## Coordinate Transforms

## Equatorial and Cartesian Coordinates

- Consider the unit sphere ("unit": i.e. the distance from the center of the sphere to its surface is $r=1$ )
- Then the equatorial coordinates can be transformed into Cartesian coordinates:

$$
\begin{aligned}
-\mathrm{x} & =\cos (\alpha) \cos (\delta) \\
-\quad y & =\sin (\alpha) \cos (\delta) \\
\mathrm{z} & =\sin (\delta)
\end{aligned}
$$



- It can be much easier to use Cartesian coordinates for some manipulations of geometry in the sky


## Equatorial and Cartesian Coordinates

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## Precession

- Because the Earth is not a perfect sphere, it wobbles as it spins around its axis
- This effect is known as precession
- The equatorial coordinate system relies on the idea that the Earth rotates such that only Right Ascension, and not declination, is a time-dependent coordinate



## The effects of Precession

- Currently, the star Polaris is the North Star (it lies roughly above the Earth's North Pole at $\delta=90^{\circ} \mathrm{N}$ )
- But, over the course of about 26,000 years a variety of different points in the sky will truly be at $\delta=90^{\circ} \mathrm{N}$
- The declination coordinate is time-dependent albeit on very long timescales
- A precise astronomical coordinate system must account for this effect


## Equatorial coordinates and equinoxes

- To account for precession, the equatorial coordinate system being used by an astronomer is always specified to be "at a certain time in history"
- For instance "2000.0" would specify coordinates in a system when the Earth's precession made the (distant) night sky look as it was at midnight on Jan 1, 2000
- Because the equatorial coordinate system is set by the position of the Sun on the Vernal Equinox, this specification (e.g., 2000.0) is called an equinox
- A point in the sky at $\alpha=12: 34: 56.78, \delta=+01: 23: 45.6$, 2000.0 is a slightly different point in the sky to $\alpha=$ $12: 34: 56.78, \delta=+01: 23: 45.6,1950.0$


## Equatorial coordinates and equinoxes

- Precession is such a small effect that the system is only re-specified every 50 years or so
- When I was in grad school, I once accidentally used B1950.0 coordinates at a telescope and wasted hours
- the $B$ here stood for a now-obsolete way of measuring epochs called the Besselian system
- Astronomers currently use the equinox $J 2000.0$
- the $J$ here denotes Julian date
- It is possible that in our lifetimes the International Astronomical Union will initiate a switch to J2050.0 coordinates


## Equatorial coordinates and equinoxes

- Note that although coordinates are specified using a certain equinox, the true equinox is always changing
- precession doesn't just stop between 1950 and 2000 and then again between 2000 and 2050
- So one might list coordinates of stars as J2000.0 in a publication, and might take them to a telescope to make observations in February, 2022
- The telescope control software then takes account of precession and rotates your coordinates until they are at a coordinate system with an equinox of $J 2022.2$
- The equinox in which coordinates are expressed by astronomers is almost never the true, current equinox


## Rotations

- The method to precess coordinates to a new equinox is a common approach to coordinate transforms
- The general approach is to define (and measure) a rotation matrix, R that transforms between systems as

$$
\begin{array}{r}
-\left(\mathrm{x}_{2}, \mathrm{y}_{2}, \mathrm{z}_{2}\right)=\begin{array}{r}
\left(\mathrm{x}_{1}\right) \\
\mathrm{R}\left(\mathrm{y}_{1}\right) \\
\left(\mathrm{z}_{1}\right)
\end{array}
\end{array}
$$

- e.g., to precess coordinates from B1950 to J2000:

- The approach is then, as before, to convert from $(\alpha, \delta)$ to ( $\mathrm{x}, \mathrm{y}, \mathrm{z}$ ) apply R and convert back to the new $(\alpha, \delta)$


## Rotations and Galactic Coordinates

- There are many common coordinate transformations in astronomy, each with its own rotation matrix
- For instance, Galactic coordinates are centered on the

NP of Galaxy Sun. The longitude is called $\ell$ and the latitude $b$. The disk of our Galaxy is the "equator" (i.e. the equatorial plane $) ;(\ell, b)=\left(0^{\circ}, 0^{\circ}\right)$ towards the Galactic center and $(\ell, b)=\left(0^{\circ}, 90^{\circ}\right)$ towards the Galactic North Pole

- Another common system is the ecliptic coordinate system, in which the equatorial plane is the ecliptic, the plane in which all of the planets orbit the Sun


## Python tasks (all of these use astropy.coordinates!)

1. Convert an RA and a dec to Cartesian coordinates (xyz)

- c.representation_type = 'cartesian' converts an RA/dec SkyCoord to Cartesian coordinates, 'spherical' will transform back. c.cartesian will print in cartesian.
- Check the SkyCoord result agrees with my equations

2. Calculate the $(\alpha, \delta)$ of the center of our Galaxy

- In what constellation is the Galactic Center? Is it near the center or edge (qualitatively) of that constellation (see the syllabus links for constellation positions/maps)?
- Consider the frame option and transform_to(). Also see get_constellation().

3. For Nashville, $\delta=36^{\circ} \mathrm{N}$. Plot how ( $\ell, b$ ) changes through the year directly above your head

## Python tasks (all of these use astropy.coordinates!)

4. Current $(\alpha, \delta)$ for the planets are available with astropy.Time and astropy.get_body(). Plot the positions of Mercury, Venus, and Mars in ecliptic ('heliocentrictrueecliptic'in astropy) coordinates
