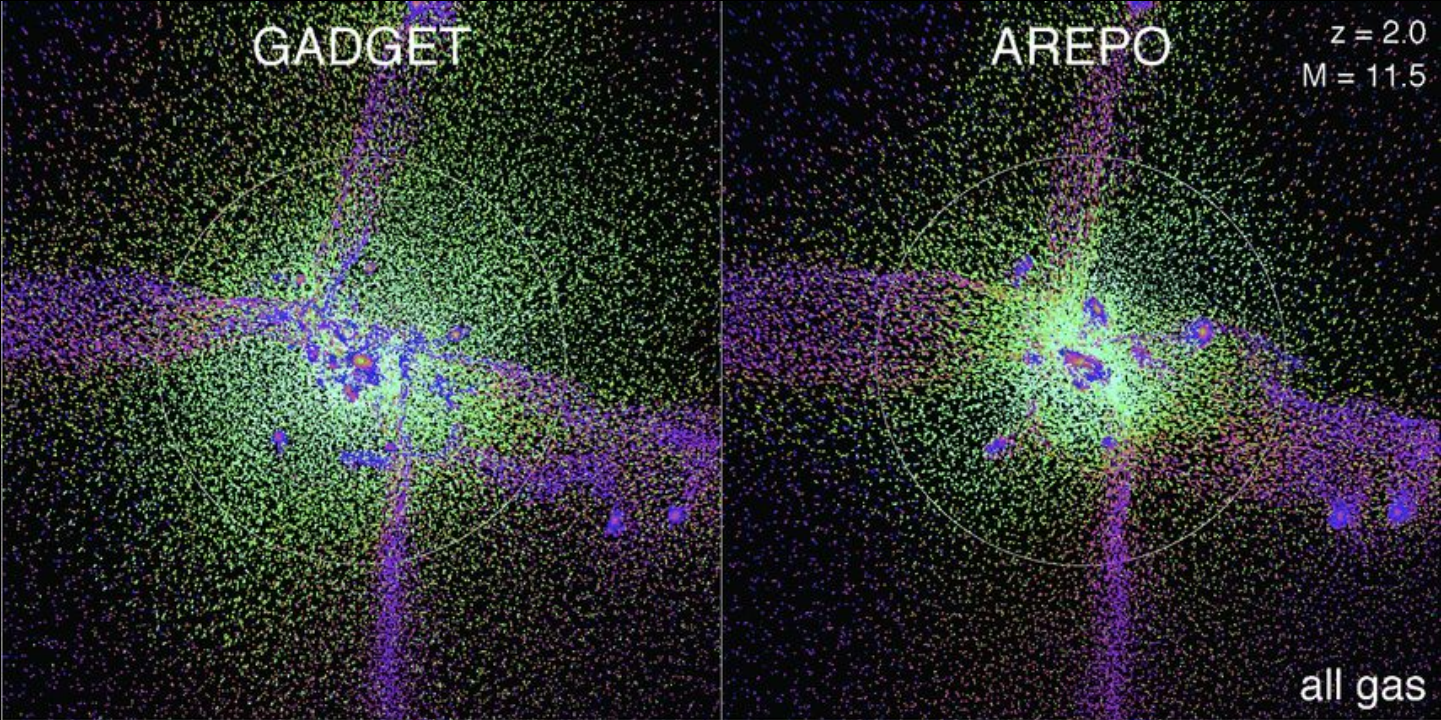
Harvard-Smithsonian Center for Astrophysics  
Institute for Theory and Computation



GADGET

AREPO

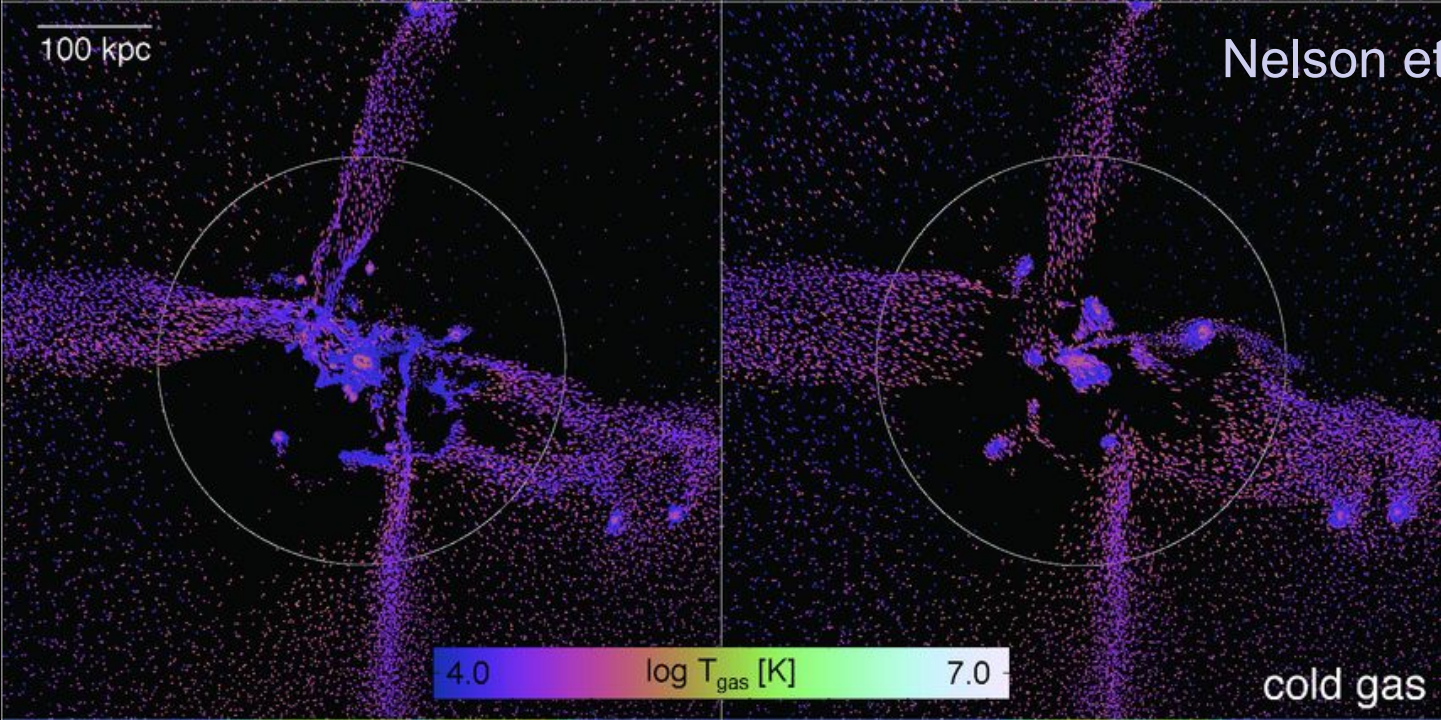
$z = 2.0$   
 $M = 11.5$



all gas

100 kpc

Nelson et al. (2013)

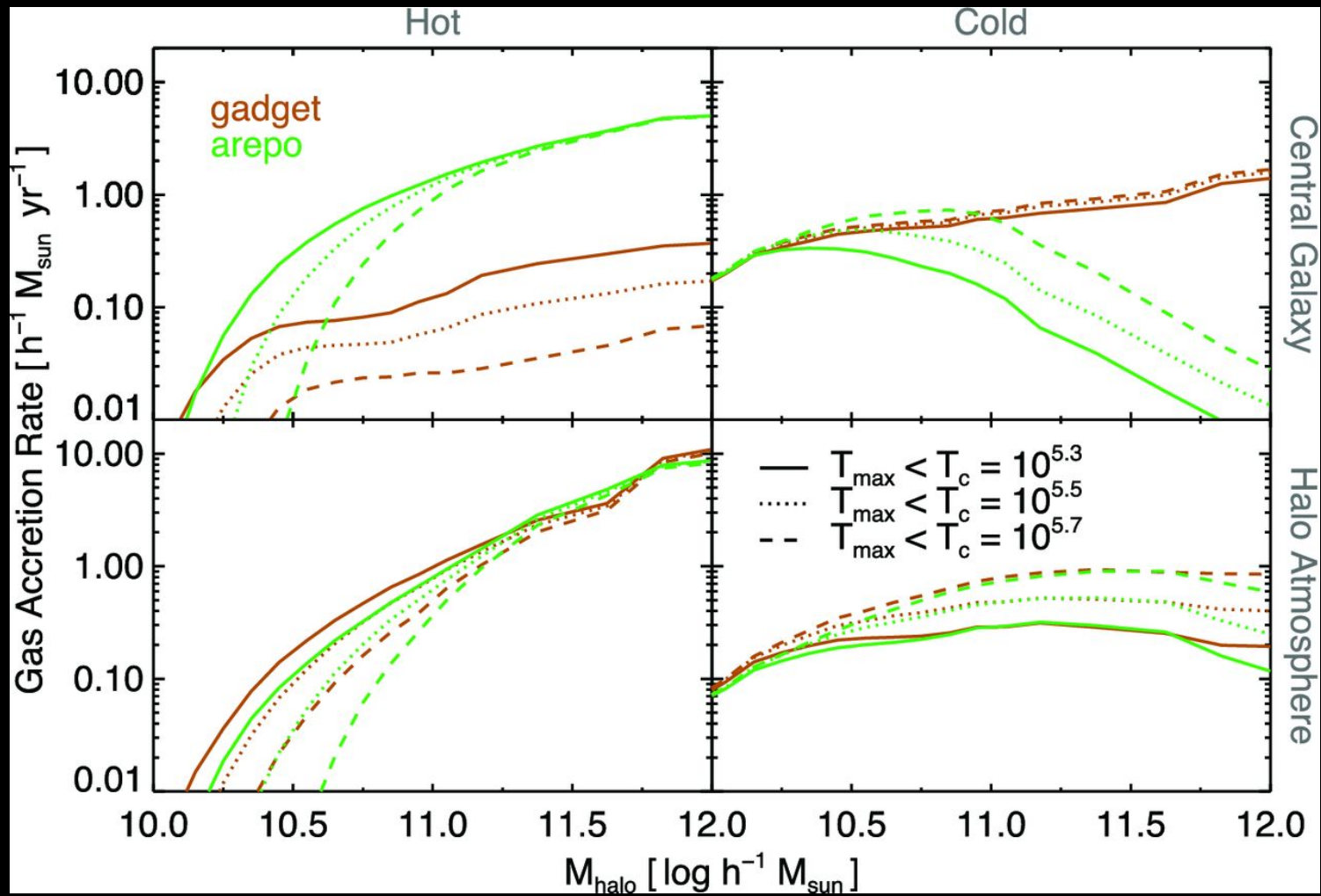


4.0  $\log T_{\text{gas}} [\text{K}]$  7.0

cold gas

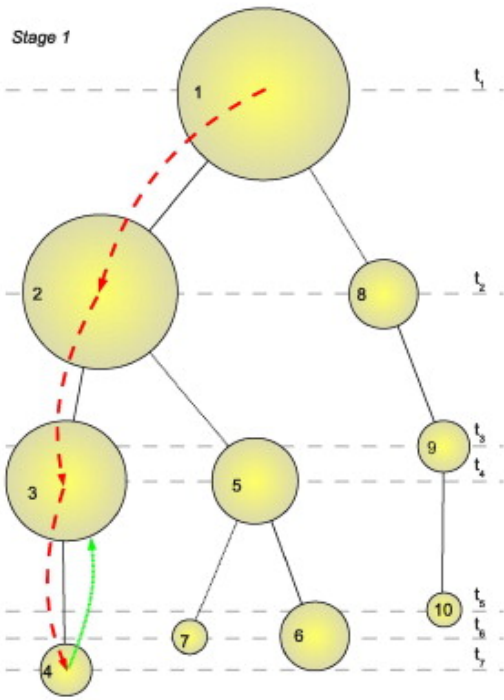


# Moving Mesh vs. SPH - Gas accretion

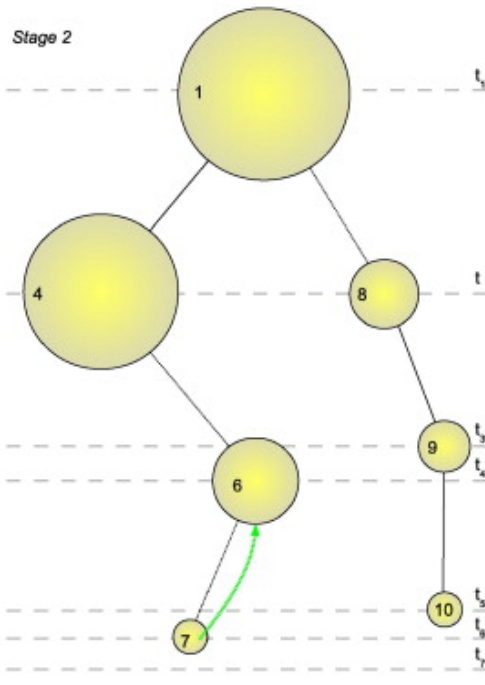


Nelson et al. (2013)

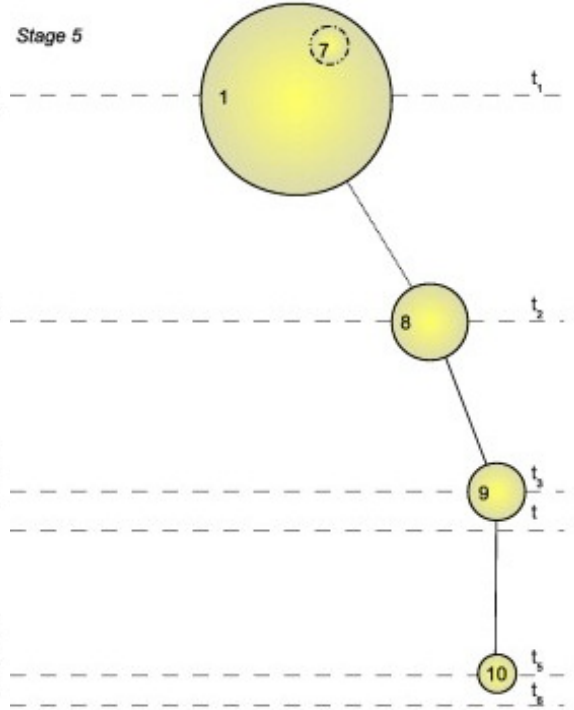
Stage 1



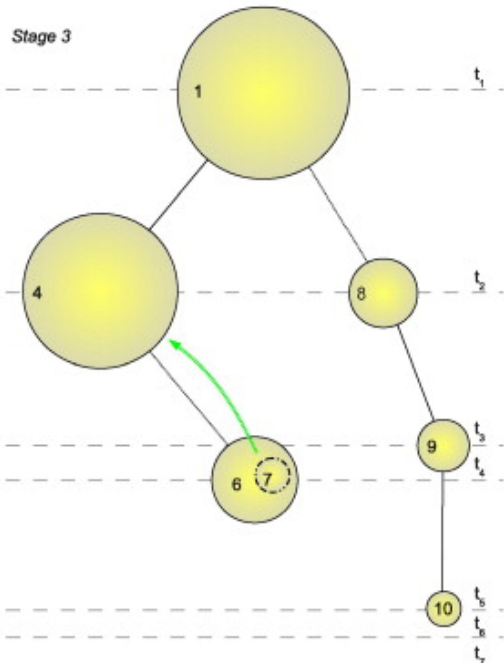
Stage 2



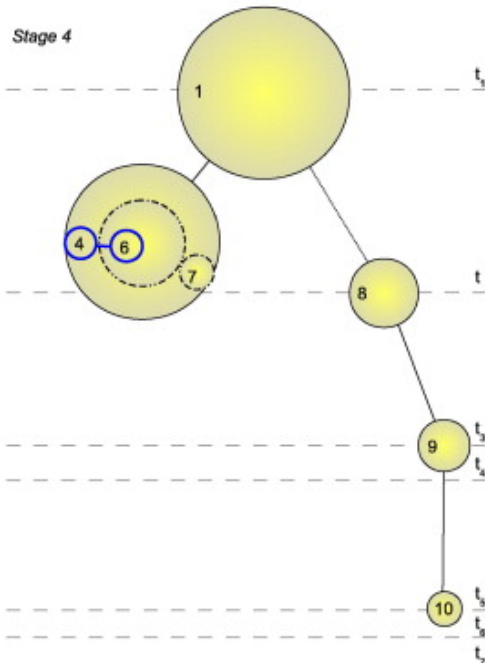
Stage 5



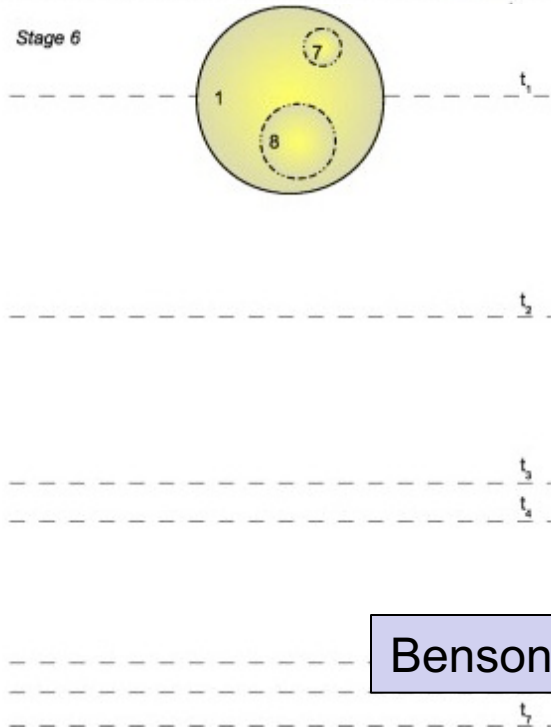
Stage 3



Stage 4

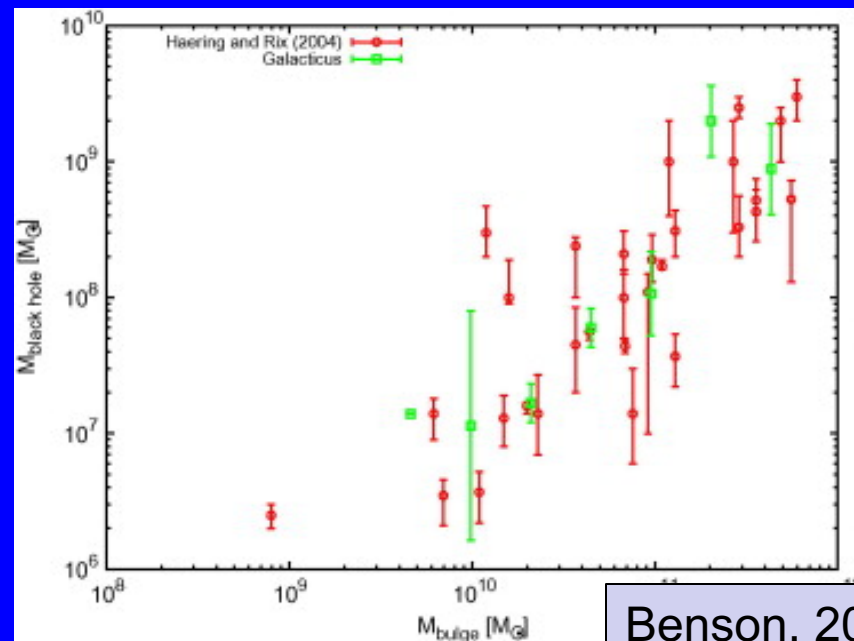
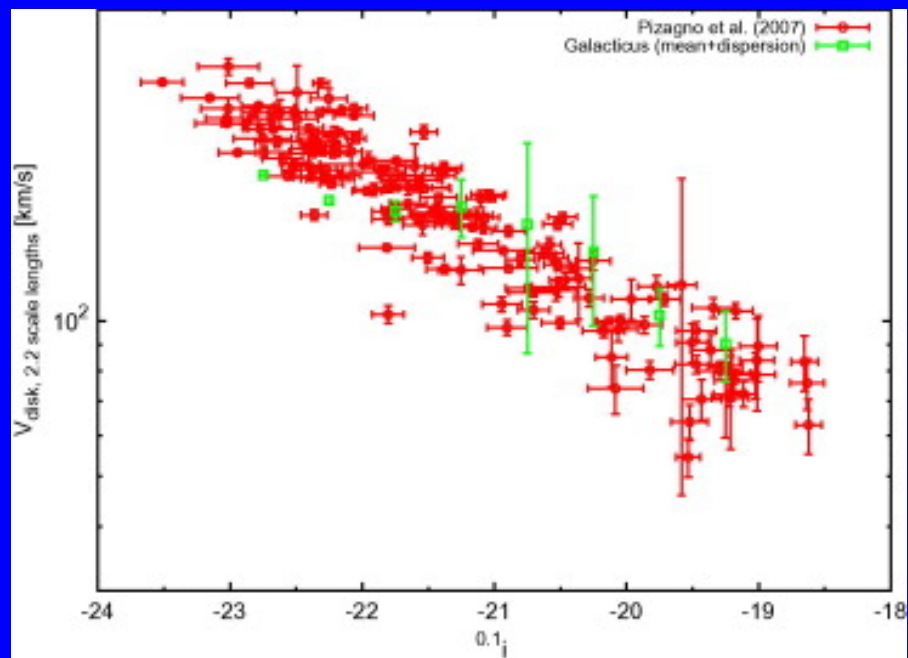
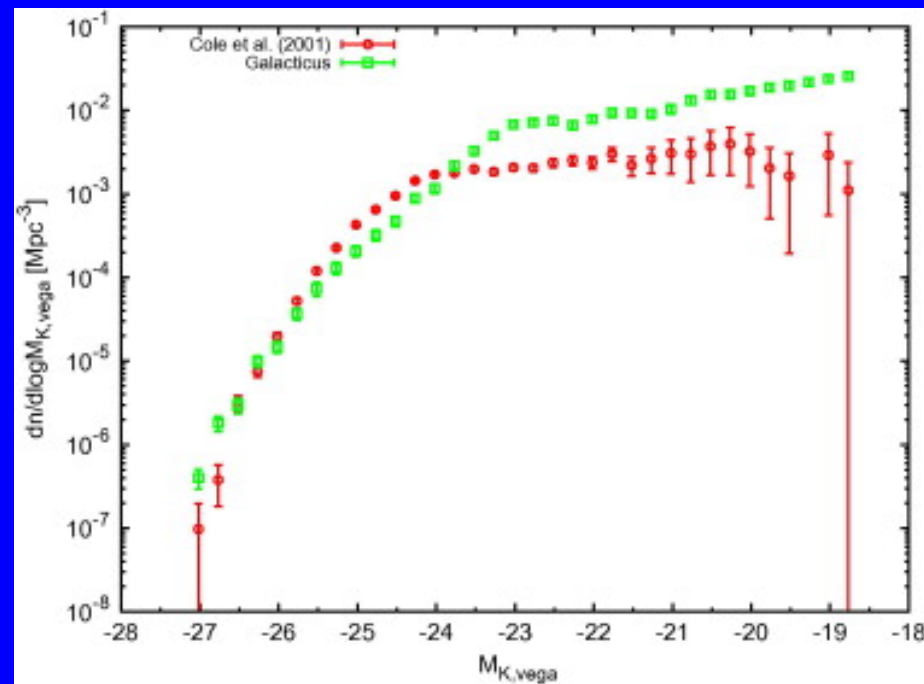
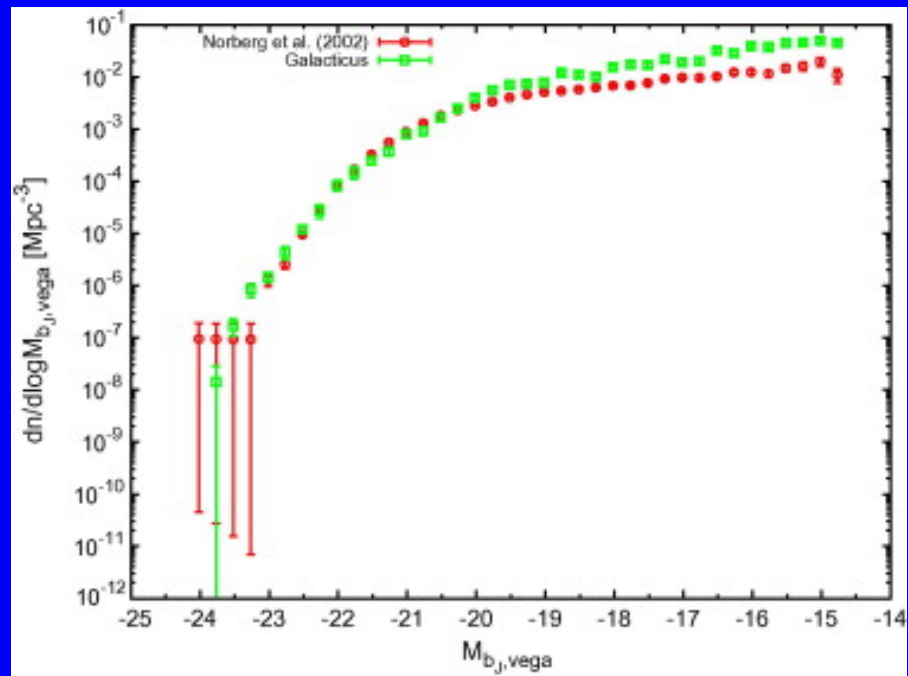


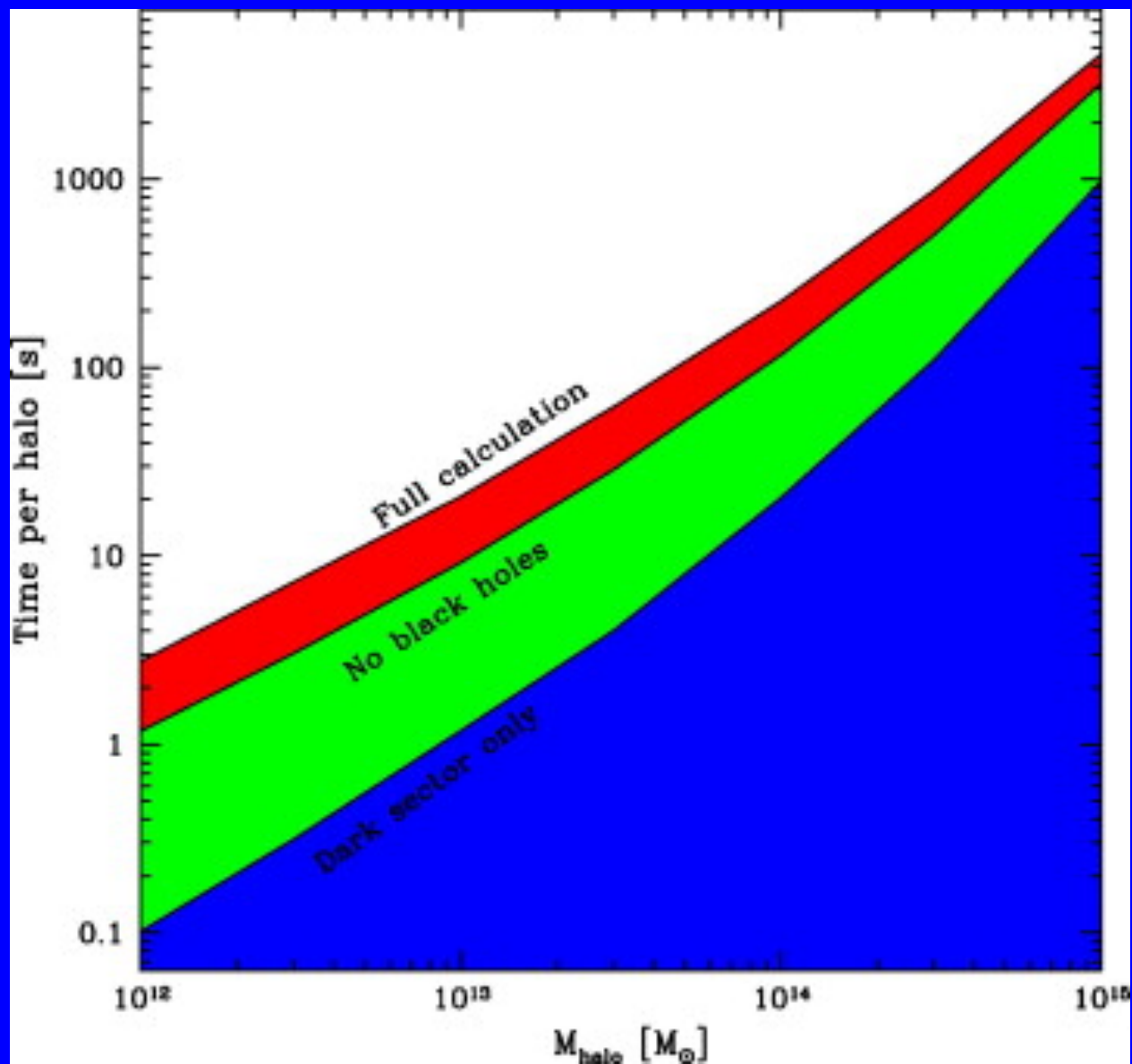
Stage 6



Parameter	Value	Reference
[H_0]	70.2 km/s	§4.2; (Komatsu et al., 2010)
[Omega_0]	0.2725	§4.2; (Komatsu et al., 2010)
[Omega_DE]	0.7275	§4.2; (Komatsu et al., 2010)
[Omega_b]	0.0455	§4.2; (Komatsu et al., 2010)
[T_CMB]	2.72548 K	§4.2; (Komatsu et al., 2010)
[accretionDisksMethod]	ADAF	§4.3
[adafAdiabaticIndex]	1.444	§4.3
[adafEnergyOption]	pure ADAF	§4.3
[adafRadiativeEfficiency]	0.01	§4.3
[adafViscosityOption]	fit	§4.3
[adiabaticContractionGnedinA]	0.8	§4.8
[adiabaticContractionGnedinOmega]	0.77	§4.8
[barInstabilityMethod]	ELN	§4.7
[blackHoleSeedMass]	100	§3.1.2
[blackHoleWindEfficiency]	0.001	§3.1.2
[bondiHoyleAccretionEnhancementHotHalo]	1	§3.1.2
[bondiHoyleAccretionEnhancementSpheroid]	1	§3.1.2
[bondiHoyleAccretionTemperatureSpheroid]	100	§3.1.2
[coolingFunctionMethod]	atomic CIE Cloudy	§4.5.1
[coolingTimeAvailableAgeFactor]	0	§4.5.5
[coolingTimeSimpleDegreesOfFreedom]	3	§4.5.4
[darkMatterProfileMethod]	NFW	§4.6.1
[darkMatterProfileMinimumConcentration]	4	§3.8.2
[diskOutflowExponent]	2	§4.23
[diskOutflowVelocity]	200 km/s	§4.23
[effectiveNumberNeutrinos]	4.34	§4.4.2
[galacticStructureRadiusSolverMethod]	adiabatic	§4.8
[haloMassFunctionMethod]	Tinker2008	§4.4.6
[haloSpinDistributionMethod]	Bett2007	§4.6.3
[hotHaloOutflowReturnRate]	1.26	§3.2.2
[imfSalpeterRecycledInstantaneous]	0.39	§4.12.2
[imfSalpeterYieldInstantaneous]	0.02	§4.12.2
[imfSelectionFixed]	Salpeter	§4.12.1
[isothermalCoreRadiusOverVirialRadius]	0.1	§4.10

[majorMergerMassRatio]	0.1	§4.9.1
[mergerRemnantSizeOrbitalEnergy]	1	§4.9.2
[mergerTreeBuildCole2000AccretionLimit]	0.1	§4.16
[mergerTreeBuildCole2000MassResolution]	$5 \times 10^9 M_{\odot}$	§4.16
[mergerTreeBuildCole2000MergeProbability]	0.1	§4.16
[mergerTreeConstructMethod]	build	§4.14
[minorMergerGasMovesTo]	spheroid	§4.9.1
[modifiedPressSchechterFirstOrderAccuracy]	0.1	§4.15
[modifiedPressSchechterG0]	0.57	§4.15
[modifiedPressSchechterGamma1]	0.38	§4.15
[modifiedPressSchechterGamma2]	-0.01	§4.15
[powerSpectrumIndex]	0.961	§4.4.1; (Komatsu et al., 2010)
[powerSpectrumReferenceWavenumber]	$1 \text{ Mpc}^{-1}$	§4.4.1; (Komatsu et al., 2010)
[powerSpectrumRunning]	0	§4.4.1; (Komatsu et al., 2010)
[randomSpinResetMassFactor]	2	§3.7.2
[reionizationSuppressionRedshift]	9	§4.1
[reionizationSuppressionVelocity]	30 km/s	§4.1
[satelliteMergingMethod]	Jiang2008	§4.22.1
[sigma_8]	0.807	§4.4.1 & §4.4.2
[spheroidEnergeticOutflowMassRate]	1	§3.4.2
[spheroidOutflowExponent]	2	§4.23
[spheroidOutflowVelocity]	50 km/s	§4.23
[spinDistributionBett2007Alpha]	2.509	§4.6.3
[spinDistributionBett2007Lambda0]	0.04326	§4.6.3
[stabilityThresholdGaseous]	0.9	§4.7
[stabilityThresholdStellar]	1.1	§4.7
[starFormationDiskEfficiency]	0.01	§4.17
[starFormationDiskMinimumTimescale]	0.001 Gyr	§4.17
[starFormationDiskVelocityExponent]	-1.5	§4.17
[starFormationSpheroidEfficiency]	0.1	§4.17
[starFormationSpheroidMinimumTimescale]	0.001 Gyr	§4.17
[starveSatellites]	true	§3.2.2
[stellarPopulationPropertiesMethod]	instantaneous	§4.18
[summedNeutrinoMasses]	0	§4.4.2
[transferFunctionMethod]	Eisenstein + Hu	§4.4.2
[virialDensityContrastMethod]	spherical top hat	§4.4.5





## Forward approach is not practical

- Hydrodynamic simulations take too long + cannot resolve much of the important physics → make many assumptions.
- Semi-analytic models have too many free parameters and do not necessarily include all the relevant physics.

For constraining cosmological parameters: too many uncertainties in galaxy formation physics. We can predict dark matter clustering to fairly high precision, but we have trouble going from DM to galaxies.

For constraining galaxy formation physics: difficult to understand how parameters affect clustering statistics. *e.g., what does it mean if a model predicts a 3-point correlation function that is too high for faint red galaxies?*

## “Halo Occupation” Bias

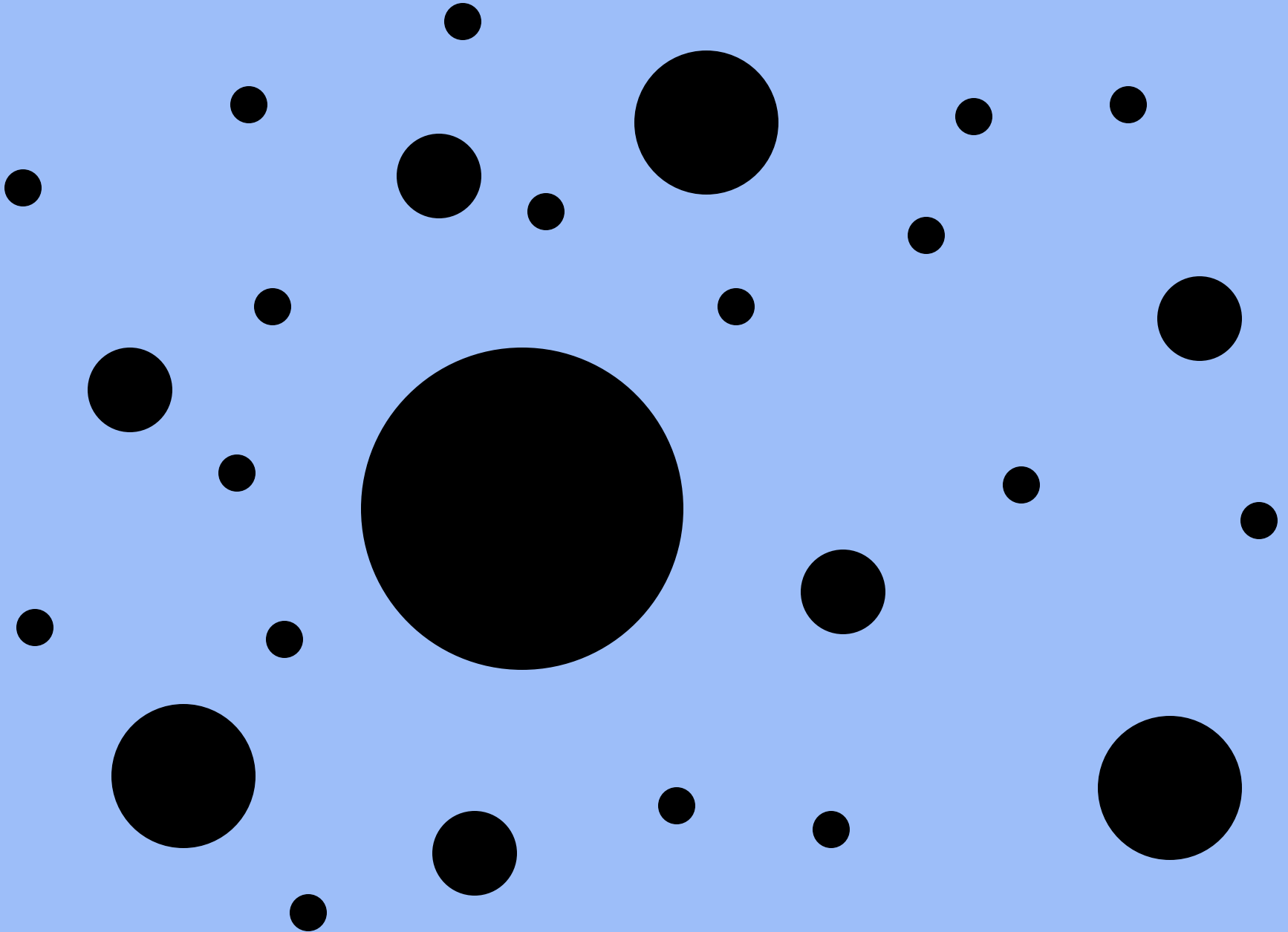
1. All galaxies live in DM halos
2. The galaxy content of a halo is statistically independent of the halo's larger scale environment (depends only on mass)

The bias of any class of galaxies (luminosity, type, etc.) is fully defined by the **Halo Occupation Distribution (HOD)**:

- The probability distribution  $P(N|M)$  that a halo of mass  $M$  contains  $N$  galaxies of that class.
- The relation between the **spatial** distributions of galaxies and DM within halos.
- The relation between the **velocity** distributions of galaxies and DM within halos.

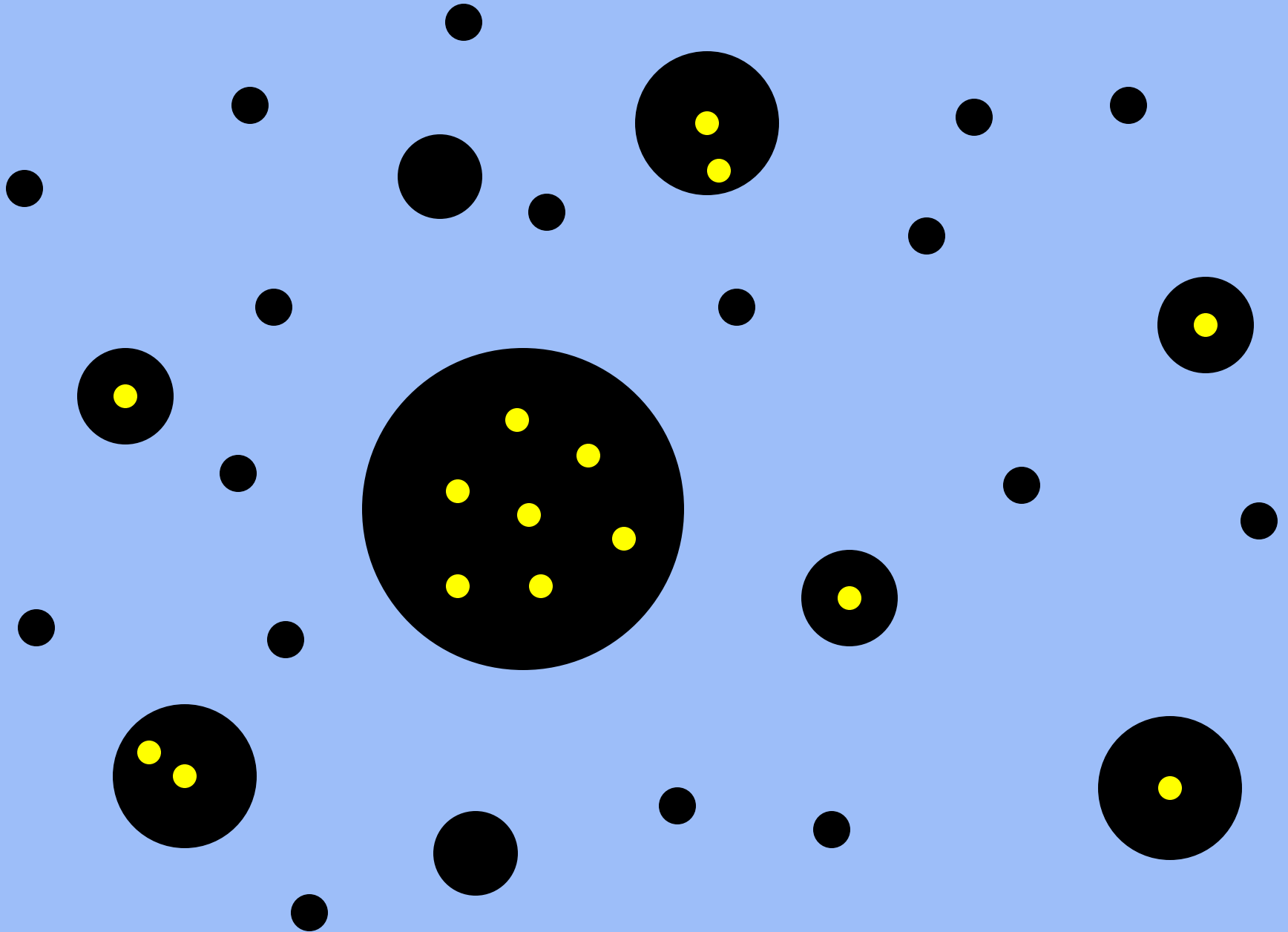


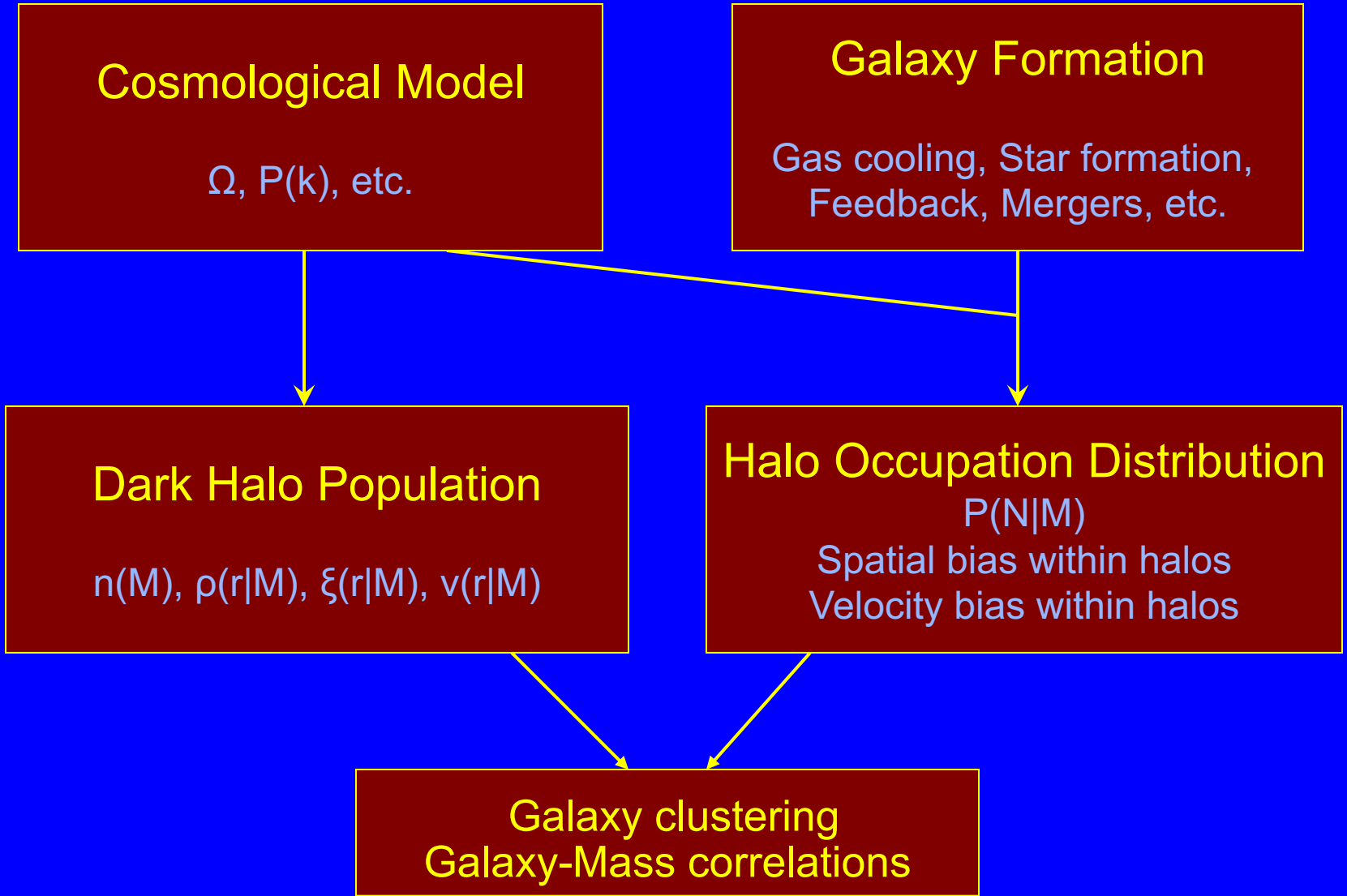
# Dark Halo Population



Dark Halo Population

Galaxy Population





## Cosmological Model

$\Omega$ ,  $P(k)$ , etc.

## Galaxy Formation

Gas cooling, Star formation,  
Feedback, Mergers, etc.

## Dark Halo Population

$n(M)$ ,  $\rho(r|M)$ ,  $\xi(r|M)$ ,  $v(r|M)$

## Halo Occupation Distribution

$P(N|M)$

Spatial bias within halos  
Velocity bias within halos

Galaxy clustering  
Galaxy-Mass correlations

## Why is the Halo Occupation Distribution (HOD) the right way to think about bias?

- **Complete:** It tells us everything a theory of galaxy formation has to say about galaxy clustering (all statistics, all scales).
- **Physically illuminating:** Discrepancies offer guidance about their physical origin.
- **Observationally powerful:** Description of bias at the level of systems in dynamic equilibrium, where methods can constrain mass.

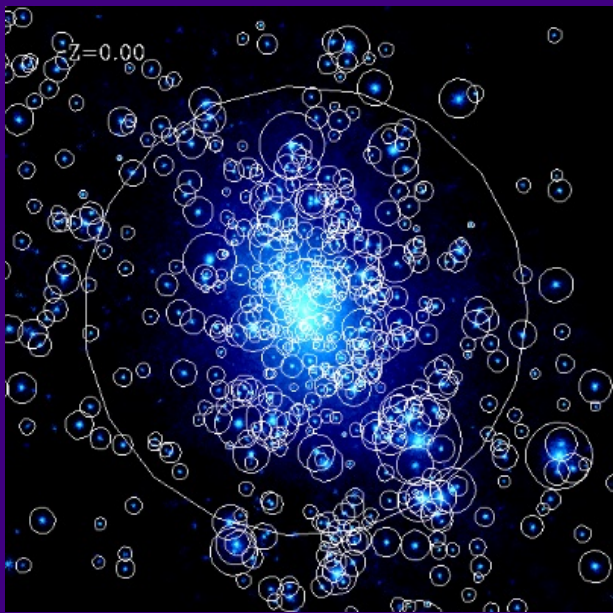
Nice conceptual division between roles of “cosmological model” and “theory of Galaxy formation”.

## The basic approach.

- We know how to go from cosmological parameters to halo properties.
- Parameterize the HOD (and thus our ignorance about galaxy formation).
- Develop machinery to compute galaxy clustering statistics given halo properties (mass function, etc.) + HOD.
- Fit cosmological + HOD parameters (or HOD parameters at fixed cosmology) to galaxy clustering measurements.
- Use measured HODs to gain insight into galaxy formation.

# How do we parameterize the HOD?

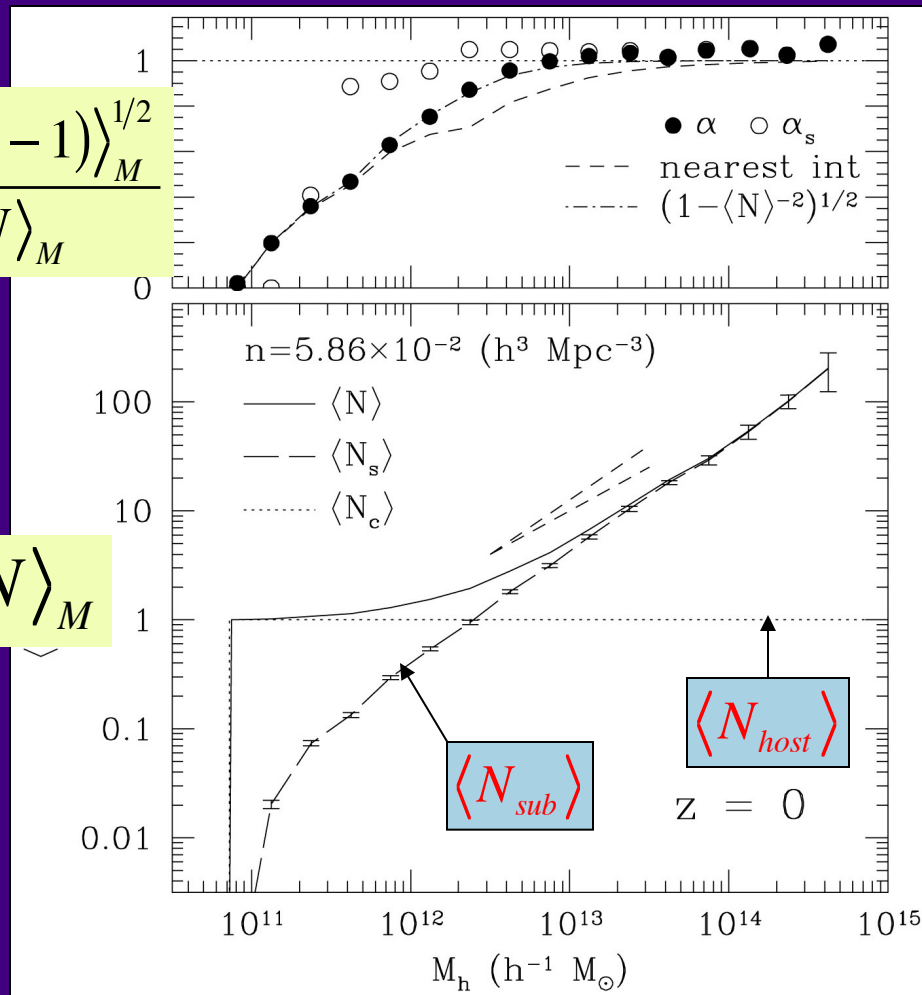
## N-body



- HOD for halos + subhalos.
- $\langle N_{\text{sub}} \rangle$  is a power law with slope  $\sim 1$ .
- Distribution about  $\langle N_{\text{sub}} \rangle$  is Poisson.

$$\frac{\langle N(N-1) \rangle_M^{1/2}}{\langle N \rangle_M}$$

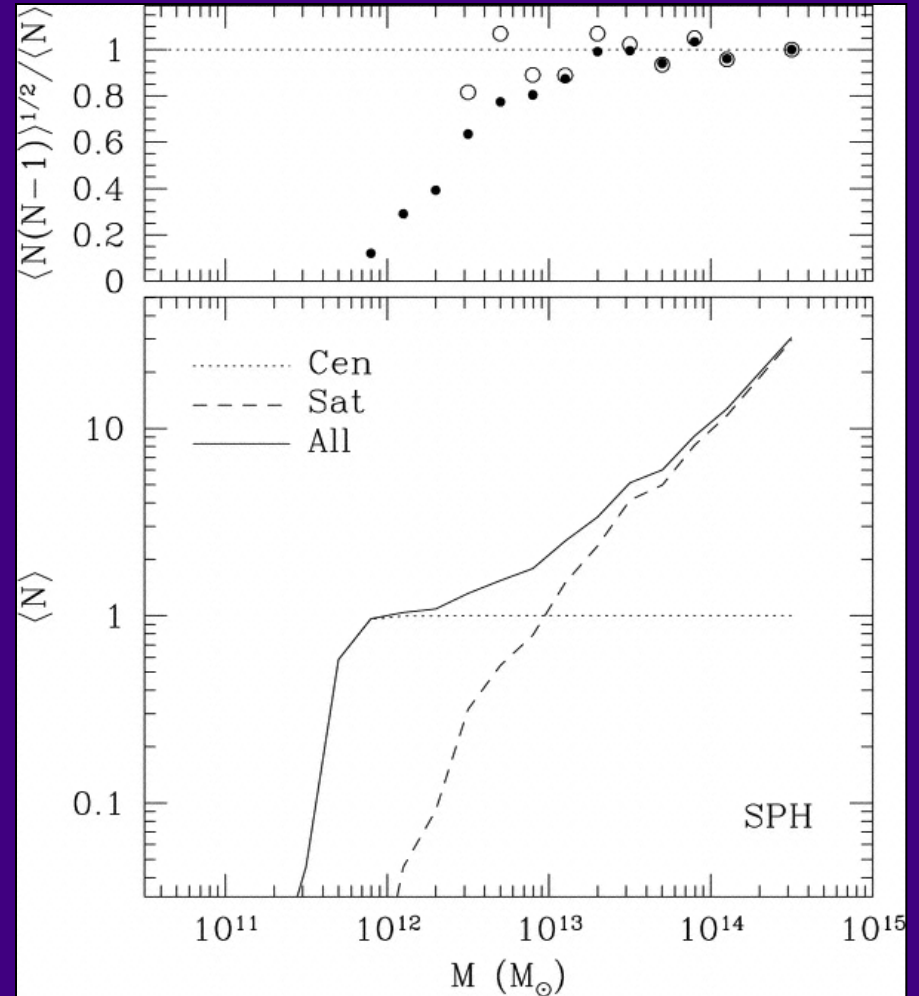
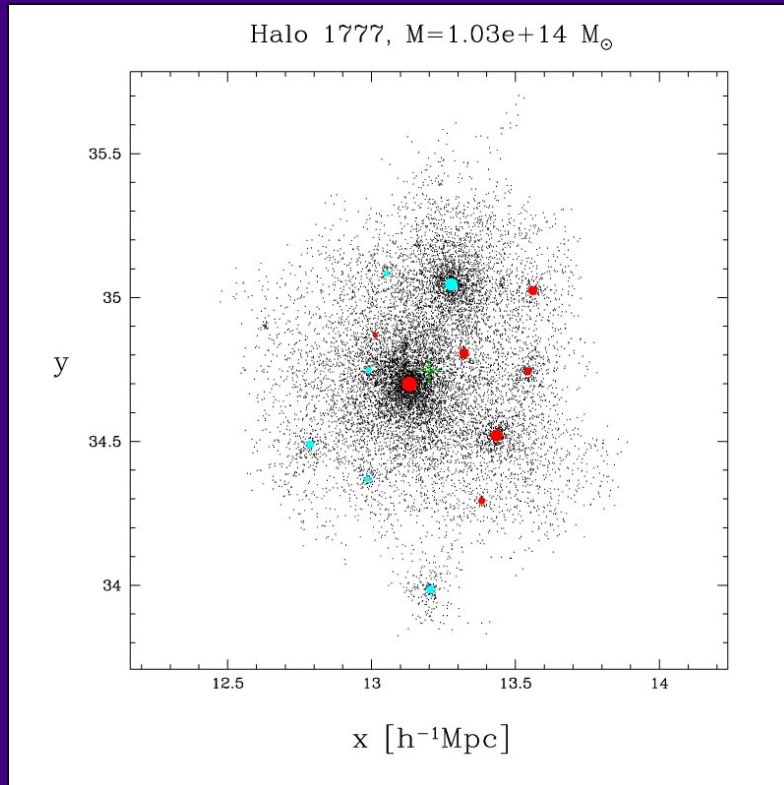
$$\langle N \rangle_M$$



Kravtsov, Berlind et al. (2004)

# How do we parameterize the HOD?

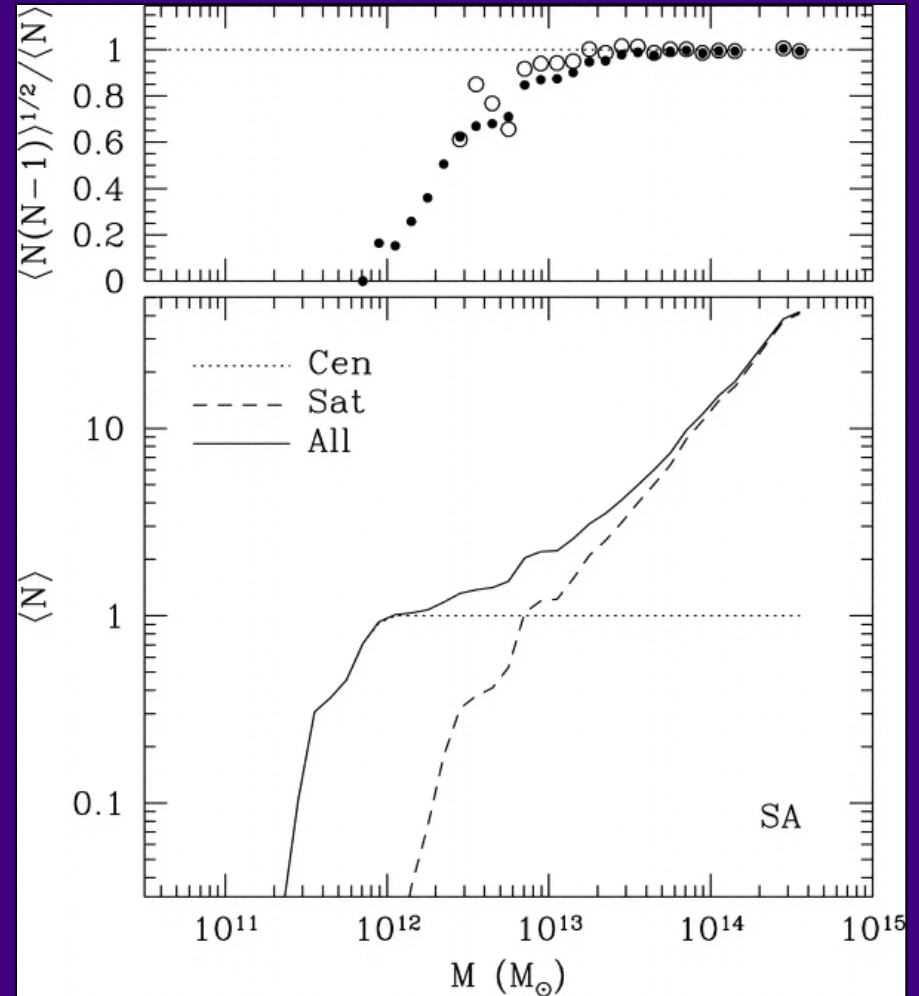
## SPH



Zheng, Berlind et al. (2005)

# How do we parameterize the HOD?

## Semi-Analytic



Zheng, Berlind et al. (2005)

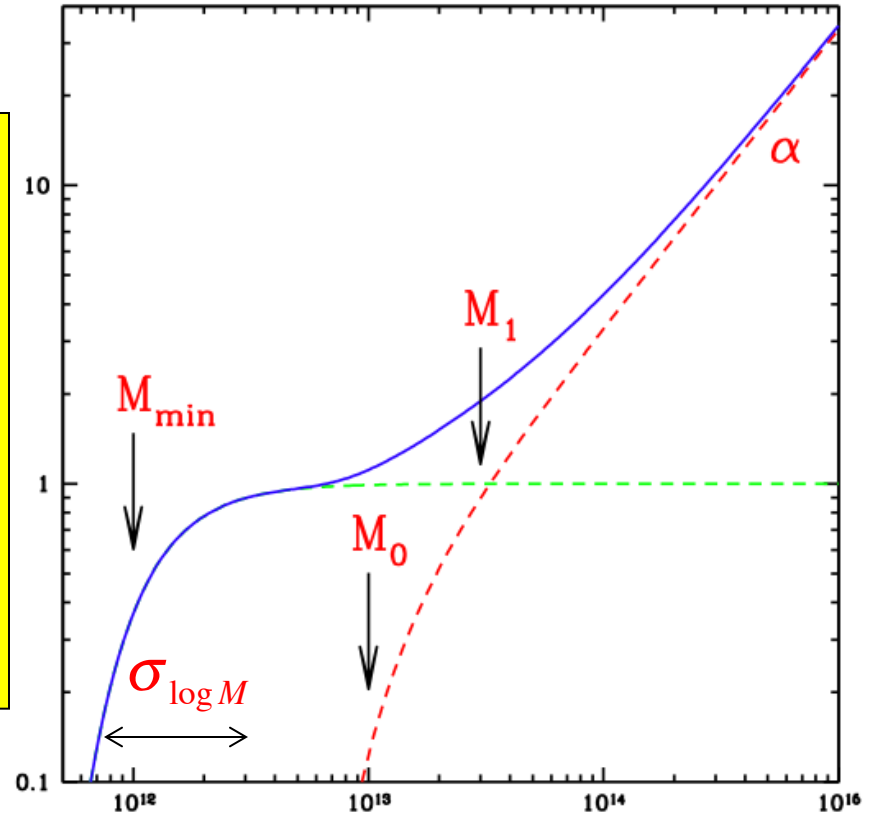


# How do we parameterize the HOD?

$$\langle N \rangle = \langle N_{cen} \rangle + \langle N_{sat} \rangle$$



Number of galaxies



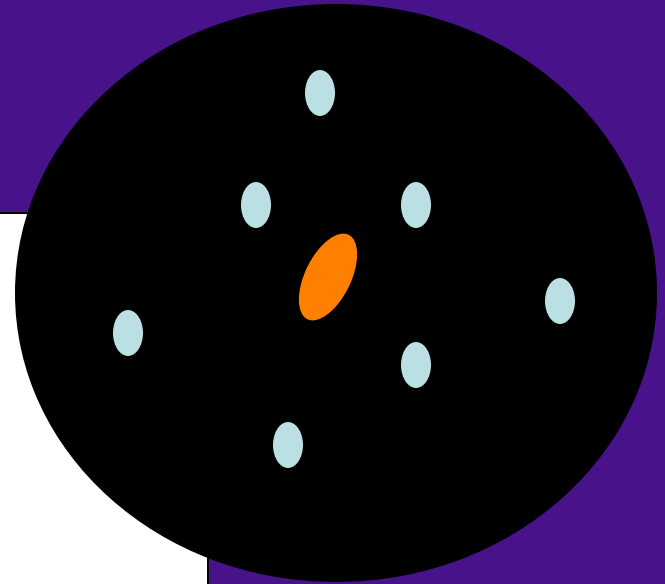
Halo Mass



# How do we parameterize the HOD?

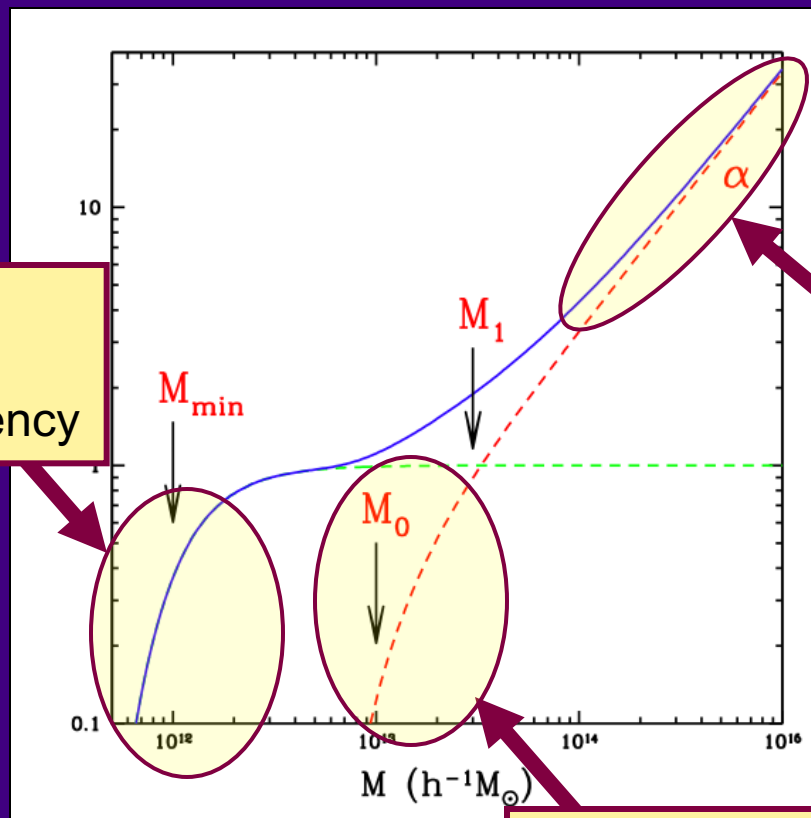
## Assume:

- Central galaxy resides at halo center
- Satellite galaxies trace the DM density distribution within the halo



# The HOD contains information about physics!

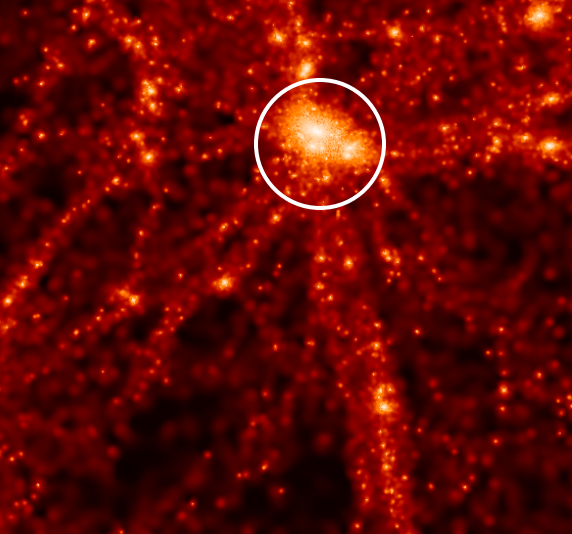
Baryon/DM fraction  
Gas cooling  
Star formation efficiency



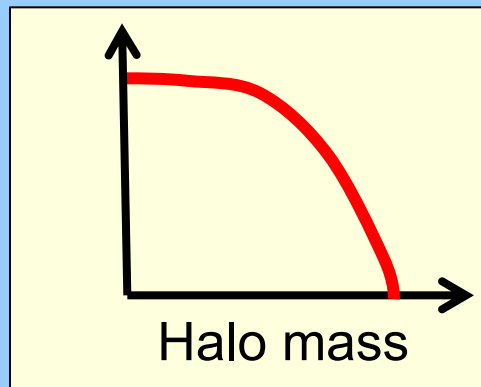
Dynamical friction  
Tidal disruption

DM halo merger statistics

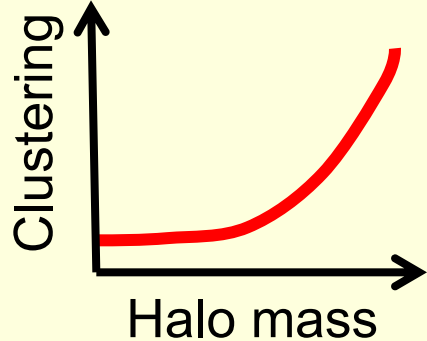
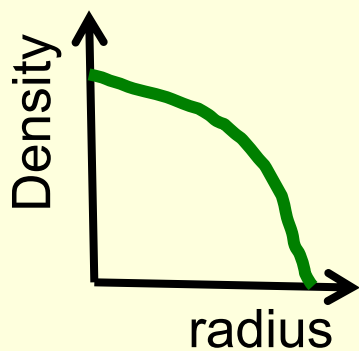
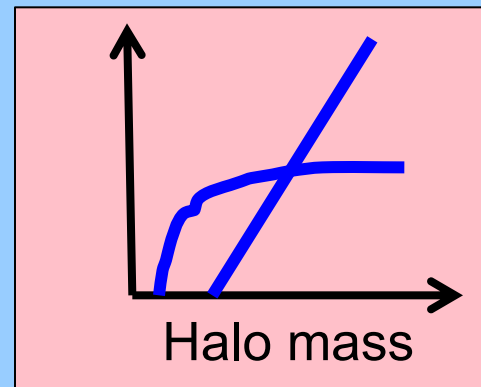
# The Analytic Halo Model



Abundance

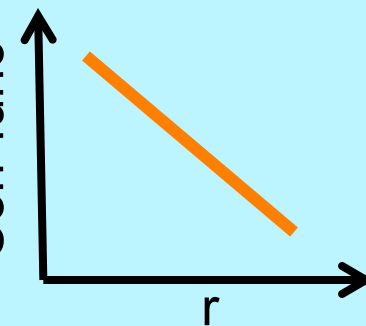


Number



Integrals  
over mass

Corr func



# How do we compute clustering statistics?

## Number density

$$n_g = \int_0^\infty dM \frac{dn}{dM} \langle N \rangle_M$$

# How do we compute clustering statistics?

## 2-point Correlation function

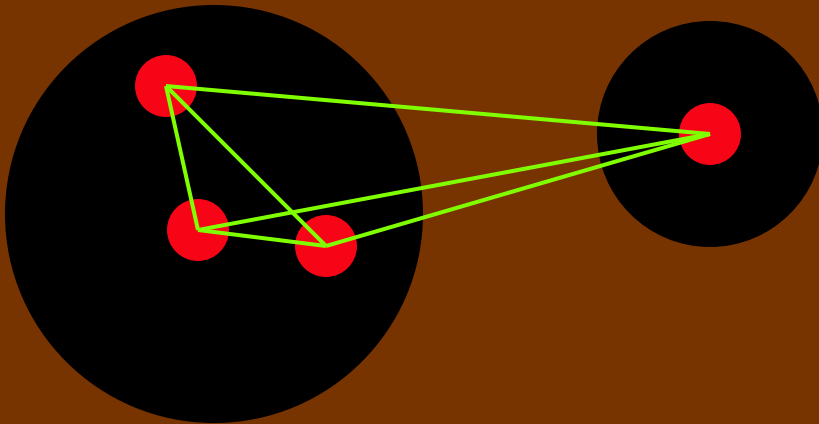
Small scales: All pairs come from same halo.  
*1-halo* term

$$1 + \xi_g^{1h}(r) = \left(2\pi r^2 n_g^2\right)^{-1} \int_0^\infty dM \frac{dn}{dM} \frac{\langle N(N-1) \rangle_M}{2} \lambda(r|M)$$

Large scales: Pairs come from separate halos.  
*2-halo* term

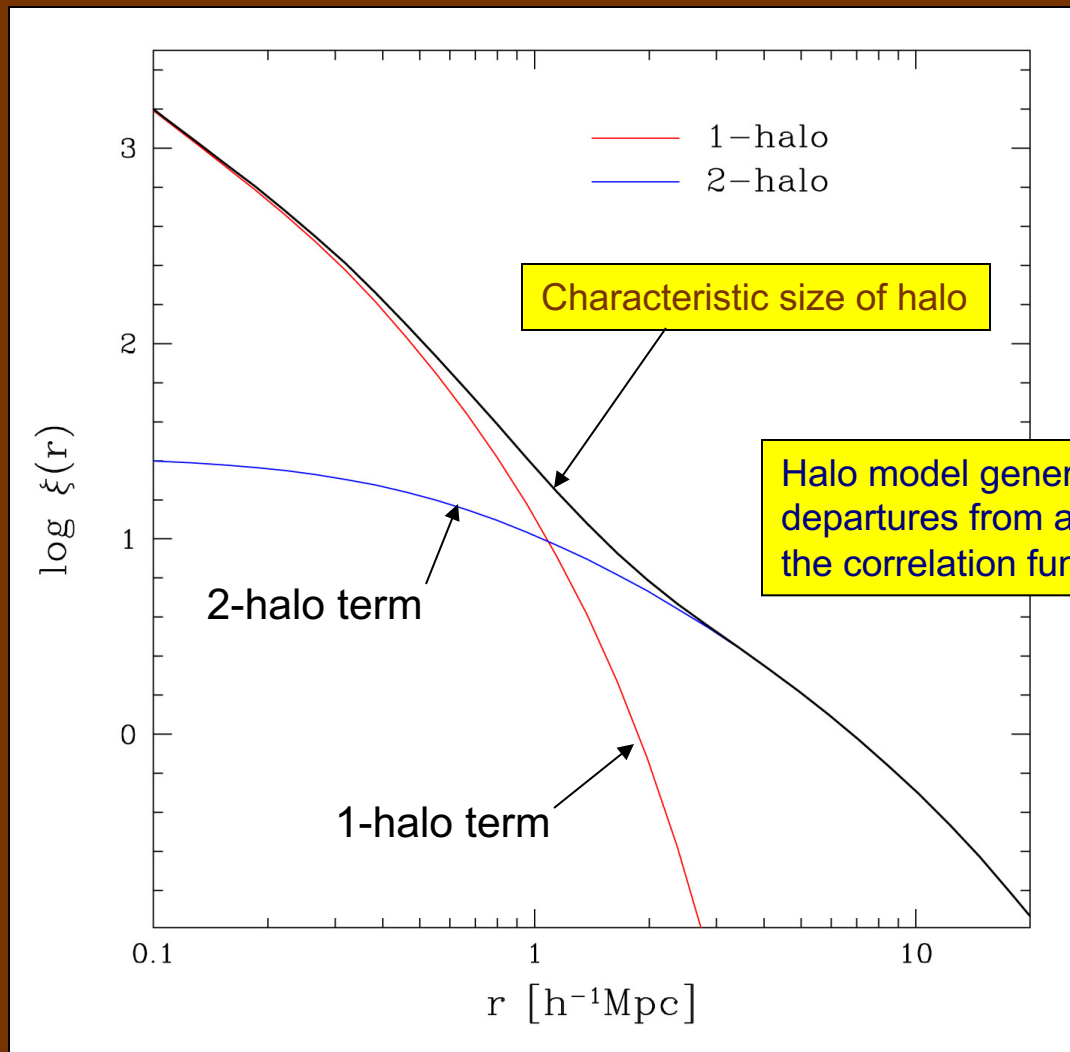
$$\xi_g(r) = b_g^2 \xi_m(r)$$

$$b_g = n_g^{-1} \int_0^\infty dM \frac{dn}{dM} \langle N \rangle_M b_h(M)$$



# How do we compute clustering statistics?

## 2-point correlation function



# How do we compute clustering statistics?

## N-point correlation functions

3-point function has 3 terms: 1-halo, 2-halo, 3-halo  
1-halo term depends on  $\langle N(N-1)(N-2) \rangle$

## Redshift-space and velocity statistics

Need model for velocity distribution in DM halo  
+ velocity bias for galaxies

## Luminosity function

$$\Phi(L) = \int_0^{\infty} dM \frac{dn}{dM} \langle N(M, L) \rangle$$



# How do we compute clustering statistics?

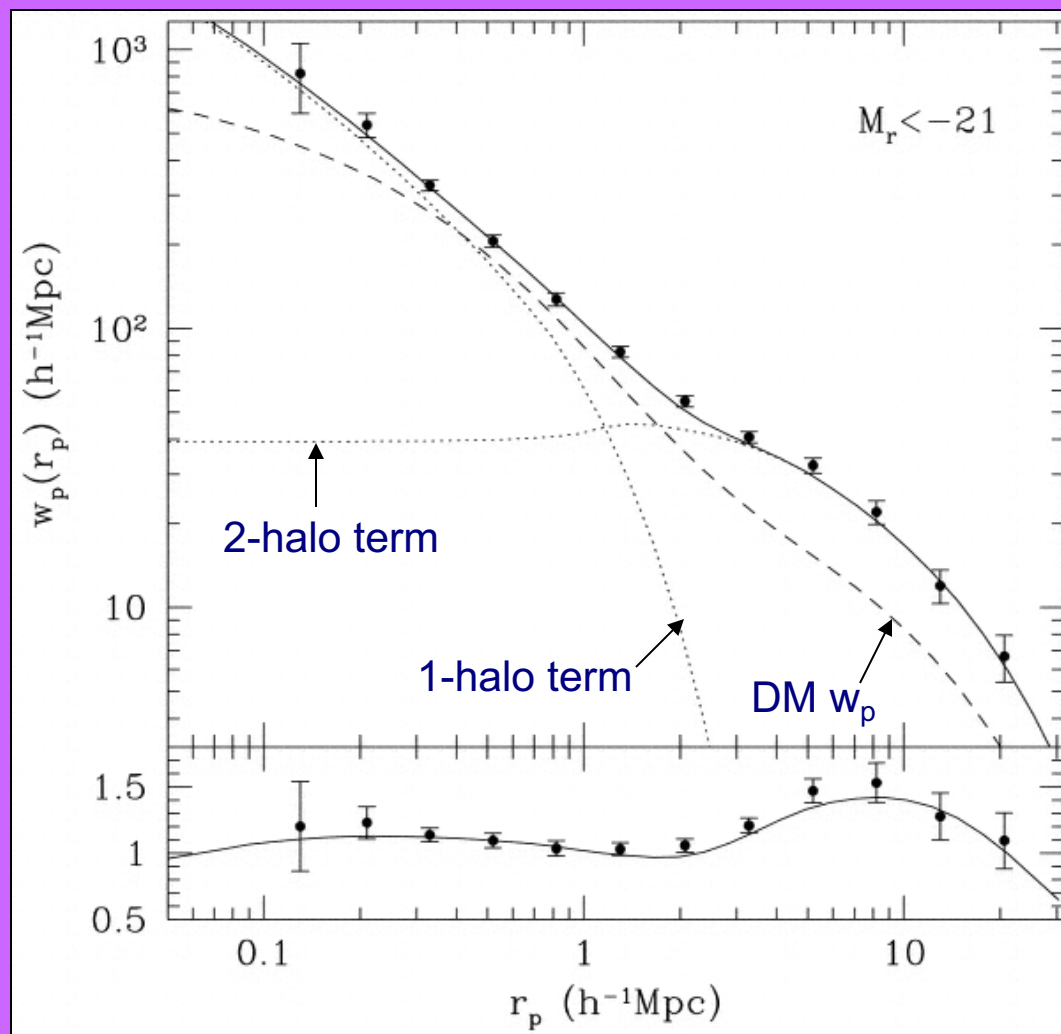
## Improvements to standard halo model

- Non-linear  $P(k)$  in 2-halo term
- Scale dependence of halo bias:  $b(M,r)$
- Halo exclusion
- Non-spherical halos
- Non-NFW profiles
- Dependence of  $b(M)$  and/or  $P(N|M)$  on halo assembly history
- Parameterize  $P(N|M)$  for non-trivial galaxy populations

# Measurements of the HOD

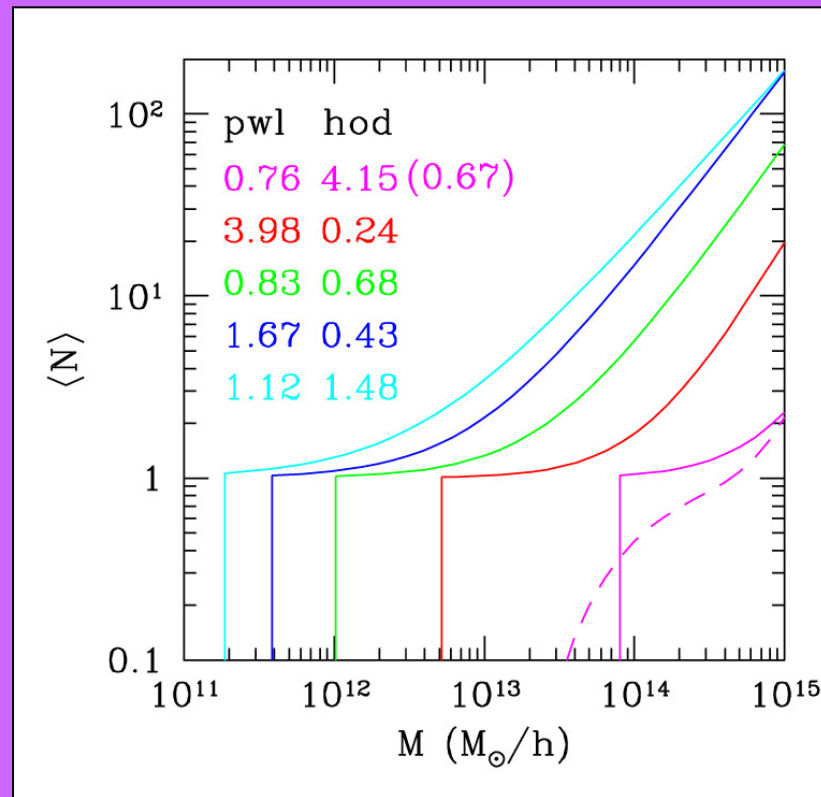
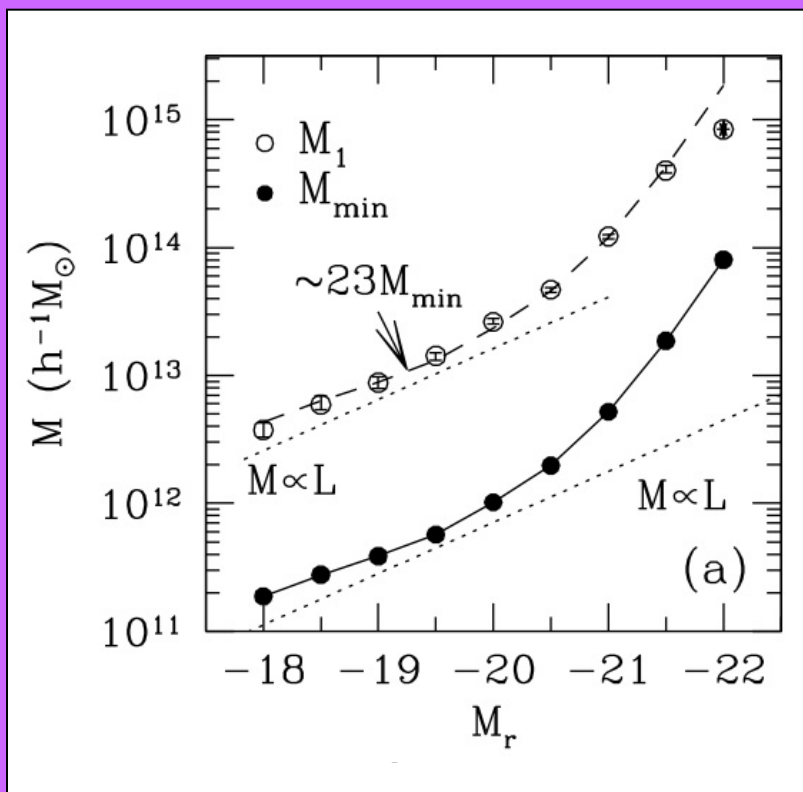


Deviation from power law detected. Halo model gives a good fit to the data.  
( $\chi^2/dof = 0.93$  vs.  $6.12$  for *plaw*)



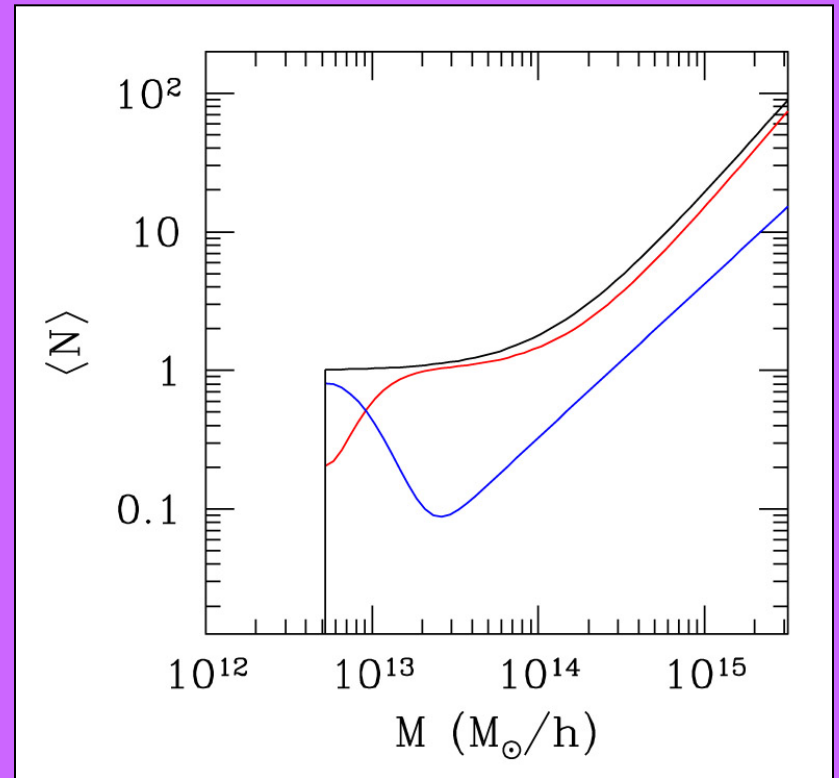
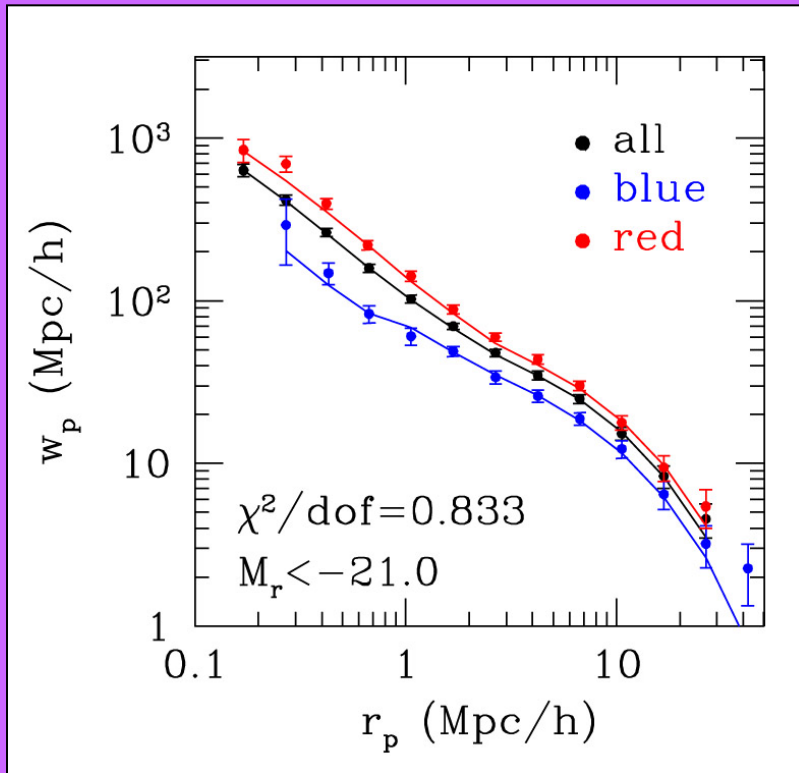
Zehavi et al. (2004)

# Measurements of the HOD



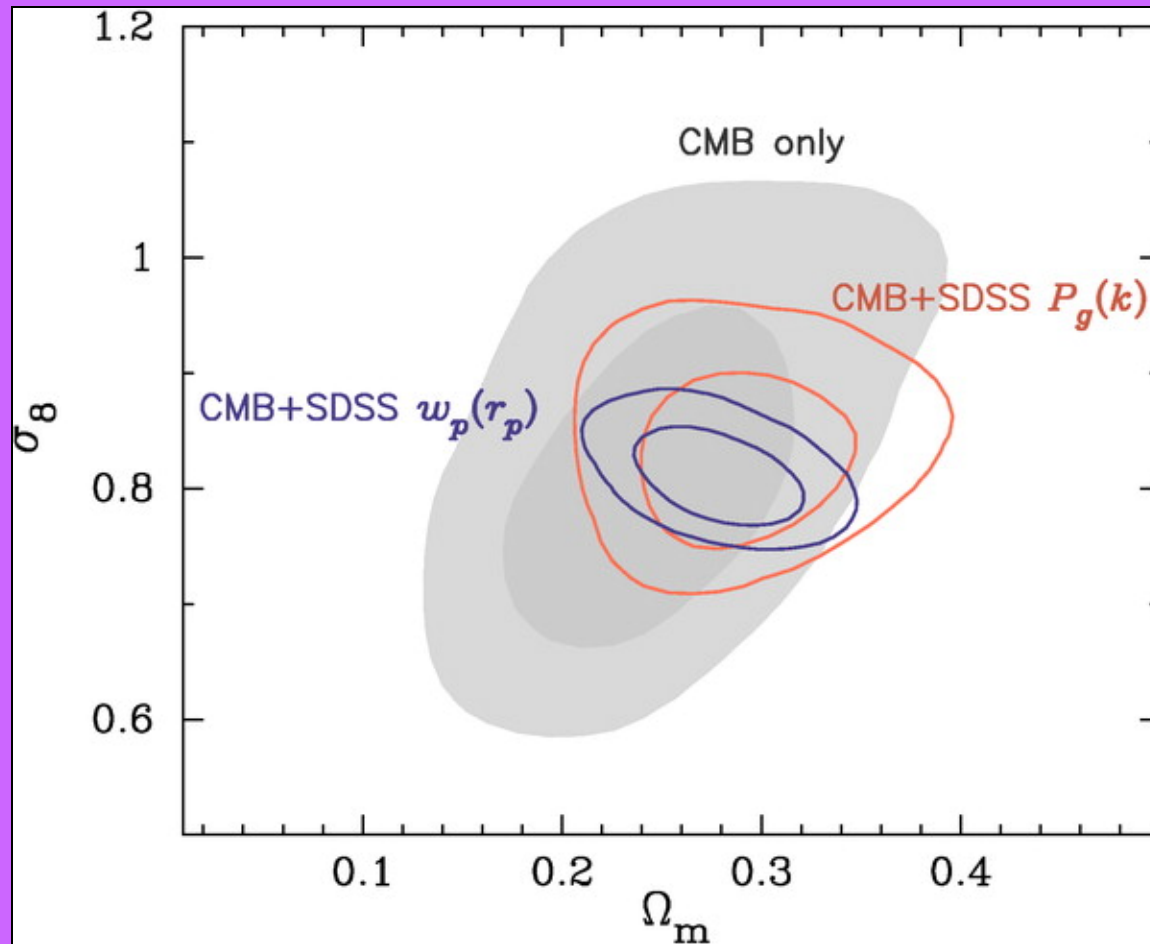
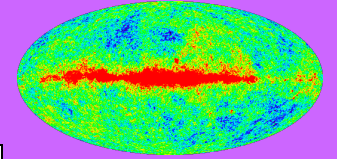
Zehavi et al. (2005)

# Measurements of the HOD



Zehavi et al. (2005)

# Measurements of cosmology



Abazajian et al. (2003)

# Testing the halo model assumptions

1. All galaxies live in halos. ▶
2. The statistical content of halos depends only on halo mass.  
i.e.,  $P(N|M)$  is sufficient, as opposed to  $P(N|M,X)$

Recent work shows that halo bias  $b_h(M)$  depends on halo assembly history at fixed mass. If  $P(N|M)$  also shows this dependence, then standard halo model will be incorrect.

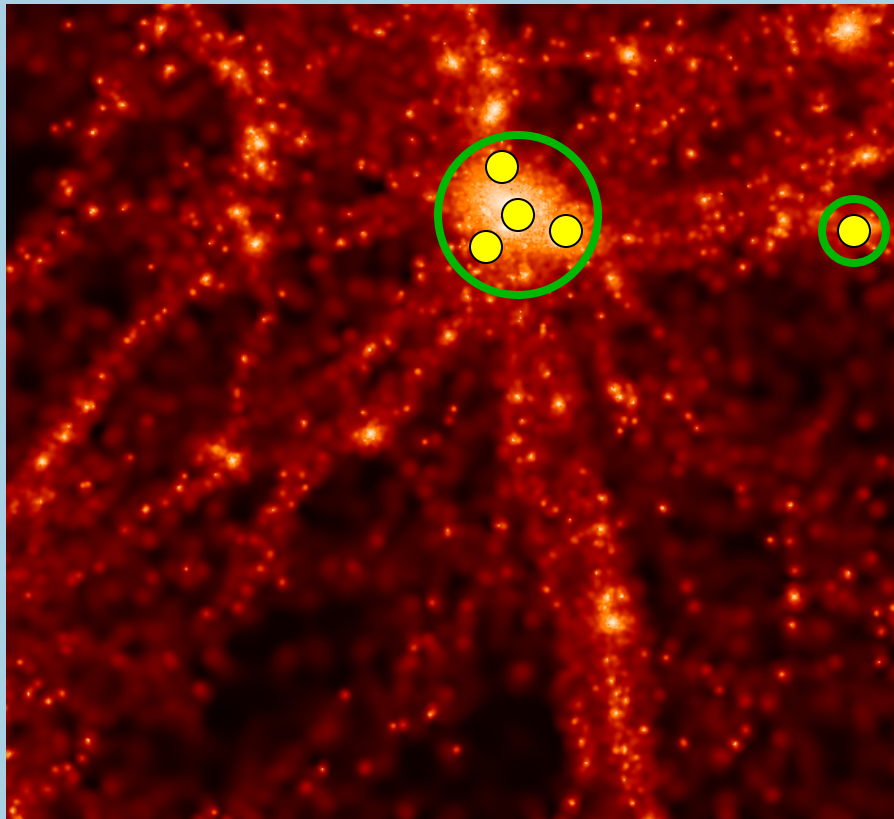
Measurements of this are not conclusive. This systematic effect needs to be addressed if galaxy clustering is to be used for precision cosmology.

3. The dark halo properties are not affected by baryons

This is almost certainly not true, but the extent of this problem is unclear.

## Alternative to the analytic halo model approach

Populate an N-body simulation with an HOD to compute clustering statistics instead of using analytic formulas.



## Alternative to the analytic halo model approach

Populate an N-body simulation with an HOD to compute clustering statistics instead of using analytic formulas.

### Advantages:

- Halo clustering, abundances, and profiles are correct on all scales above the simulation's resolution limit.
- Can calculate any clustering statistic.

### Disadvantages:

- Not good for very small scale clustering.
- Much more computationally intensive.



## Alternatives to the halo model / HOD approach

Use a Conditional Luminosity Function (CLF) to model the luminosity dependence of clustering.

$$\Phi(L) = \int_0^{\infty} dM \frac{dn}{dm} \Phi(L|M) \quad \langle N \rangle_M = \int_{L_{\min}}^{\infty} dL \Phi(L|M)$$

### Advantages:

- Don't have to assume a form for  $\langle N(M) \rangle$
- More ambitious: model the luminosity dependence explicitly

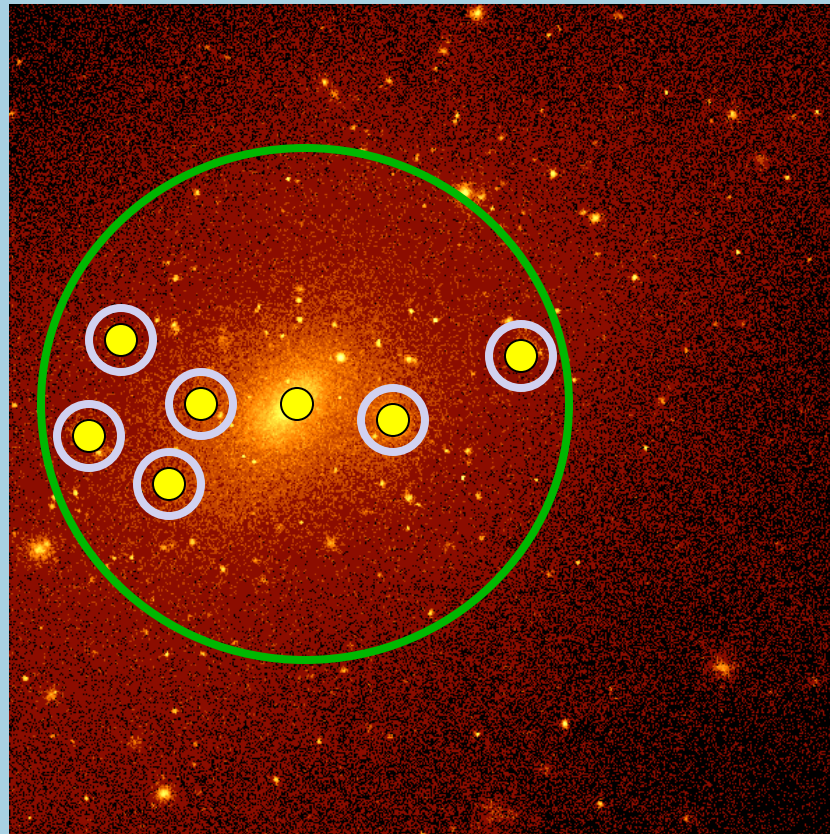
### Disadvantages:

- Have to assume a form for  $\phi(L|M)$
- More ambitious: luminosity dependence is model dependent

Methods are very similar and complementary.

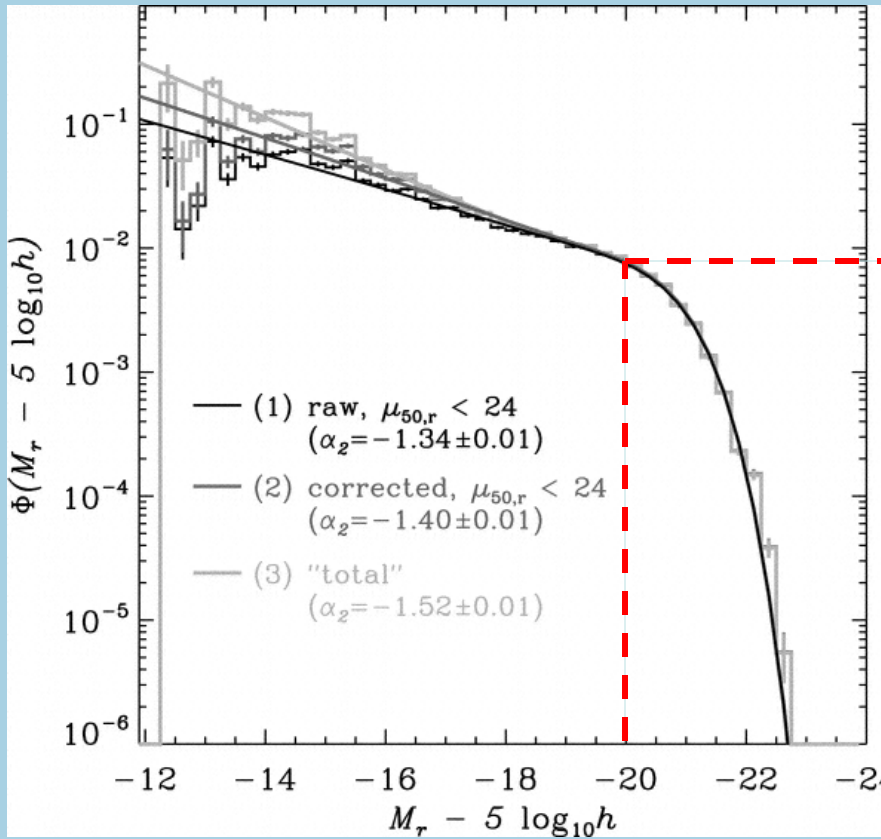
## Alternatives to the halo model / HOD approach

Use a high resolution N-body simulation to place galaxies in halos + subhalos, assuming relations between galaxy and subhalo properties. (i.e., use subhalo distribution instead of HOD)

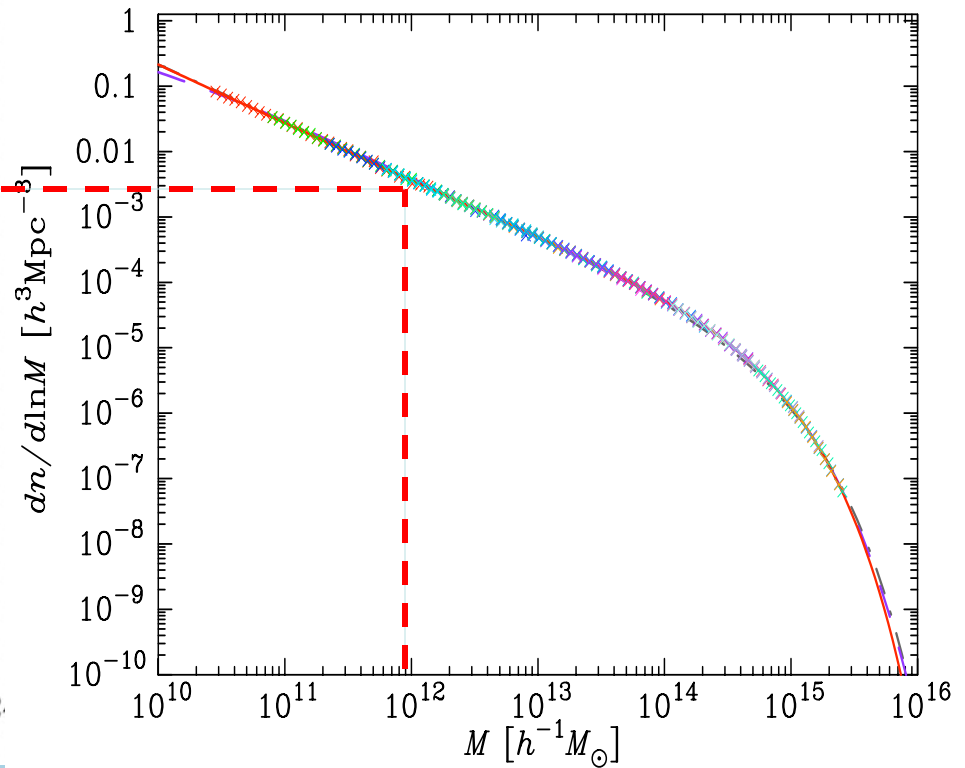


# Halo/Subhalo Abundance Matching

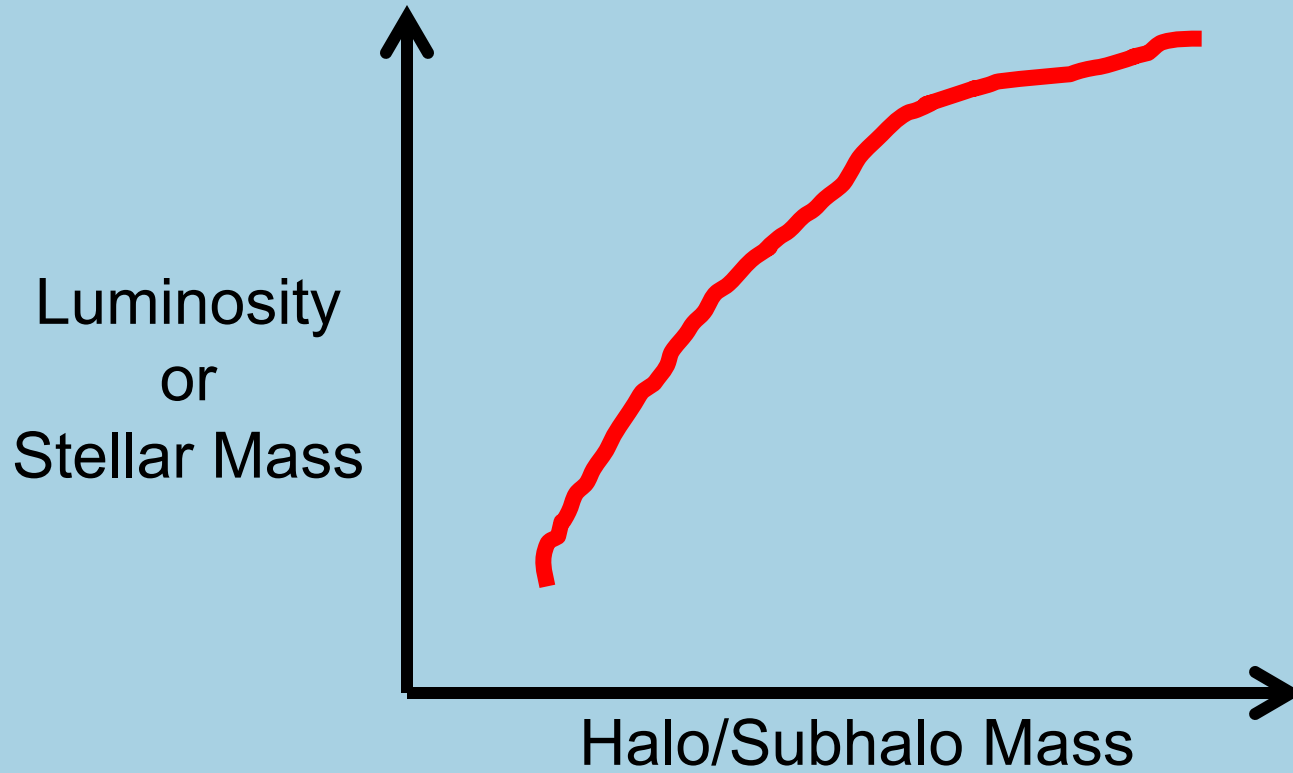
## Galaxy luminosity function



## Halo mass function (including subhalos)

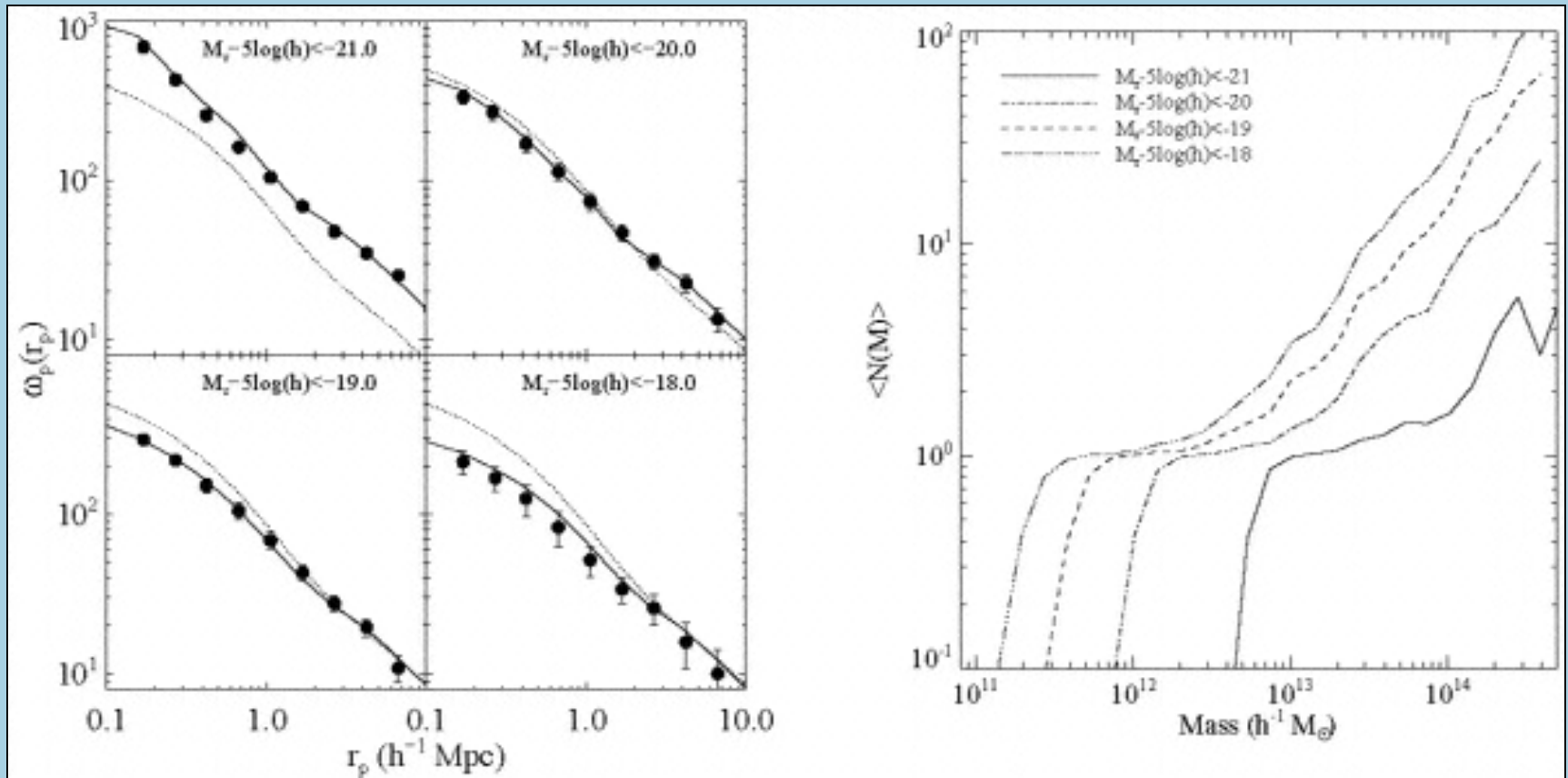


# Halo/Subhalo Abundance Matching



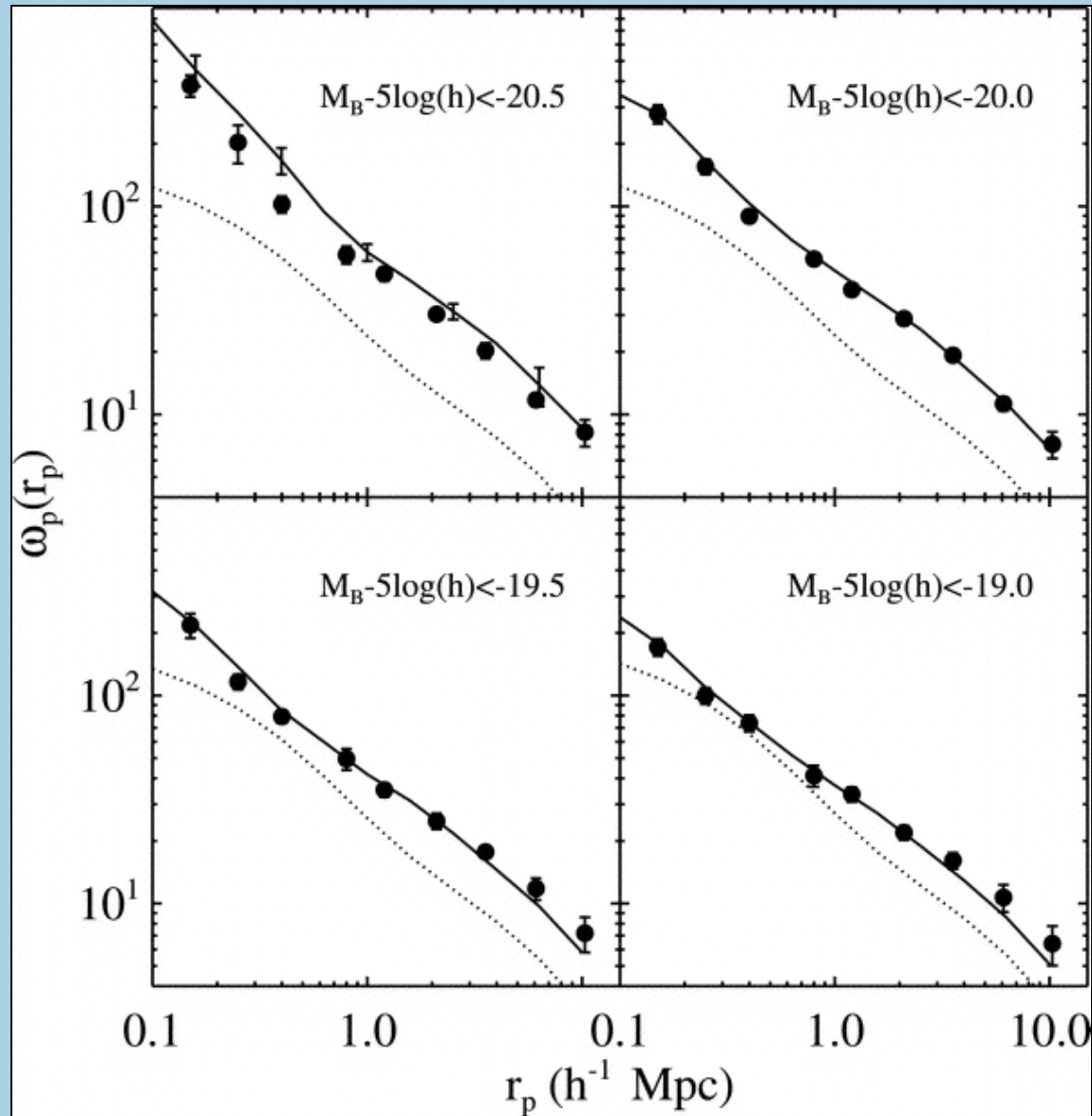
# Halo/Subhalo Abundance Matching

SDSS  
 $z \sim 0$



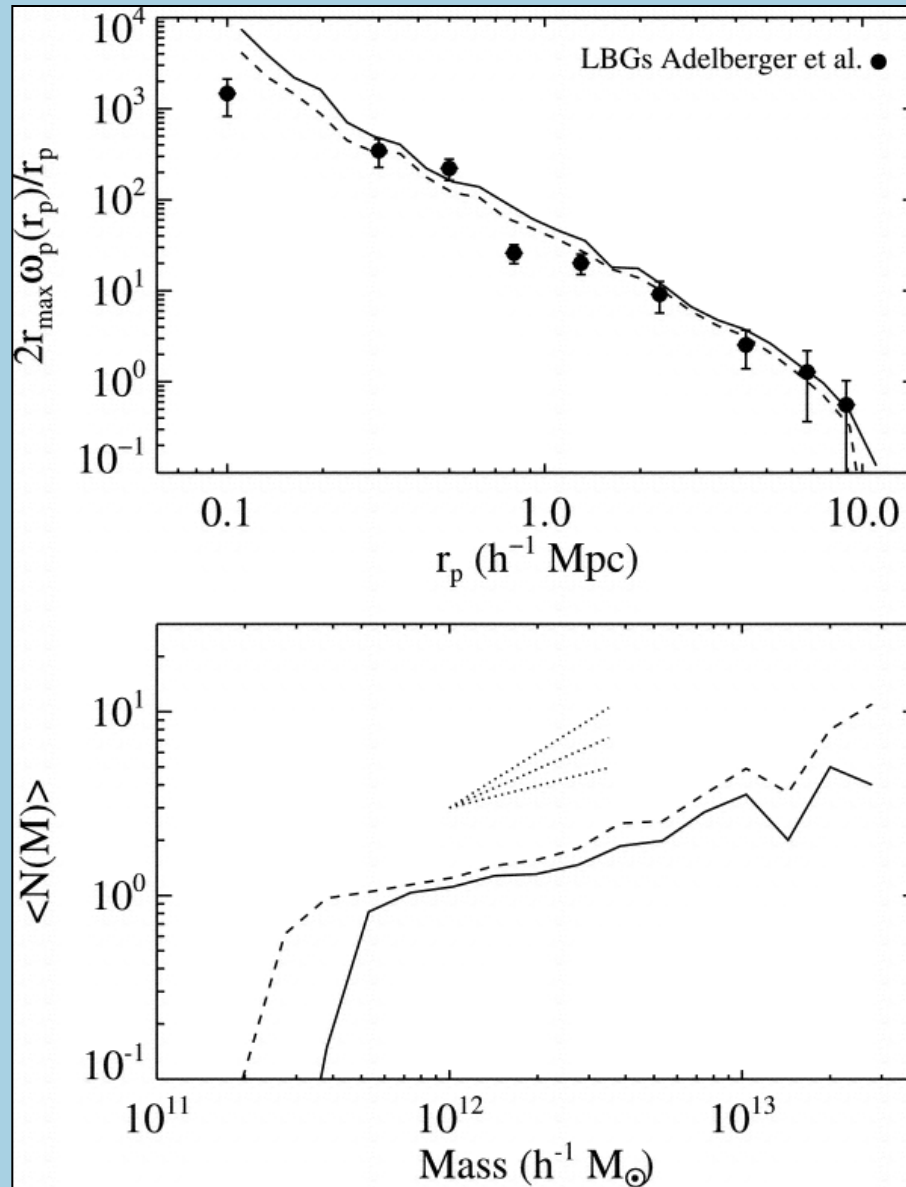
Conroy et al. (2006)

# Halo/Subhalo Abundance Matching



DEEP2  
 $z \sim 1$

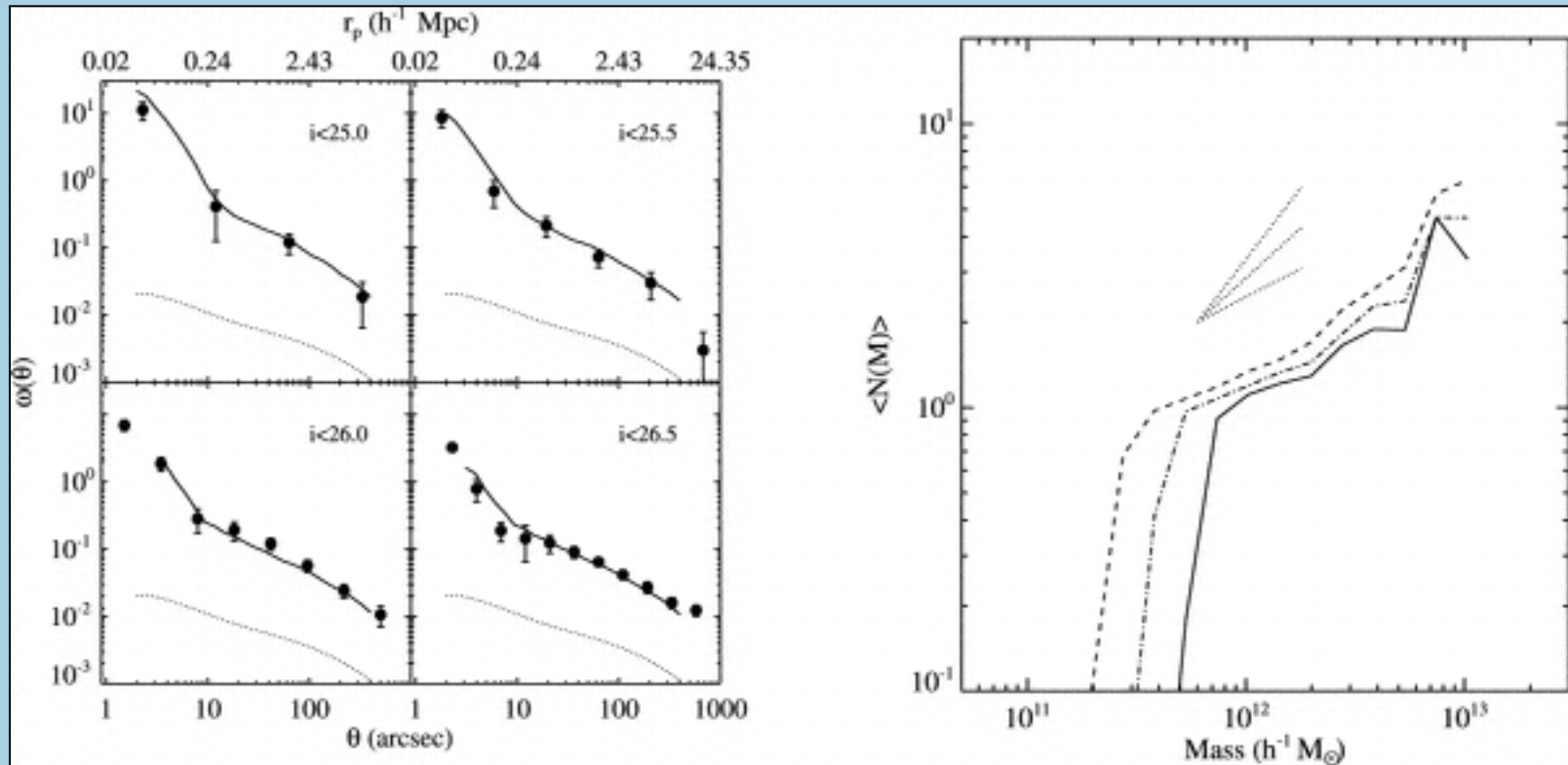
# Halo/Subhalo Abundance Matching



LBGs  
 $z \sim 3$

# Halo/Subhalo Abundance Matching

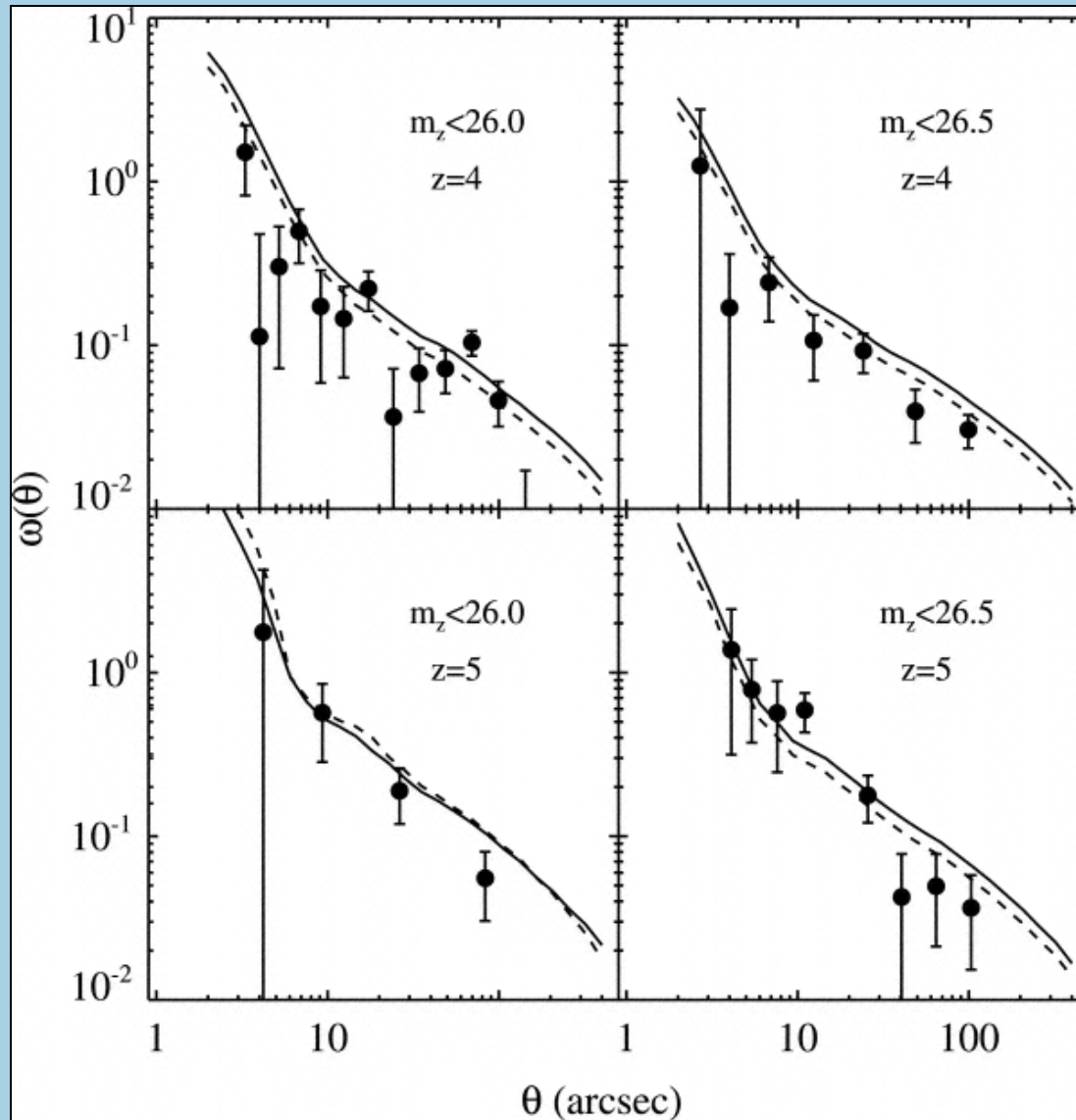
Subaru  
 $z \sim 4$



Conroy et al. (2006)



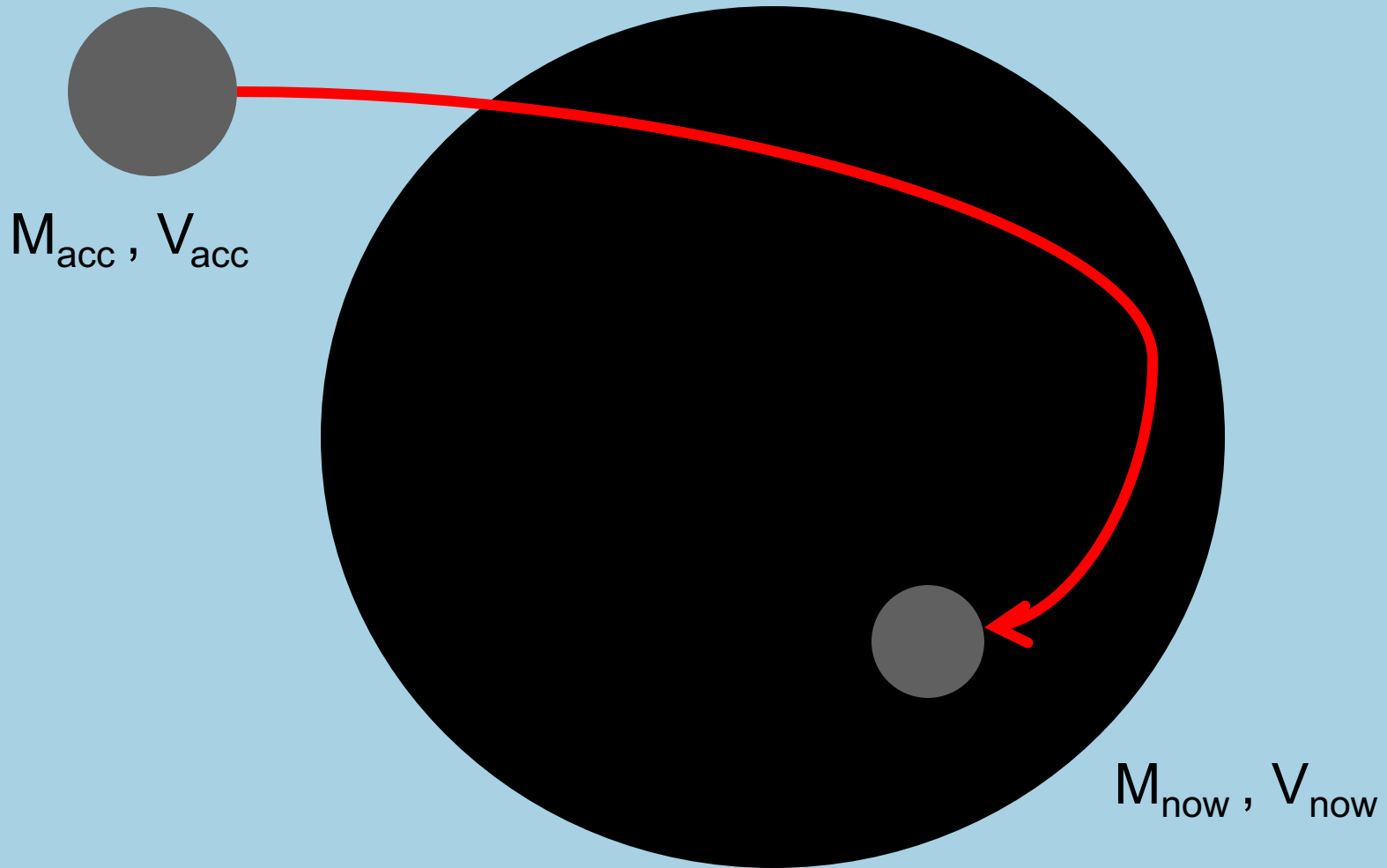
# Halo/Subhalo Abundance Matching



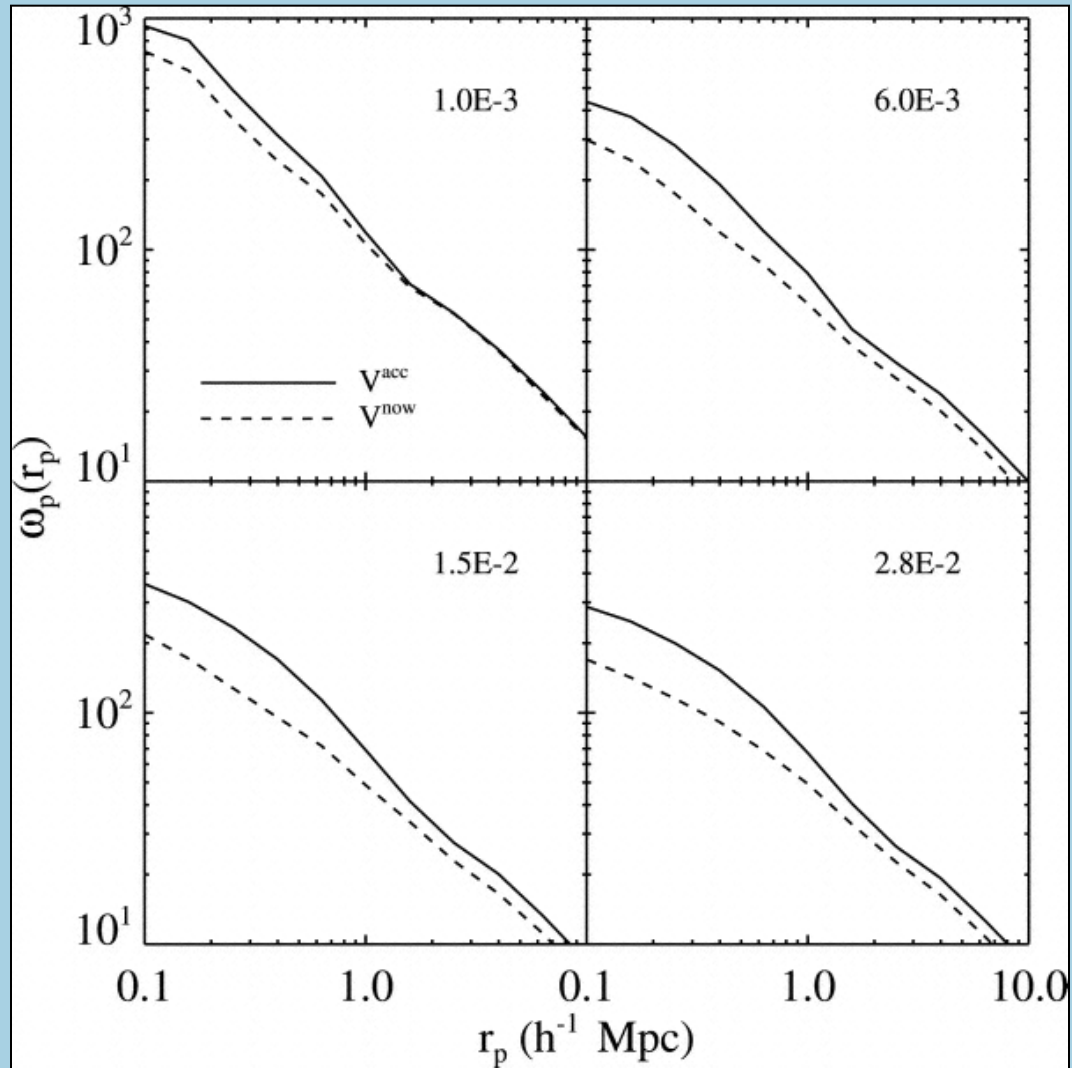
GOODS  
 $z \sim 4-5$

# Halo/Subhalo Abundance Matching

What subhalo property should be used?

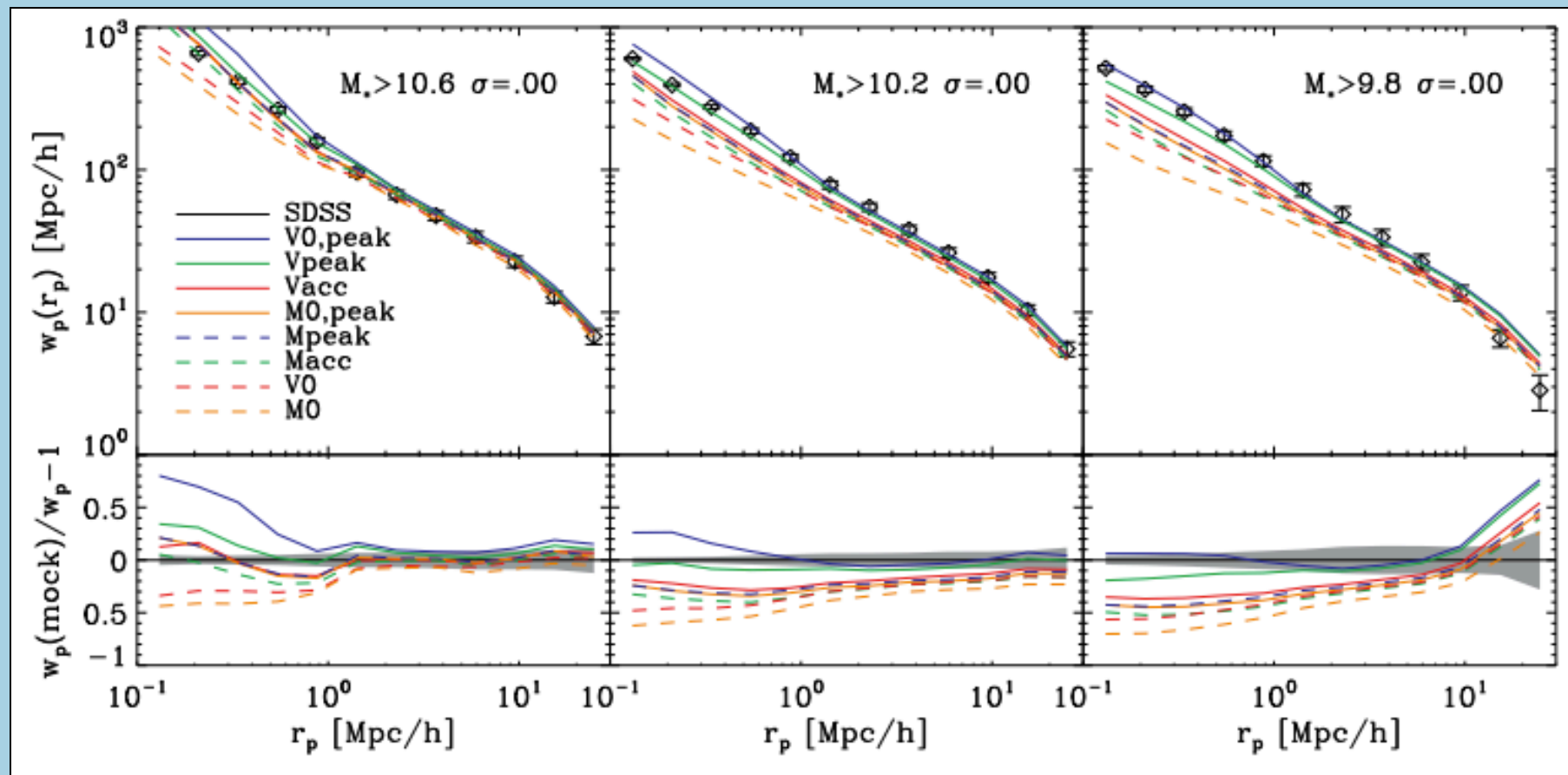


# Halo/Subhalo Abundance Matching



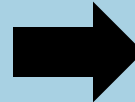
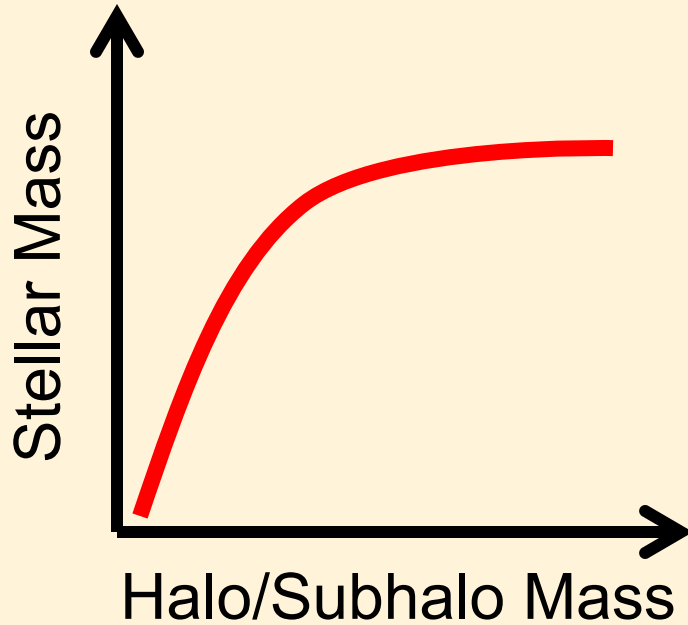
Conroy et al. (2006)

# Halo/Subhalo Abundance Matching

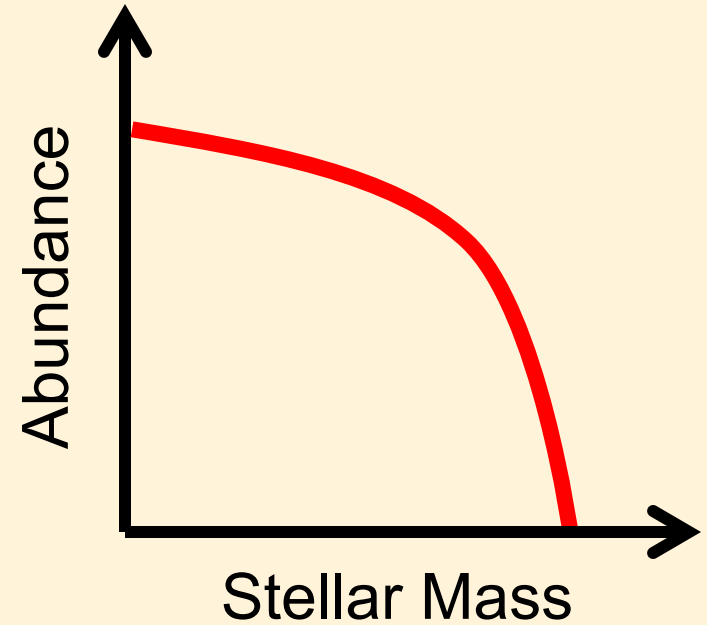


# Or do a forward approach

Parameterize this



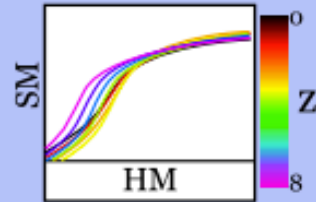
Predict this



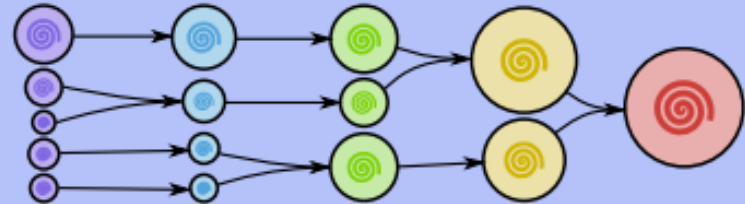
# The modeling is getting very ambitious

Markov Chain Monte Carlo

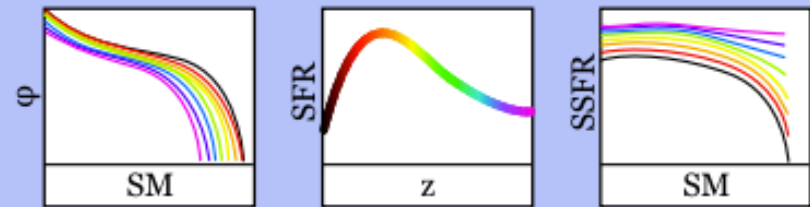
1. Choose a stellar mass - halo mass (SMHM) relation from parameter space.



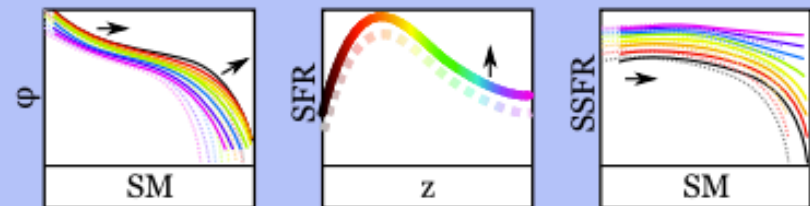
2. Find galaxy growth histories by applying the SMHM relation to dark matter merger trees.



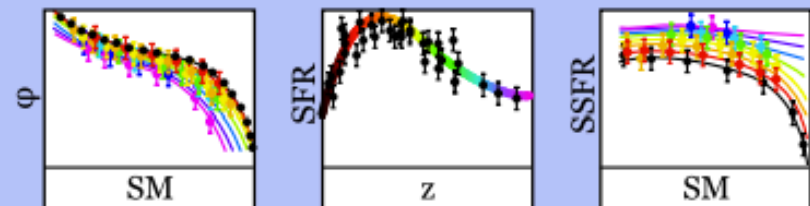
3. Derive the inferred stellar mass functions and star formation rates.



4. Apply effects to simulate observational errors and biases.



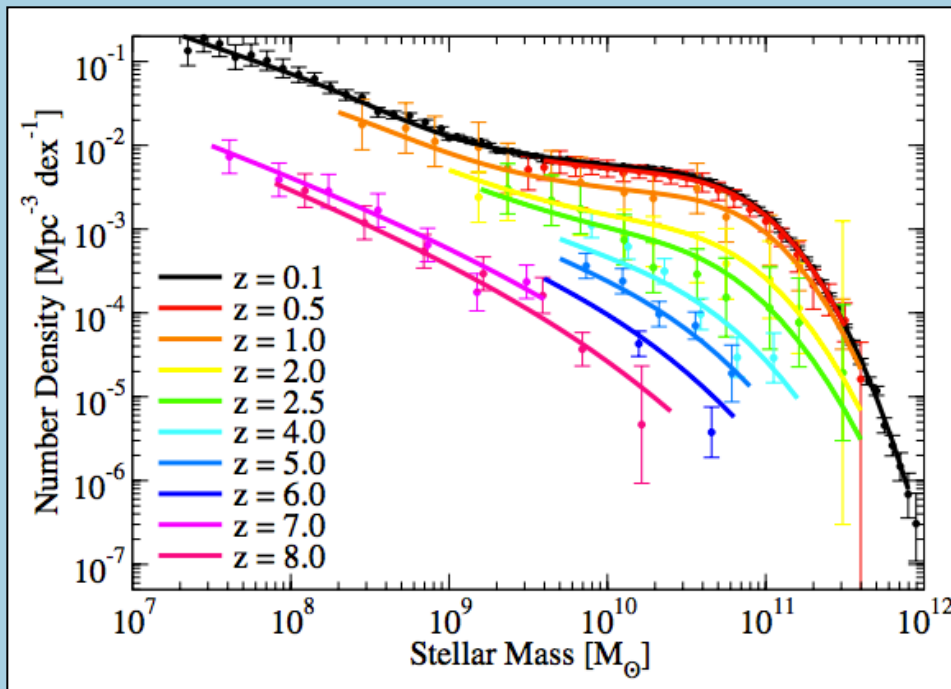
5. Compare to data and calculate likelihood of the chosen SMHM relation.



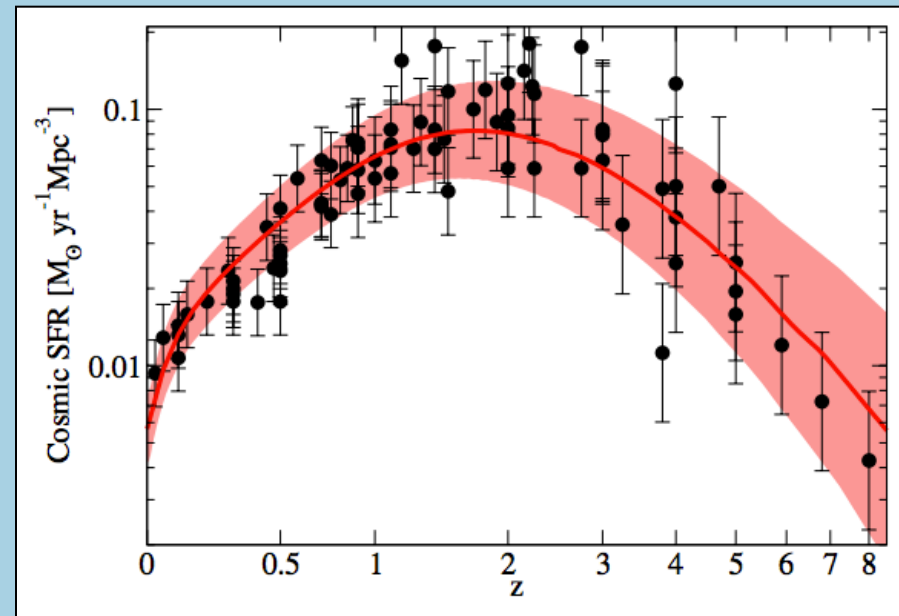
# The modeling is getting very ambitious

Fit model at all redshifts to:

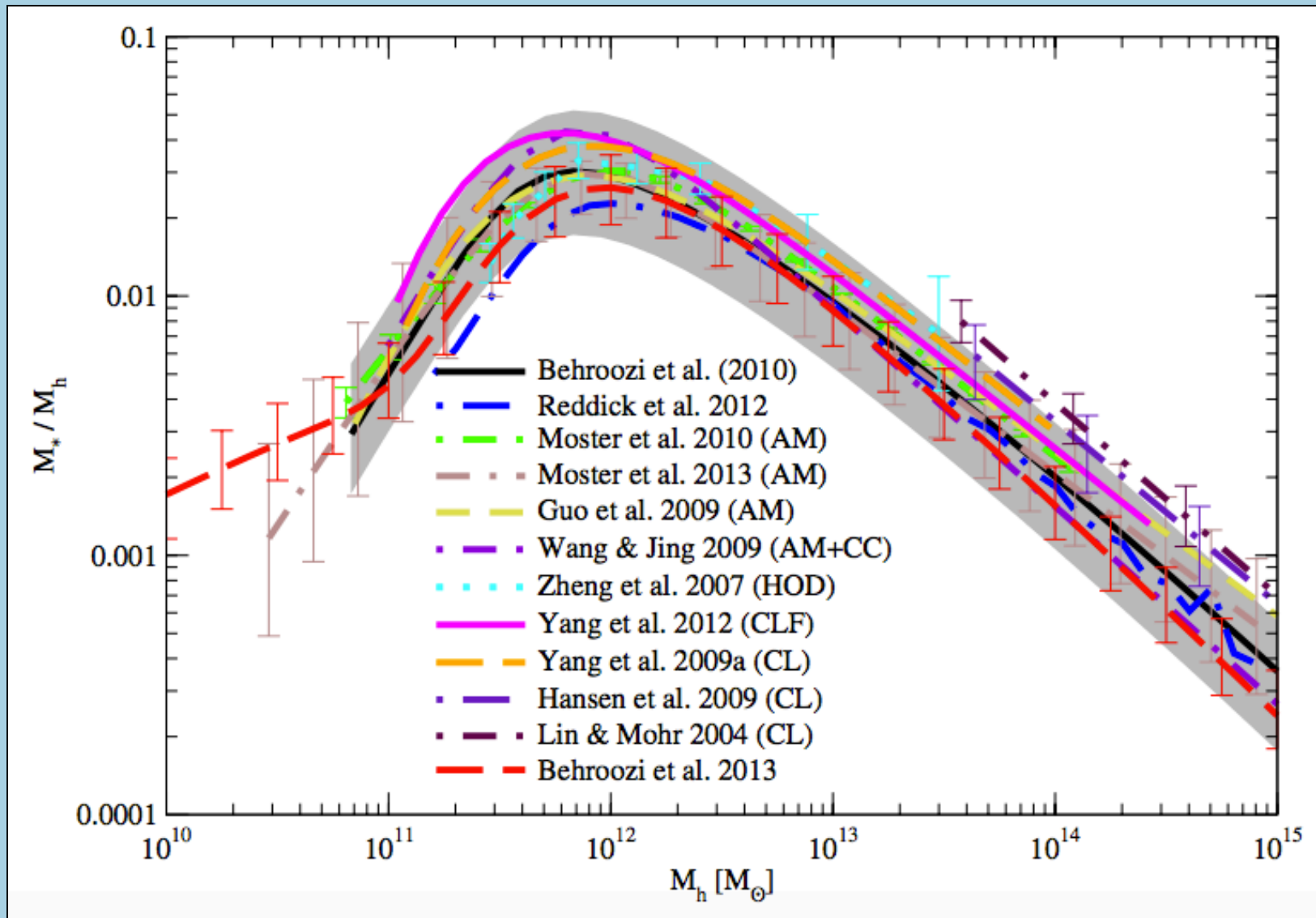
(1) stellar mass function



(2) star formation rate



# The modeling is getting very ambitious





# Describing vs. Understanding

HOD/HAM/CLF are excellent statistical tools for *describing* the wealth of galaxy clustering data: for translating complicated statistics into a more physically informative language.

It is still essential that we *understand* the physics behind the data: gas cooling, star formation, feedback, etc. For this we need ab-initio models such as hydrodynamic simulations and semi-analytic models.

The methods are highly complementary.

# SYNOPSIS

- Galaxy properties
- Stellar populations
- Distance measures
- Hubble expansion and z-space distortions
- Redshift surveys
- Galaxy environments
- Galaxy groups and clusters
- Galaxy clustering statistics
- Cosmological parameters
- Expansion history of the universe
- Growth of perturbations
- N-body simulations
- Dark matter halos
- Galaxy formation
- The halo model